

§9

The domain of $f: \mathbb{R}^n \rightarrow \mathbb{R}$ are those $p \in \mathbb{R}^n$ for which $f(p)$ makes sense.

The graph of $f: \mathbb{R} \rightarrow \mathbb{R}$ are those $(x, y) \in \mathbb{R}^2$ such that $f(x) = y$.

The graph of $g: \mathbb{R}^2 \rightarrow \mathbb{R}$ are those (x, y, z) such that $g(x, y) = z$.

To draw the graph of $g: \mathbb{R}^2 \rightarrow \mathbb{R}$, begin by drawing the $x = \text{const.}$, $y = \text{const.}$, and $z = \text{const.}$ cross sections.

A level curve for $f: \mathbb{R}^2 \rightarrow \mathbb{R}$ is a sketch in \mathbb{R}^2 of the solutions of $f(x, y) = \text{const.}$

A contour map for $f: \mathbb{R}^2 \rightarrow \mathbb{R}$ are several level curves for f drawn on the same xy -axes.

A level surface for $g: \mathbb{R}^3 \rightarrow \mathbb{R}$ is a sketch in \mathbb{R}^3 of the solutions of $g(x, y, z) = \text{const.}$