## QUIZ #3 – MATH 2200 SPRING 2018

## FEBRUARY 23RD, 2018

**1.** Let  $S = \mathbb{R}_{>0}$  and let  $T = \{n^2 \mid n \in \mathbb{Z}_{>0}\}.$ 

(a) Is S finite, countably infinite or uncountable?

(b) Is T finite, countably infinite or uncountable?

(c) Is S - T finite, countably infinite or uncountable?

(d) Is T - S finite, countably infinite or uncountable?

You don't need to justify your answer, but it might be helpful to recall the following facts that we proved in the worksheet on countability.

(i) If A and B are countably infinite sets, then so is  $A \cup B$ .

(ii) If A and B are countably infinite sets, then so is  $A \times B$ .

(iii) If A is uncountable and  $B \subseteq A$  is countably infinite, then A - B is uncountable.

(iv) If A and B are uncountable, it is possible that A - B is finite, or countably infinite, or uncountable (it just depends on what the sets are).

(v) For any set S,  $|S| \neq |\mathcal{P}(S)|$ .

**2.** Let  $S = \mathbb{R}$ . We define a relation on  $\mathbb{Q}$  as follows.  $a \sim b$  if and only if a + b = 0. Is ~ symmetric, transitive, or reflexive? Make sure to justify your answer with a proof (if it is) or with a counter-example (if not).

**3.** Suppose that  $f: A \to B$  and  $g: B \to C$  are surjective functions. Prove carefully that  $g \circ f$  is also surjective.