

Sea Ice, Climate Change, and Polar Ecosystems

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Workshop on Spatio-Temporal Dynamics in Ecology
Lorentz Center, Leiden

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Frey

SEA ICE covers 7 - 10% of earth's ocean surface

- boundary between ocean and atmosphere
- mediates exchange of heat, gases, momentum
- global ocean circulation
- indicator and agent of **climate change**



polar ice caps critical to global climate in reflecting incoming solar radiation



white snow and ice
reflect

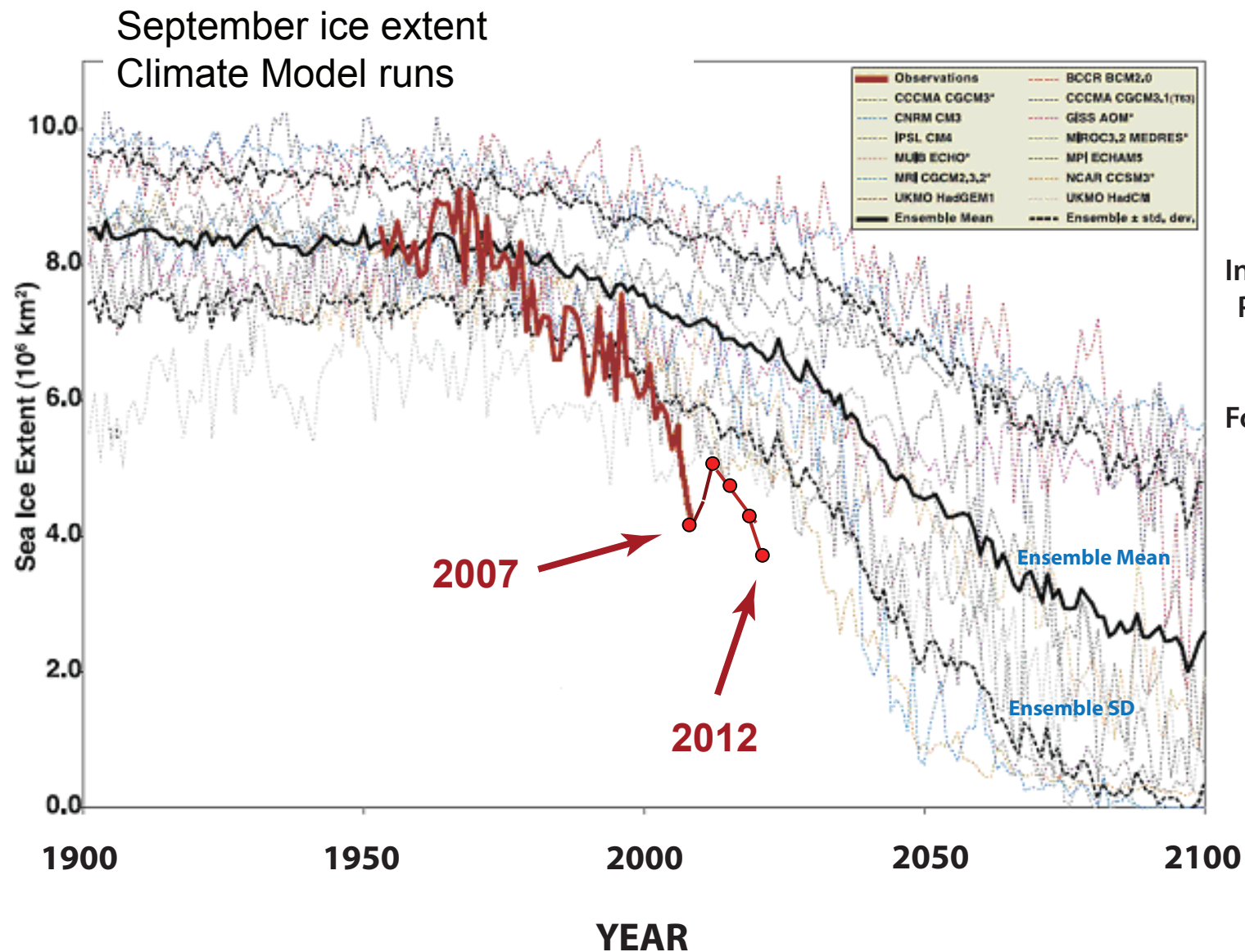


dark water and land
absorb

$$\text{albedo } \alpha = \frac{\text{reflected sunlight}}{\text{incident sunlight}}$$

Arctic sea ice decline - faster than predicted by climate models

Stroeve et al., GRL, 2007



**IPCC AR4
Models**

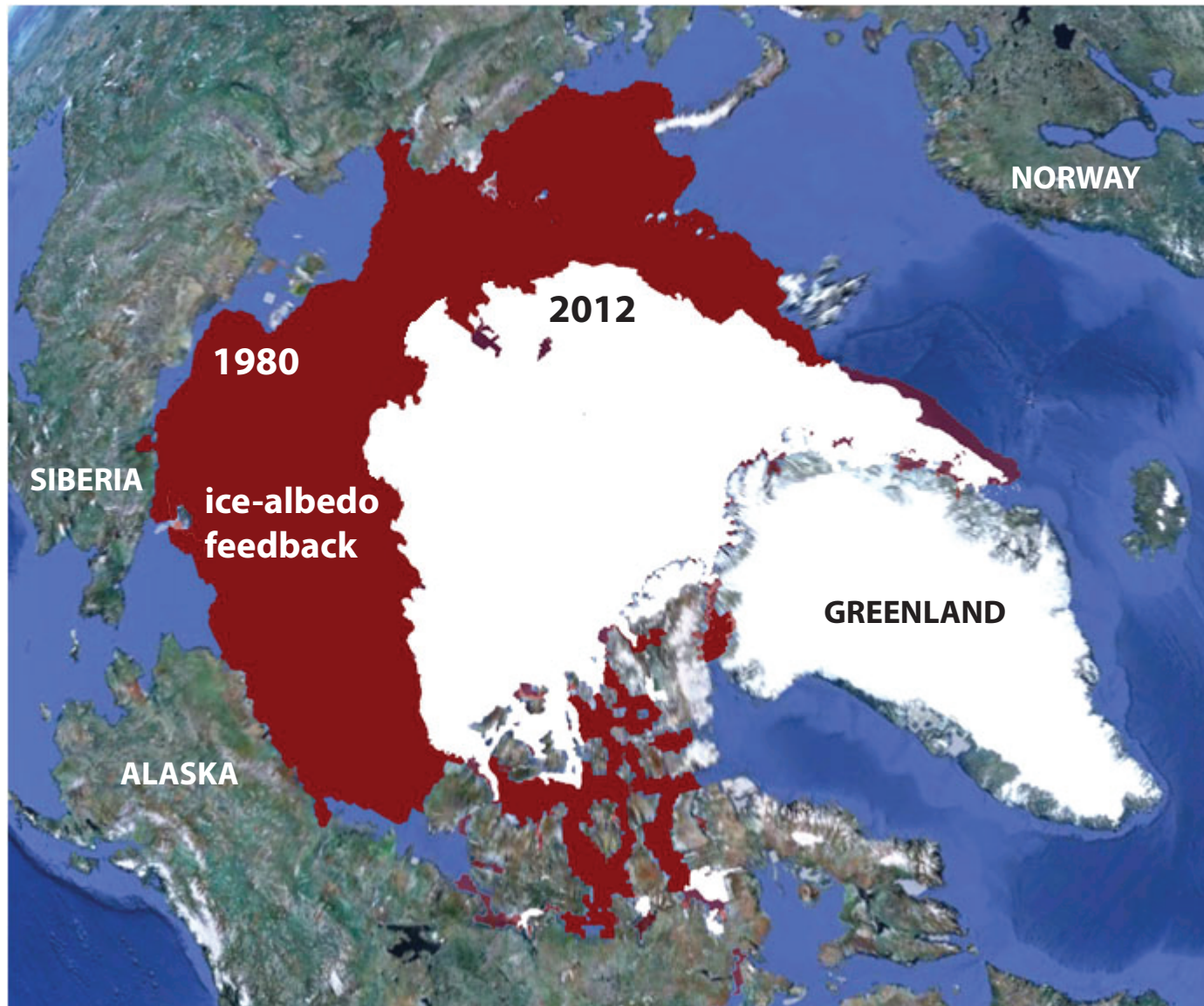
Intergovernmental
Panel on Climate
Change (IPCC)

Fourth Assessment
AR4, 2007

Change in Arctic Sea Ice Extent

September 1980 -- **7.8** million square kilometers

September 2012 -- **3.4** million square kilometers



Has Arctic sea ice loss passed through a “tipping point”?

an irreversible downward slide to ice-free Arctic summers (with hysteresis)
driven by ice-albedo feedback

low order (toy) models of climate change

Eisenman, Wettlaufer, PNAS 2009:

nonlinear ODE for energy in upper ocean

look for bifurcations in solutions

multiple equilibria: ice-free, ice covered, ...

