1. Calculate the following limits. If a particular limit does not exist, state this clearly and tell why.

(a)
$$\lim_{x \to \sqrt{2}} 3x^2$$
 (b)
$$\lim_{\theta \to \pi/2} \tan \theta$$
 (c)
$$\lim_{x \to -1} \frac{x^2 - x + 2}{x + 1}$$
 (d)
$$\lim_{x \to 0^+} \sqrt{x} \sin\left(\frac{1}{x^2}\right)$$

(e)
$$\lim_{x \to 0} \frac{\sin(x^2)}{x}$$
 (f)
$$\lim_{x \to +\infty} \frac{\sin x}{x}$$
 (g)
$$\lim_{x \to 2} f(x), \text{ where } f(x) = \begin{cases} x^3, & x \le 2\\ x, & x > 2 \end{cases}$$

(h)
$$\lim_{x \to \pi} f(x), \text{ where } f(x) = \begin{cases} 0, & x \text{ irrational}\\ \sin\left(\frac{1}{q}\right), & x = \frac{p}{q} \text{ rational} \end{cases}$$
 (i)
$$\lim_{x \to +\infty} \sqrt[3]{\frac{8x^7 + 3x^5}{x^7 + 6x^2}}$$

- 2. (a) Let $f(x) = \sqrt{x}$. Using the *definition* of the derivative, calculate f'(x). Do the same for g(x) = 1/x.
 - (b) Using your result from (a), find the equation of the line tangent to the graph of $f(x) = \sqrt{x}$ at x = 1. Do the same for g(x) = 1/x.
- 3. Let f(x) = -x when $x \le 0, x \ne -1$; 2 when x = -1; \sqrt{x} when 0 < x < 1; $\sqrt[3]{3-x}$ when $x \ge 1$. Sketch the graph of f(x).
 - (a) For which points c does $\lim_{x \to c} f(x)$ exist? (b) For which points is f continuous?
 - (c) For which points is f differentiable?
- 4. Let f(x) = x + 2 when $x \le 0$; $-\frac{1}{2}x + 2$ when $0 < x \le 2$; $\sqrt{x 2} + 1$ when x > 2. Sketch the graph of f(x), and then using your result sketch the graph of f'(x).
- 5. Find the derivative and antiderivative of (a) $f(x) = 12x^5 + 5x^4 + x^2 + 2x + 1$, (b) $f(x) = (x+1)^3$, (c) $f(x) = (3x^2 2x + 1)(x 1)$.
- 6. Let the position x(t) of a particle at time t be given by $x(t) = 3t^2 2t + 1$. Find the instantaneous velocity v(t) of the particle for any time t. Where is the particle when its velocity is zero?
- 7. A clever tick falls strategically from the top of a 22 foot tree onto the top of the head of a 6 foot tall hiker. How long does it take the tick to hit the hiker's head (neglecting air friction), and what is the tick's velocity when it hits?
- 8. On earth, the acceleration a(t) due to gravity is essentially constant in time, with a(t) = -g, where $g = 32 f/s^2$. On nearby planet Ψ , scientists have discovered how to vary their planet's gravitational force with time. If the acceleration due to gravity on Ψ is a(t) = -t, find the analog of the earth formula $x(t) = -16t^2 + v_0t + x_0$ for planet Ψ . That is, find x(t) for a(t) = -t with initial velocity v_0 and position x_0 . Using your expression for x(t), find how long it will take for a ball thrown upward from the ground on Ψ at t = 0 with initial velocity 6 f/s to hit the ground.