- tipping point unlikely in loss of summer ice

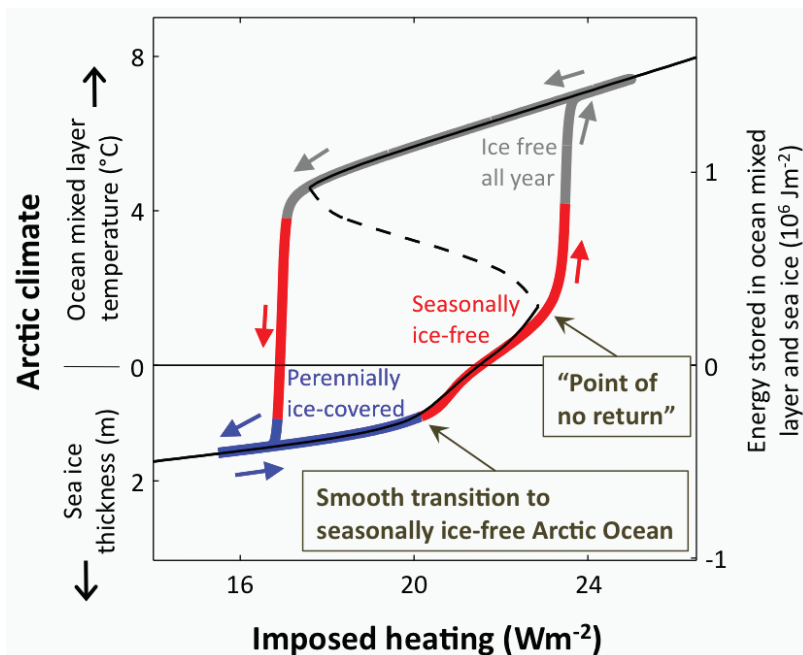
Abbot, Silber, Pierrehumbert, JGR 2011

bifurcations when include clouds, ice loss

Sudakov, Vakulenko, Golden

Comm. Nonlinear Sci. & Num. Sim., 2014

impact of melt ponds



challenge

represent sea ice more rigorously in climate models

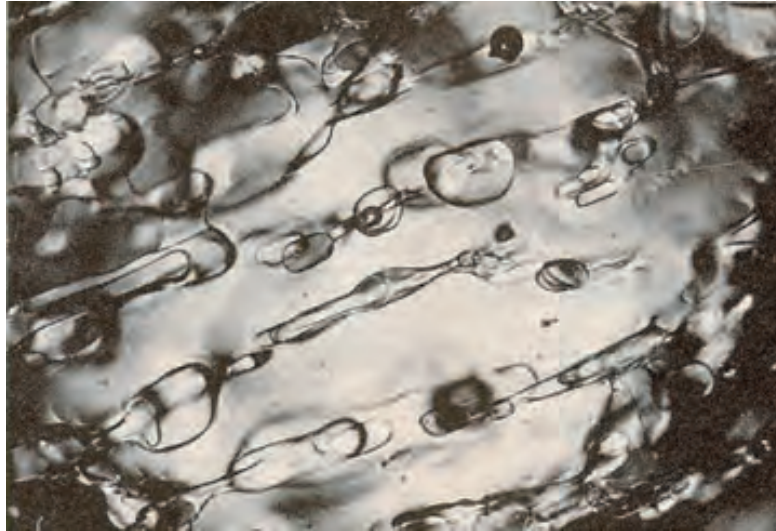
incorporate key processes

fundamental problem -- linkage of scales

sub-grid scale processes

sea ice is a multiscale composite

structured on many length scales



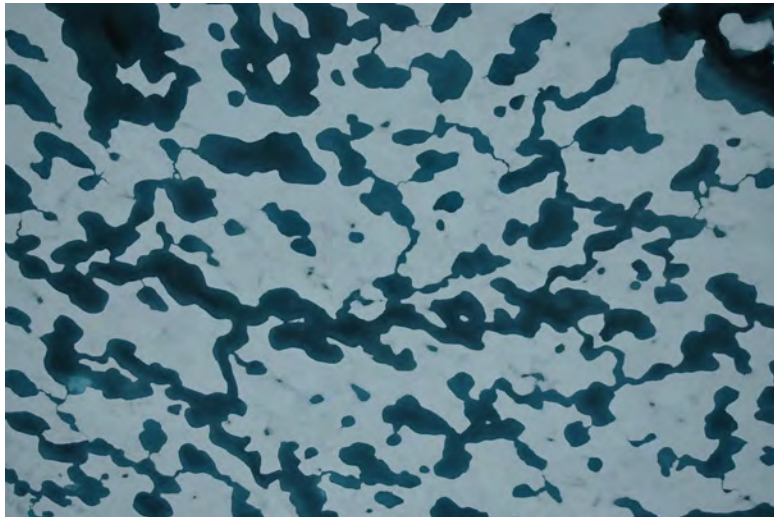
*brine
inclusions*

millimeters



pancakes

centimeters



*melt
ponds*

meters



*ice
floes*

kilometers



**Who cares if
Arctic sea ice
disappears?**

Use of sea ice as a platform

- Walrus life cycle tied to sea-ice cycle
- Ice floes as diving platforms for feeding over shallow shelf



Photo: Marc Webber, US Fish & Wildlife Service

BMCM Tim Sullivan

sea ice microphysics

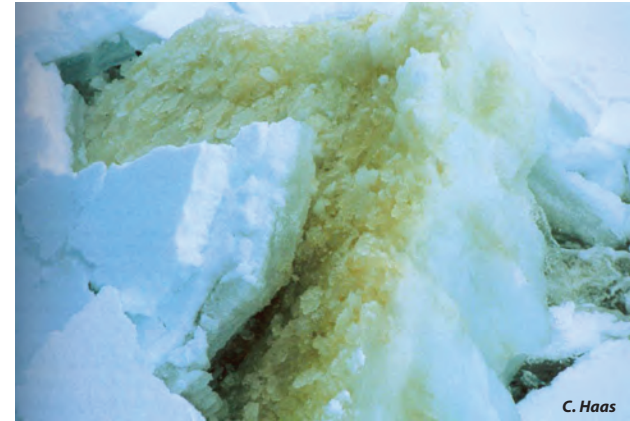
fluid transport

fluid flow through the porous microstructure of sea ice governs key processes in polar climate and ecosystems

evolution of Arctic melt ponds and sea ice albedo



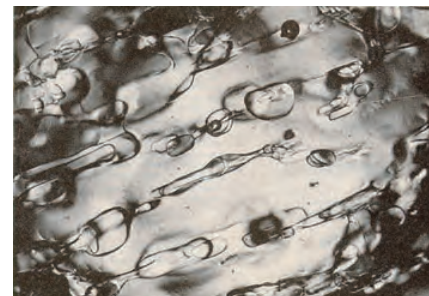
nutrient flux for algal communities



- *drainage of brine and melt water*
- *ocean-ice-air exchanges of heat, CO₂*
- *Antarctic surface flooding and snow-ice formation*
- *evolution of salinity profiles*



linkage of scales



Darcy's Law for slow viscous flow in a porous medium

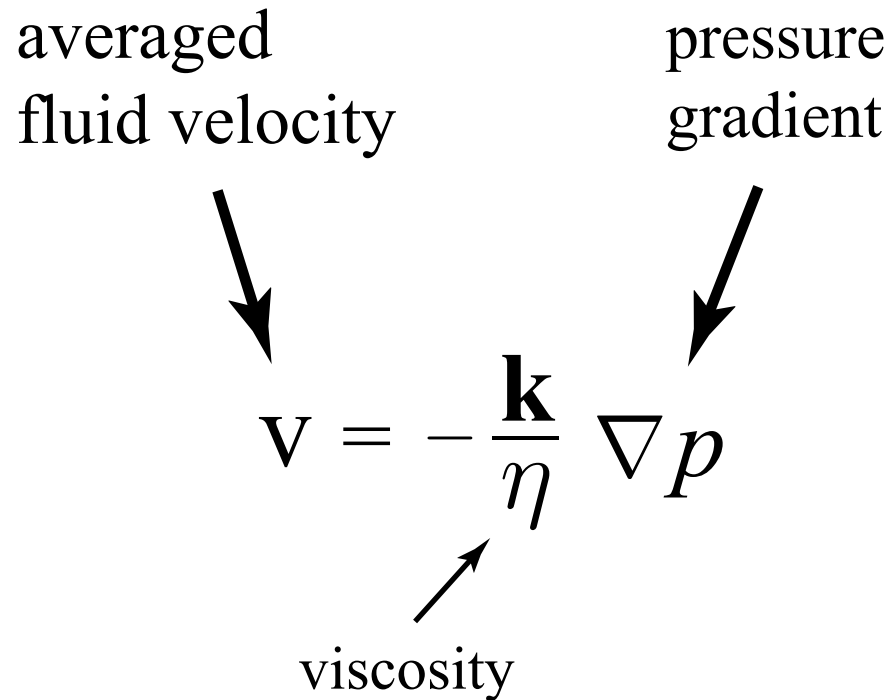


Diagram illustrating Darcy's Law for slow viscous flow in a porous medium. The equation is shown as $\mathbf{v} = -\frac{\mathbf{k}}{\eta} \nabla p$. Arrows point from the following labels to the corresponding terms in the equation:

- averaged fluid velocity points to \mathbf{v}
- pressure gradient points to ∇p
- viscosity points to η

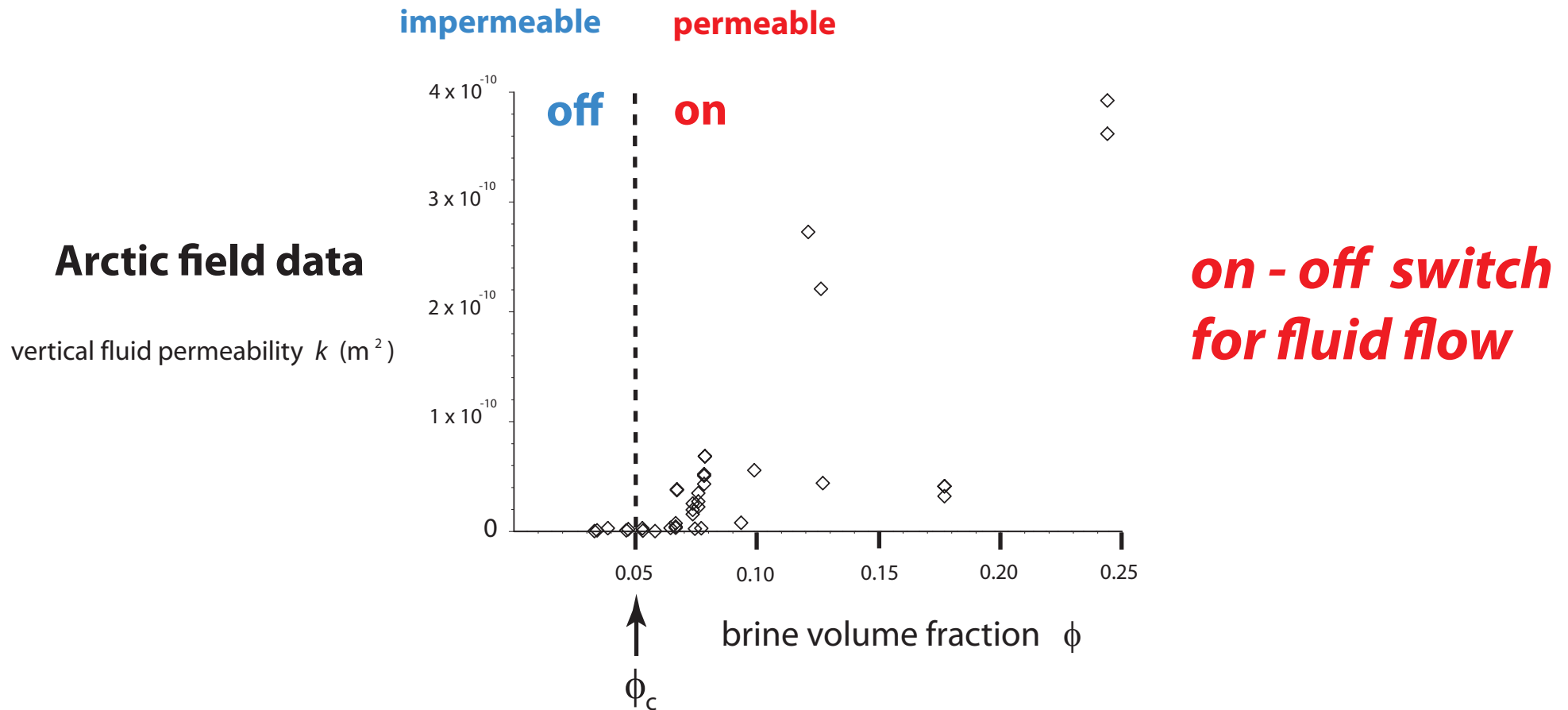
\mathbf{k} = fluid permeability tensor

example of *homogenization*

mathematics for analyzing effective behavior of heterogeneous systems

e.g. transport properties of composites - electrical conductivity, thermal conductivity, etc.

Critical behavior of fluid transport in sea ice



critical brine volume fraction $\phi_c \approx 5\%$ \longleftrightarrow $T_c \approx -5^\circ \text{C}$, $S \approx 5 \text{ ppt}$

RULE OF FIVES

Golden, Ackley, Lytle *Science* 1998

Golden, Eicken, Heaton, Miner, Pringle, Zhu, *Geophys. Res. Lett.* 2007

Pringle, Miner, Eicken, Golden *J. Geophys. Res.* 2009



sea ice algal communities

D. Thomas 2004

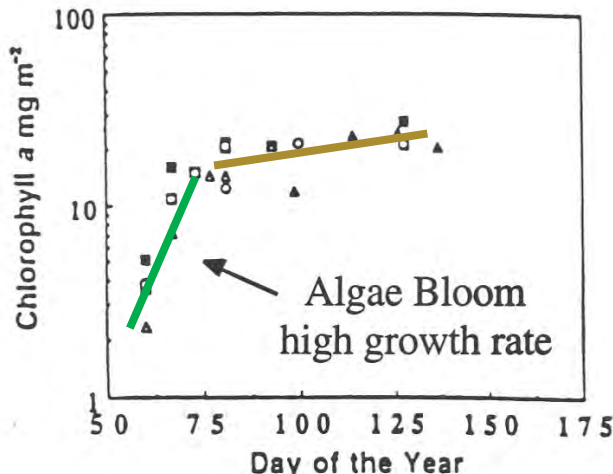
nutrient replenishment
controlled by ice permeability

biological activity turns on
or off according to
rule of fives

Golden, Ackley, Lytle Science 1998

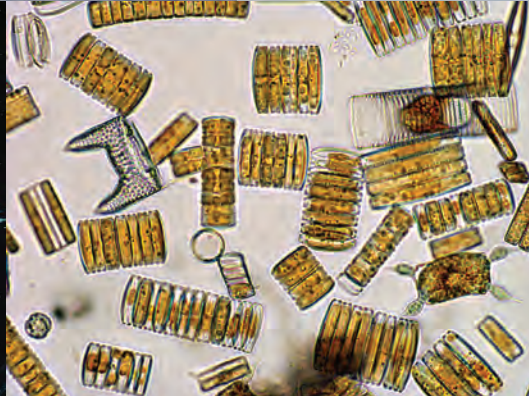
Fritsen, Lytle, Ackley, Sullivan Science 1994

critical behavior of microbial activity



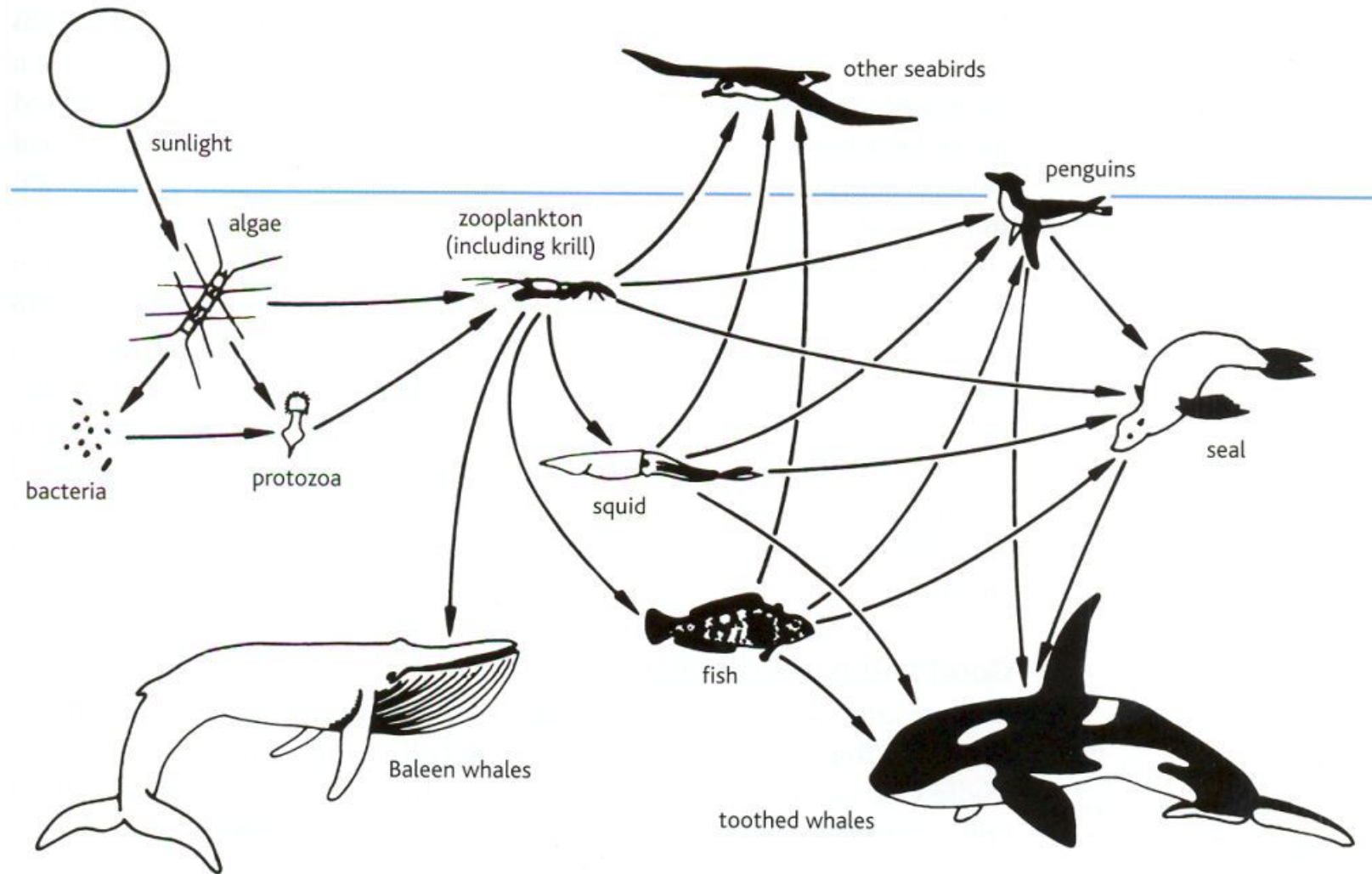
Convection-fueled algae bloom
Ice Station Weddell

sea ice ecosystem



sea ice algae
support life in the polar oceans

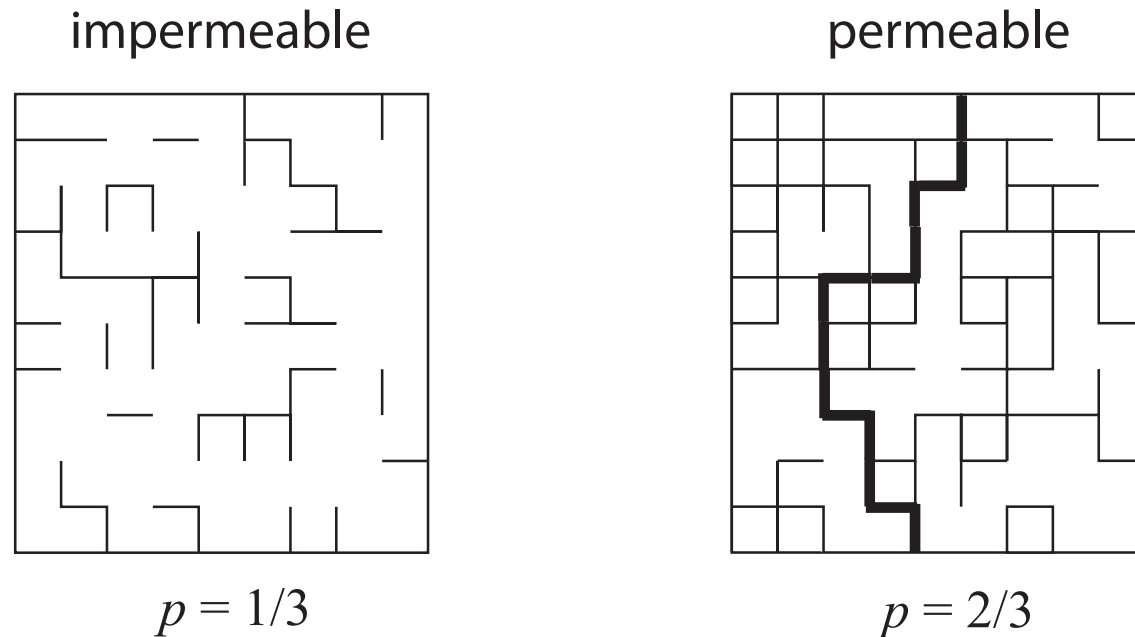
Antarctic marine food web



Why is the rule of fives true?

percolation theory

mathematical theory of connectedness



bond \longrightarrow *open* with probability p
closed with probability $1-p$

percolation threshold

$$p_c = 1/2 \quad \text{for } d = 2$$

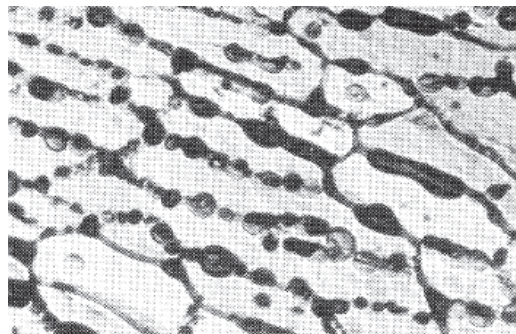
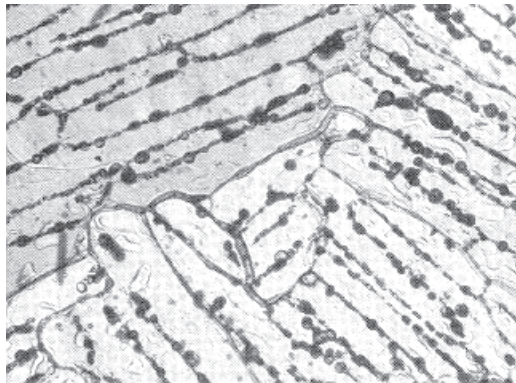
first appearance of infinite cluster

“tipping point” for connectivity

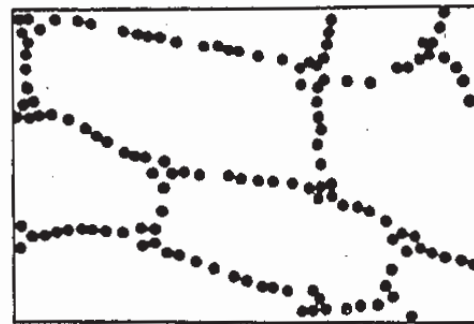
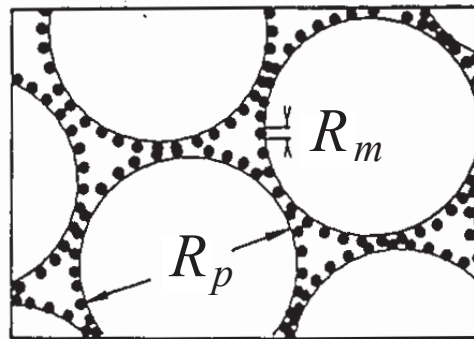
Continuum percolation model for **stealthy** materials applied to sea ice microstructure explains **Rule of Fives** and Antarctic data on **ice production** and **algal growth**

$$\phi_c \approx 5 \%$$

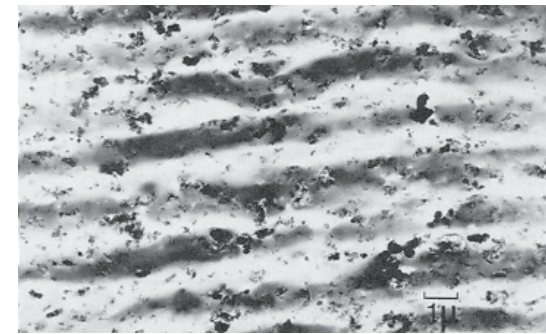
Golden, Ackley, Lytle, *Science*, 1998



sea ice



compressed
powder



radar absorbing
composite

sea ice is radar absorbing

**Geophysical
Research
Letters**

28 AUGUST 2007
Volume 34 Number 16
American Geophysical Union

***rigorous bounds
percolation theory
hierarchical model
network model***

field data

micro-scale
controls
macro-scale
processes

X-ray tomography for
brine inclusions

***unprecedented look
at thermal evolution
of brine phase and
its connectivity***

A unified approach to understanding permeability in sea ice • Solving the mystery of
booming sand dunes • Entering into the "greenhouse century": A case study from Switzerland

Arctic and Antarctic field experiments

*develop electromagnetic methods
of monitoring fluid transport and
microstructural transitions*

extensive measurements of fluid and
electrical transport properties of sea ice:

2007 Antarctic SIPEX

2010 Antarctic McMurdo Sound

2011 Arctic Barrow AK

2012 Arctic Barrow AK

2012 Antarctic SIPEX II

2013 Arctic Barrow AK

2014 Arctic Chukchi Sea



Notices

of the American Mathematical Society

May 2009

Volume 56, Number 5

Climate Change and
the Mathematics of
Transport in Sea Ice

page 562

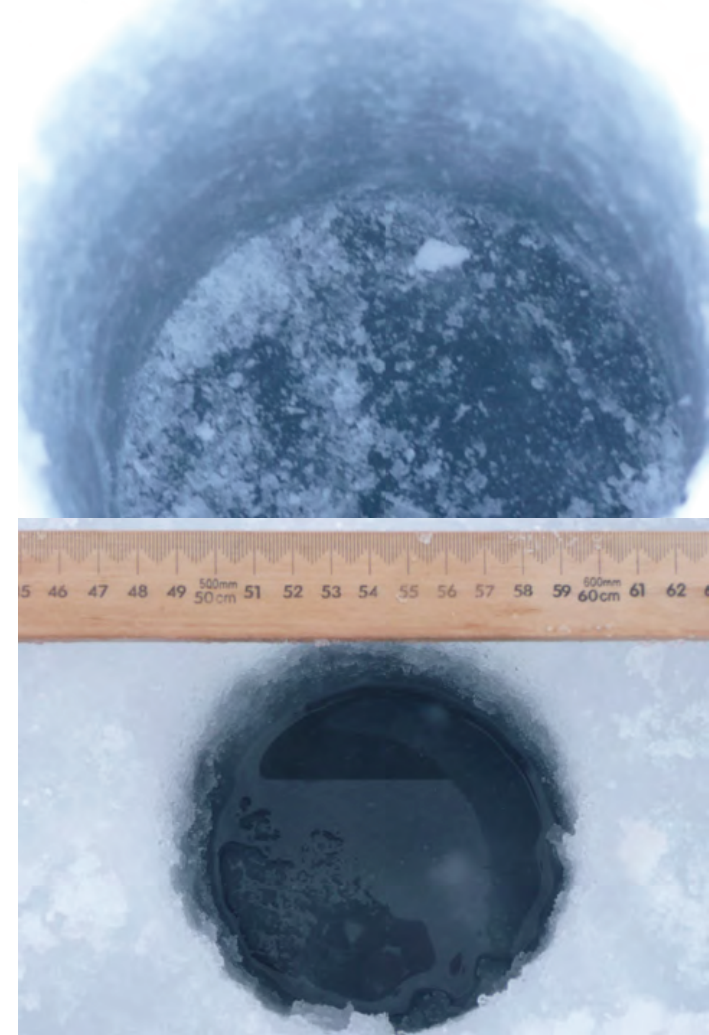
Mathematics and the
Internet: A Source of
Enormous Confusion
and Great Potential

page 586



photo by Jan Lieser

Real analysis in polar coordinates (see page 613)



**measuring
fluid permeability
of Antarctic sea ice**

SIPEX 2007

Homogenization for diffusion processes

Anomalous diffusion and sea ice dynamics

*sub- and super-diffusive behavior of motion
of sea ice floes as tracked by buoy data*

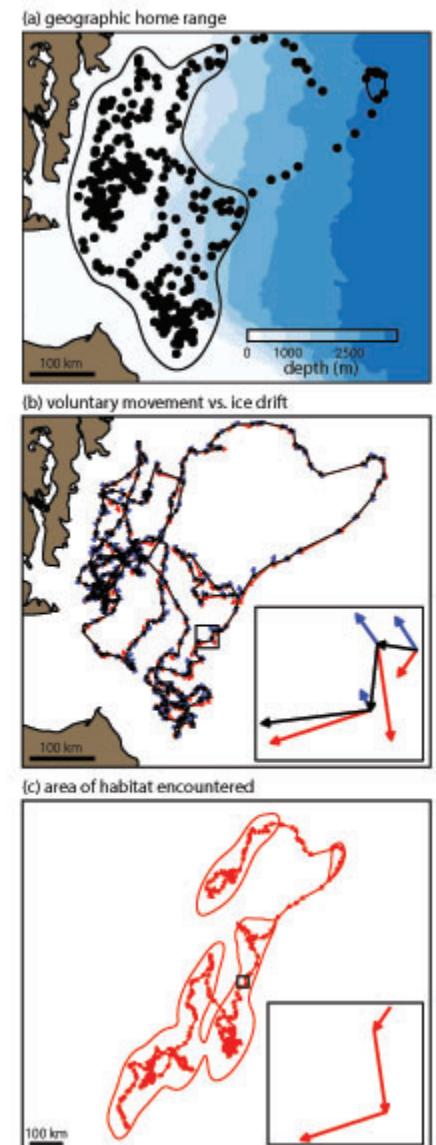
Jennifer Lukovich, Jennifer Hutchings, David Barber, 2014

Ben Murphy, Court Strong, Jack Xin (UC Irvine), Ken Golden

Home ranges in moving habitats: polar bears and sea ice

*“diffusive” polar bear motion superimposed
with drifting sea ice*

Marie Auger-Méthé, Mark Lewis, Andrew Derocher, 2014



Question:

**Given ongoing changes in sea ice
in places like the Chukchi Sea...**

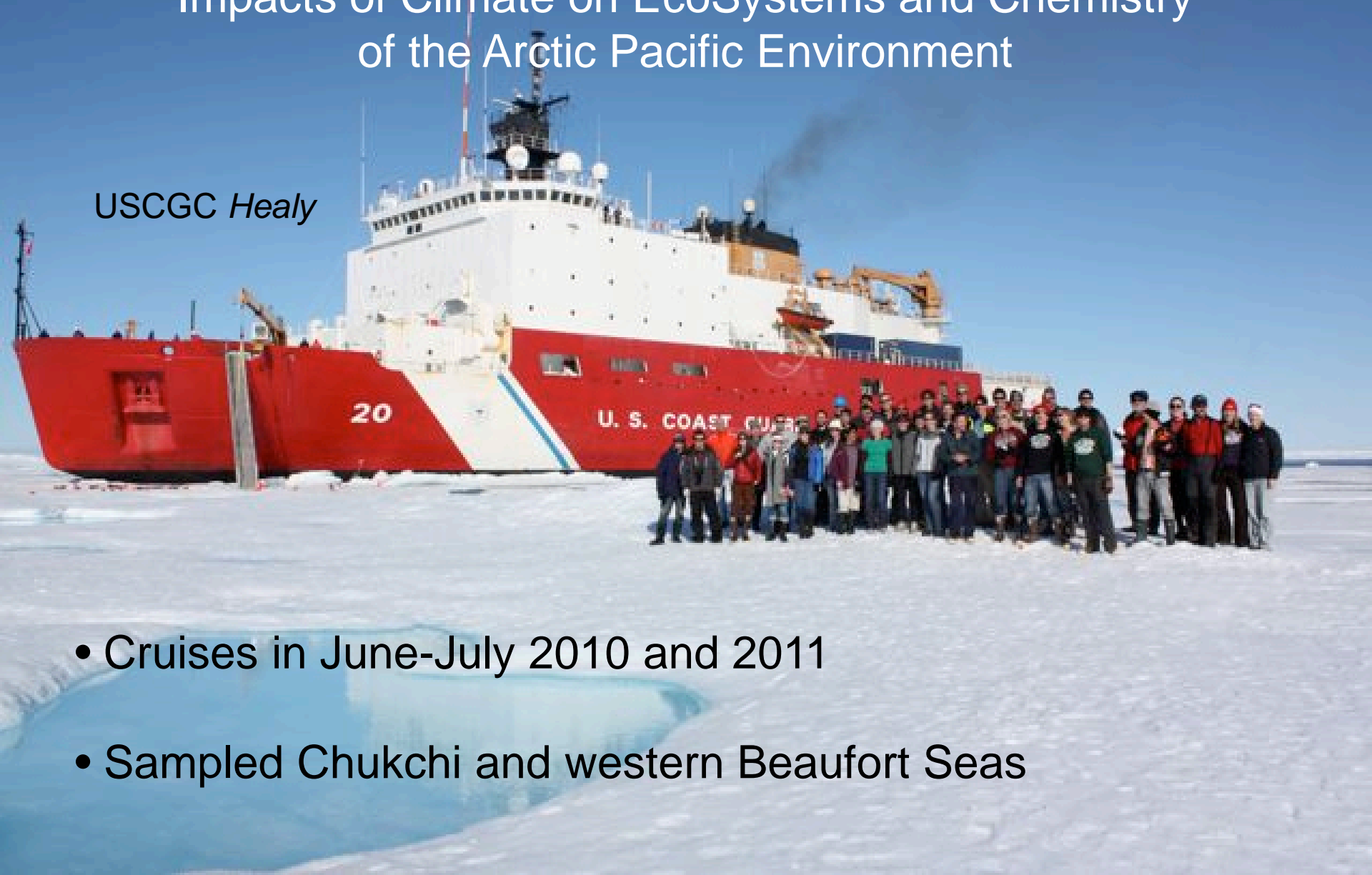
**How have phytoplankton
responded?**

Slides Courtesy of Kevin Arrigo, Stanford

ICESCAPE

Impacts of Climate on EcoSystems and Chemistry
of the Arctic Pacific Environment

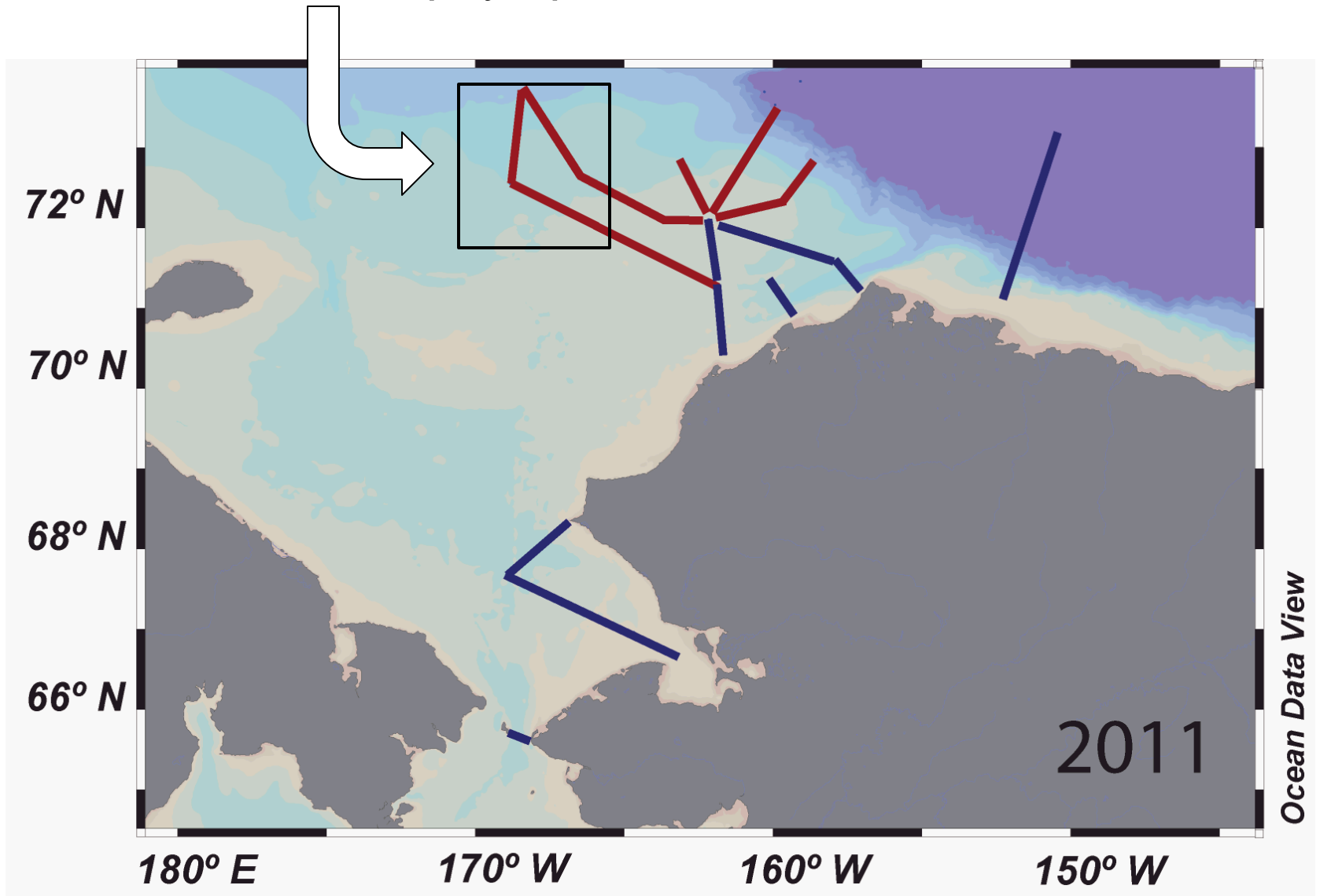
USCGC Healy



- Cruises in June-July 2010 and 2011
- Sampled Chukchi and western Beaufort Seas

ICESCAPE 2011

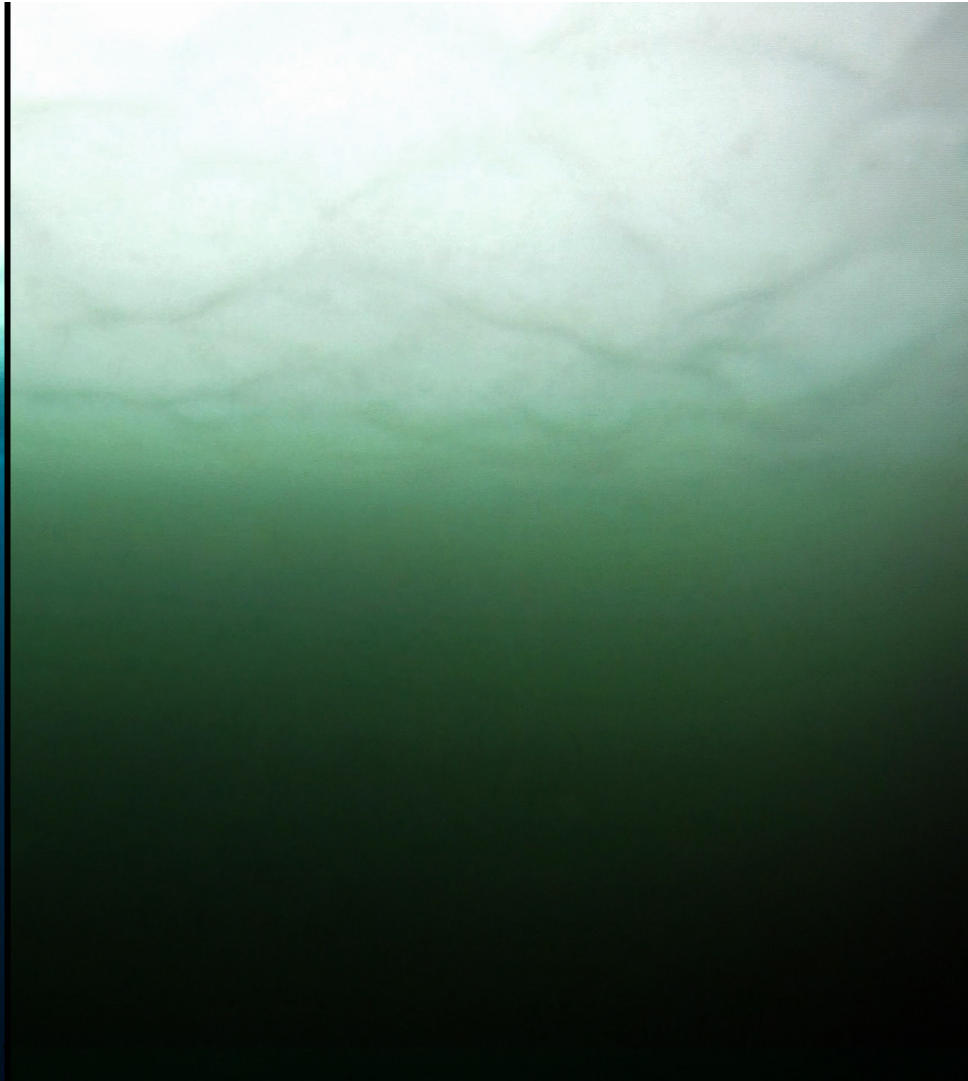
Site of under-ice phytoplankton bloom



Extremely high biomass



No bloom under ice

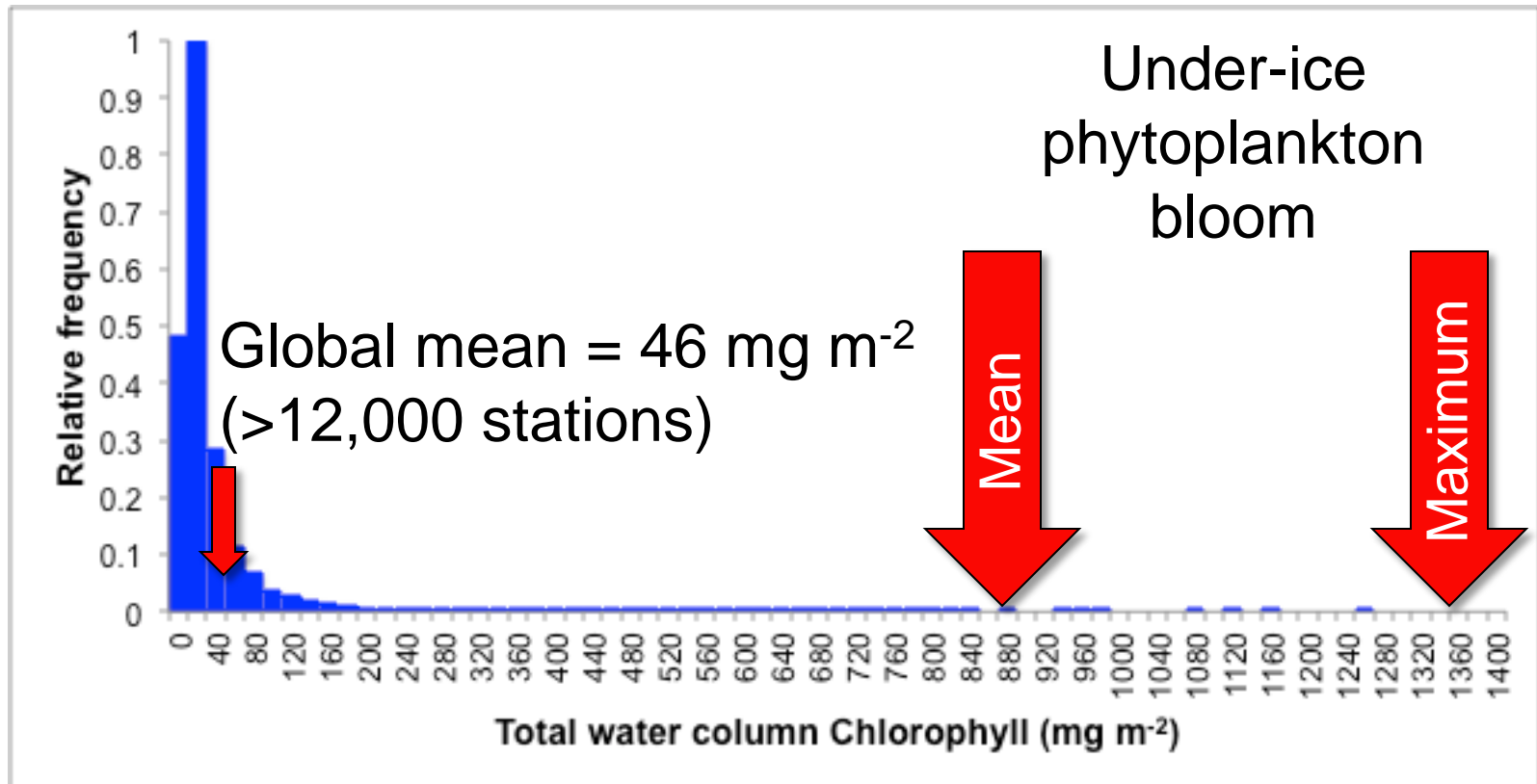


Bloom under ice

Extremely high biomass

Phytoplankton standing crops associated with **under-ice blooms** were some of the highest measured anywhere in the world

PHYTOPLANKTON STANDING CROPS WORLDWIDE



How is such an intense bloom possible?

“Old” Chukchi Sea



How is such an intense bloom possible?

“New” Chukchi Sea



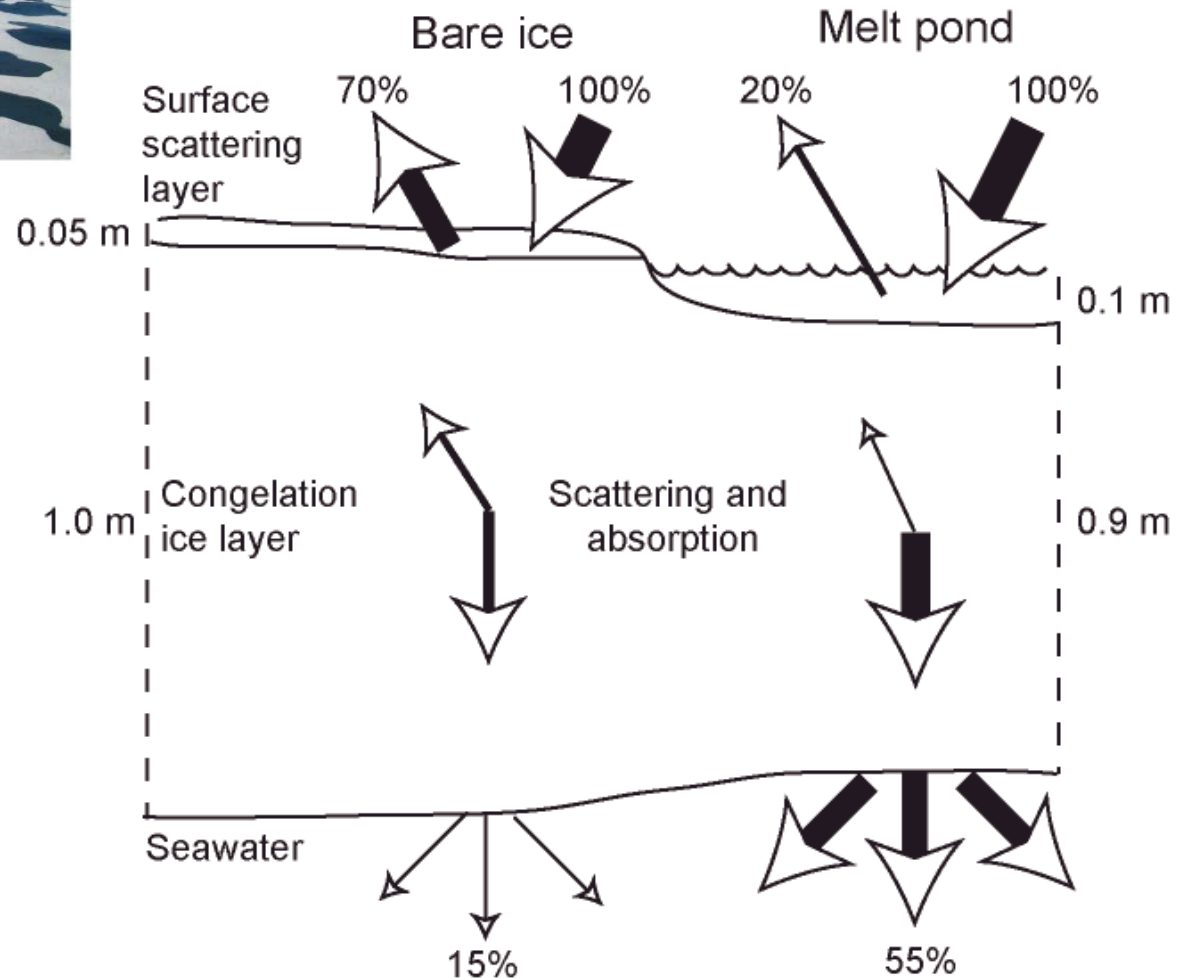
Enough light under the ice?



Ice was thick but melt pond fraction was high (30-50%)

Melt ponds transmit
>50% of incident
surface irradiance

~4 times more than
bare ice



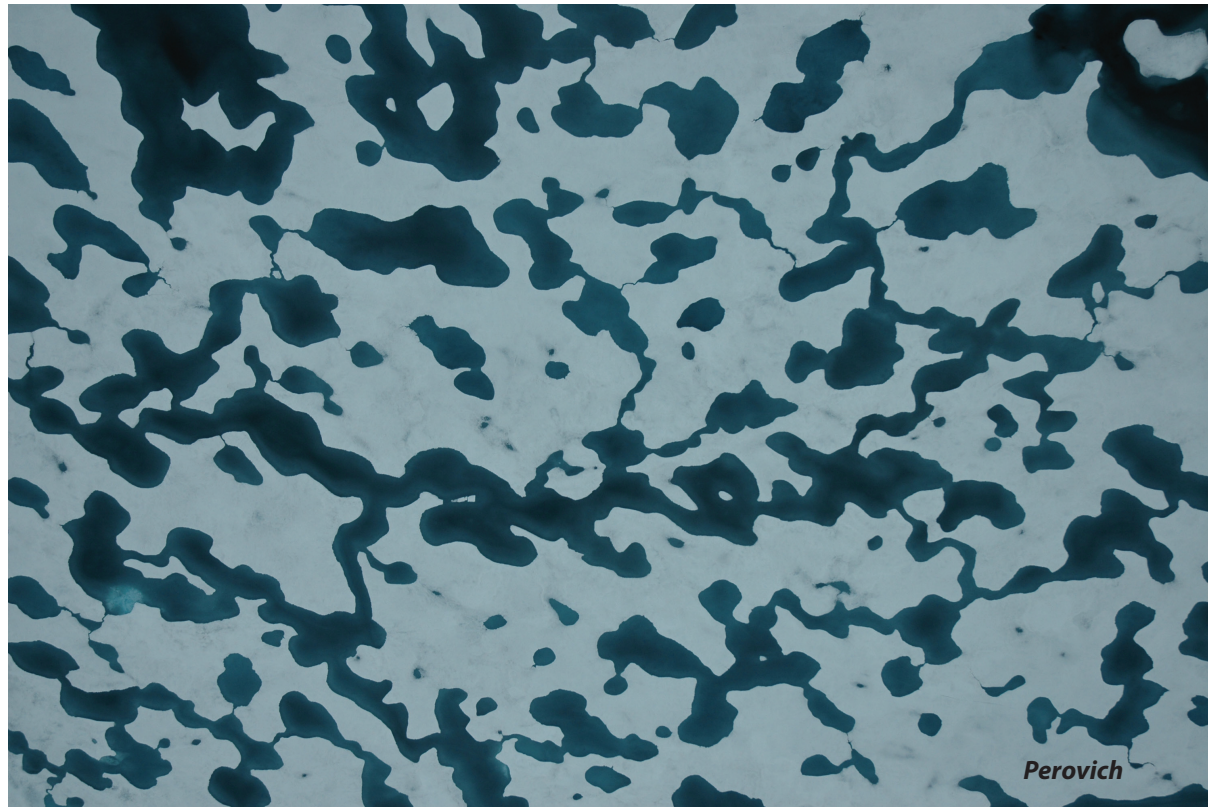
melt pond formation and albedo evolution:

- *major drivers in polar climate*
- *key challenge for global climate models*

numerical models of melt pond evolution, including topography, drainage (permeability), etc.

Lüthje, Feltham,
Taylor, Worster 2006
Flocco, Feltham 2007

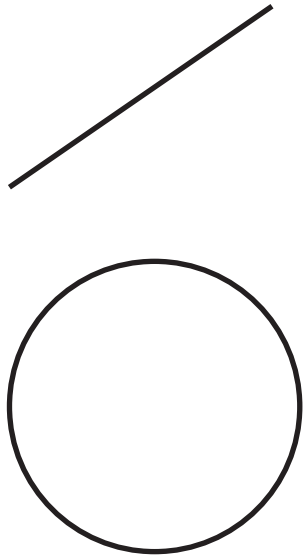
Skyllingstad, Paulson,
Perovich 2009
Flocco, Feltham,
Hunke 2012



Are there universal features of the evolution similar to phase transitions in statistical physics?

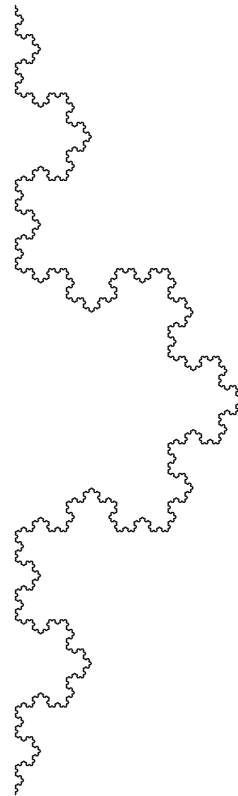
fractal curves in the plane

they wiggle so much that their dimension is >1



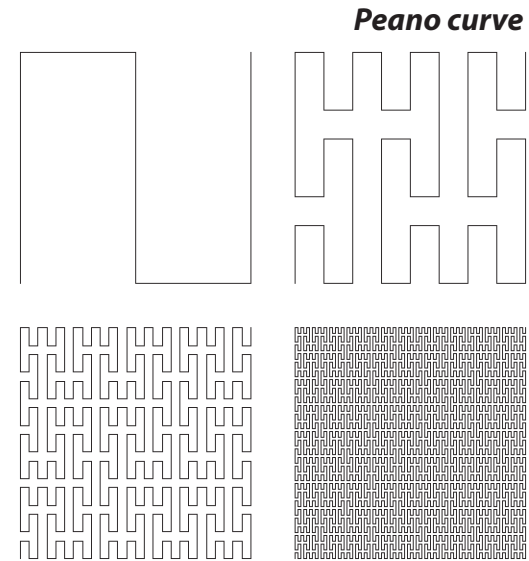
simple curves

$D = 1$



Koch snowflake

$D = 1.26$



Peano curve

Brownian motion

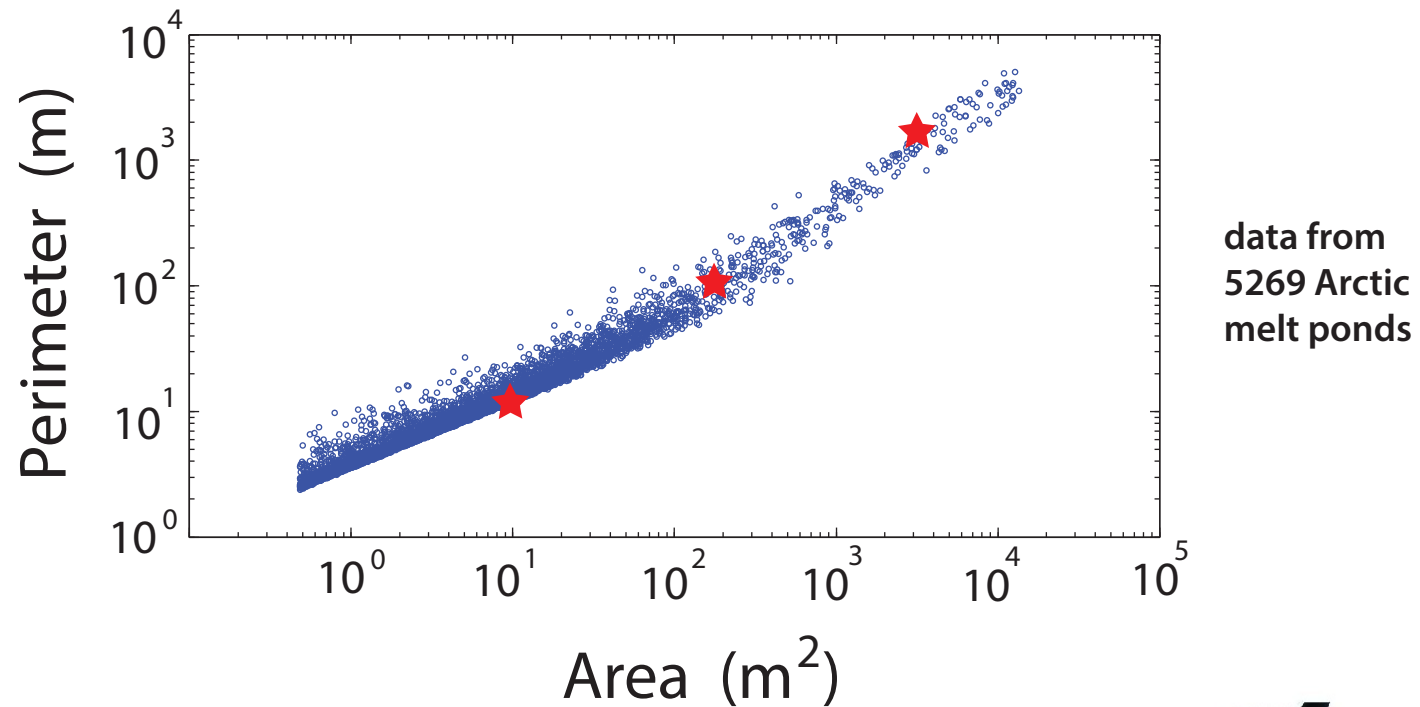
space filling curves

$D = 2$

Transition in the fractal geometry of Arctic melt ponds

The Cryosphere, 2012

Christel Hohenegger, Bacim Alali, Kyle Steffen, Don Perovich, Ken Golden



~ 30 m



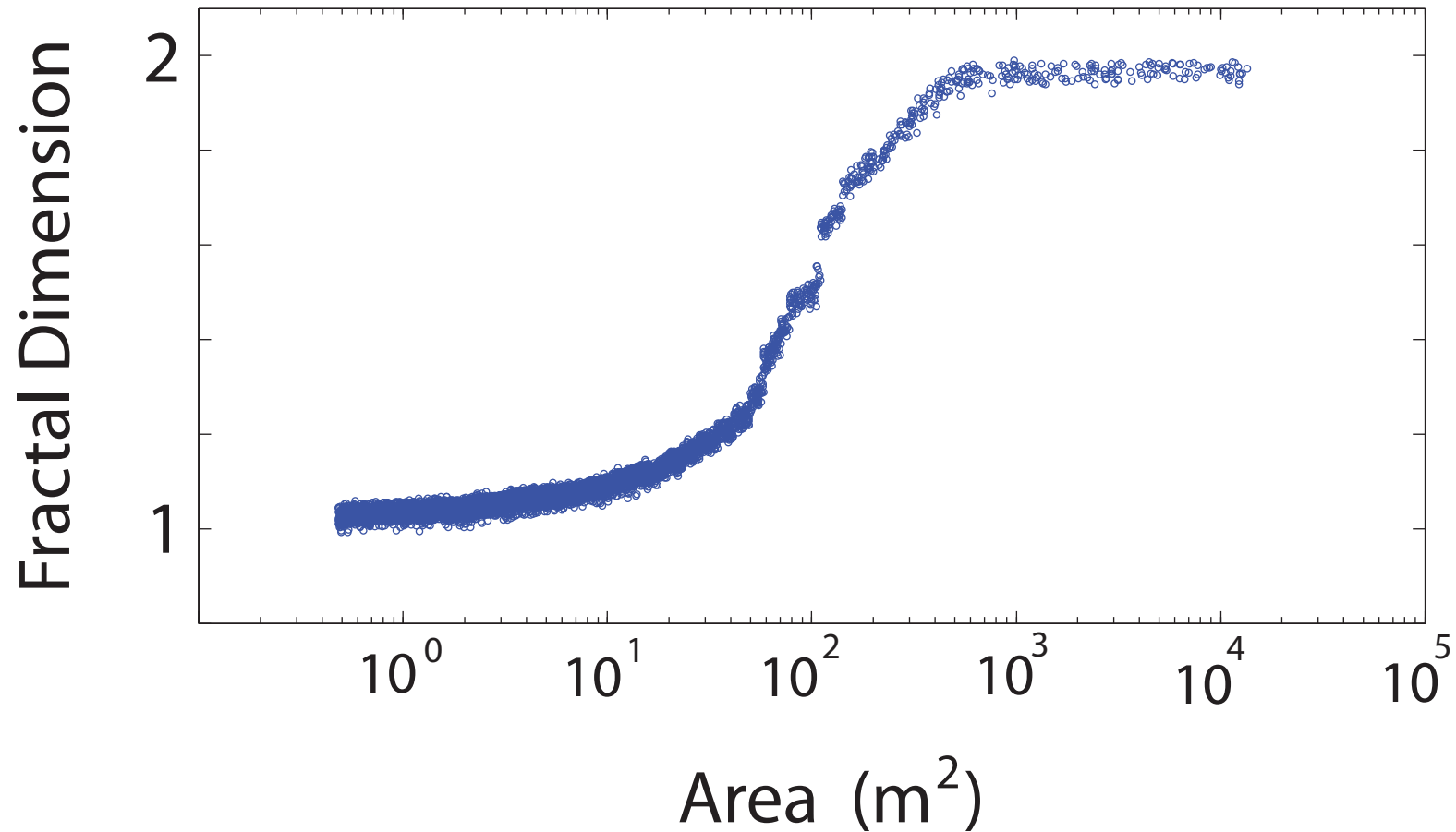
simple pond

transitional pond

complex pond

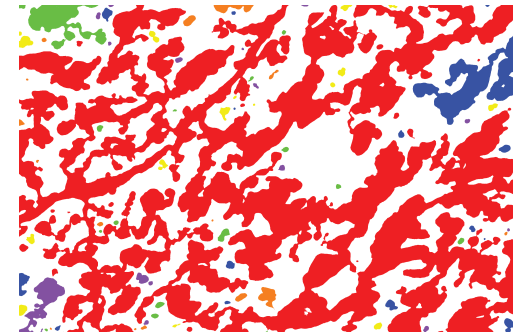
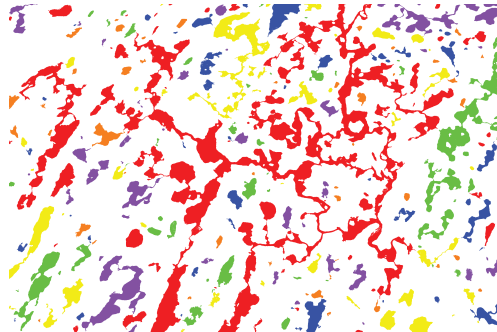
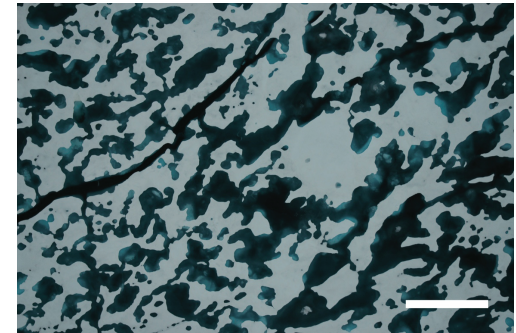
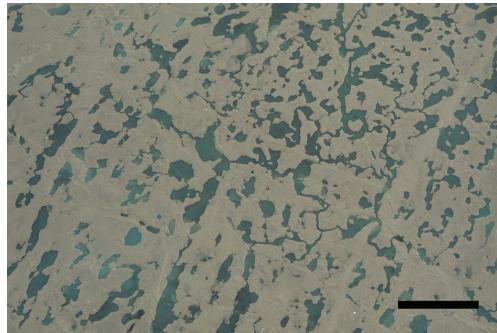
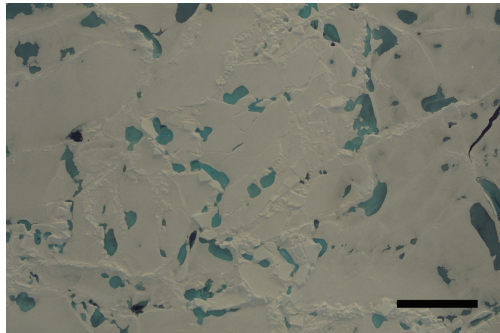
transition in the fractal dimension

complexity grows with length scale



compute “derivative” of area - perimeter data

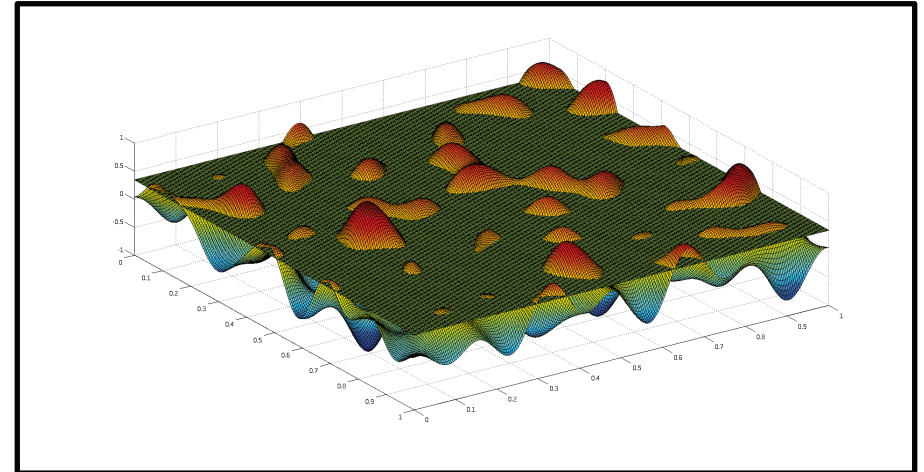
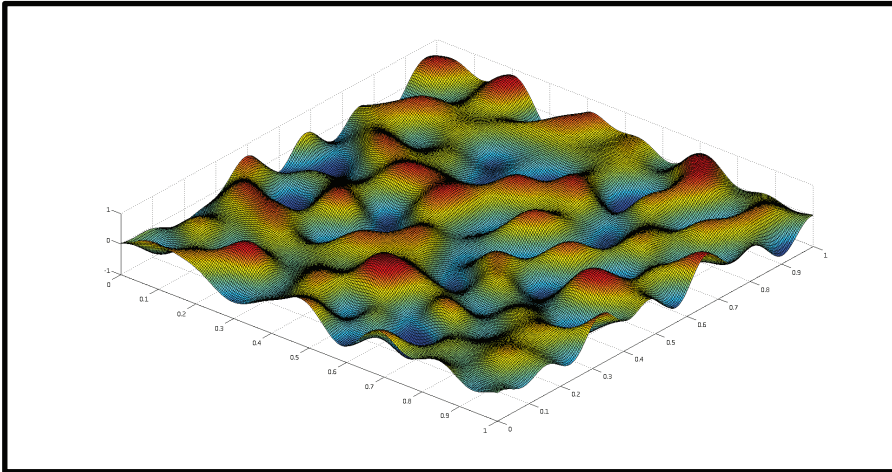
***small simple ponds coalesce to form
large connected structures with complex boundaries***



melt pond percolation

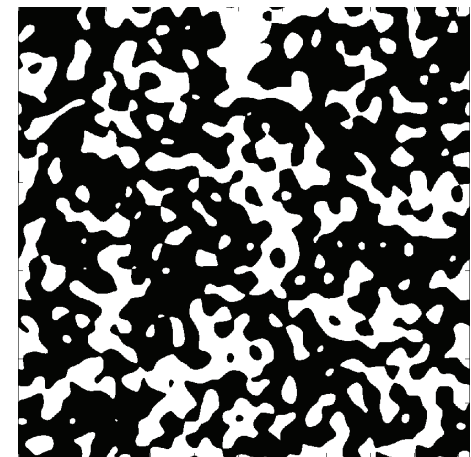
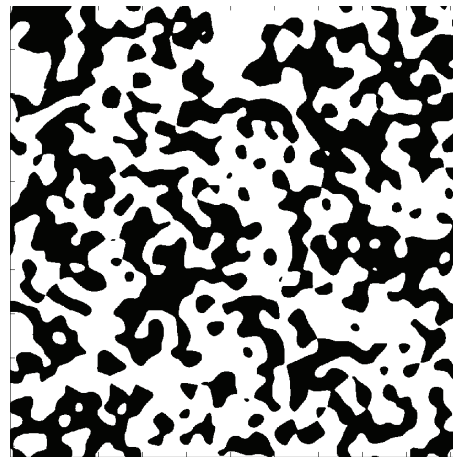
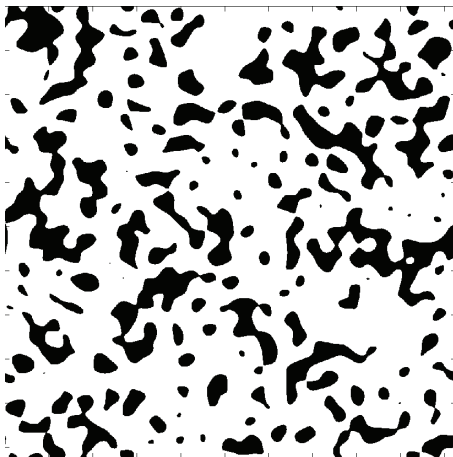
Continuum percolation model for melt pond evolution

Brady Bowen, Court Strong, Ken Golden, 2014



random Fourier series representation of surface topography

intersections of a plane with the surface define melt ponds

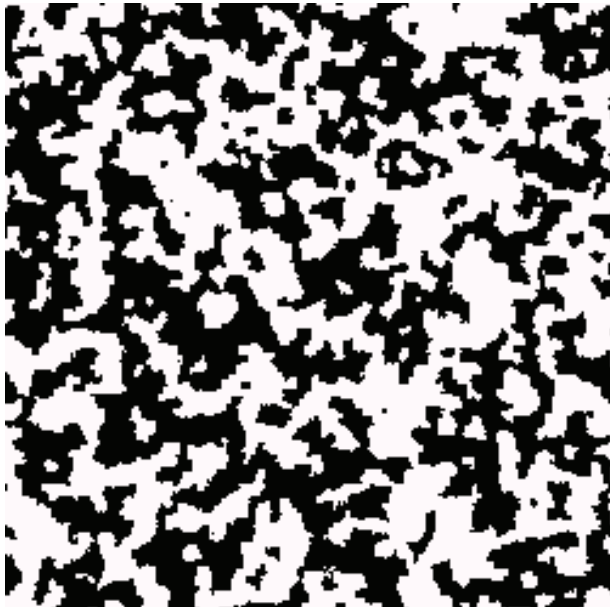
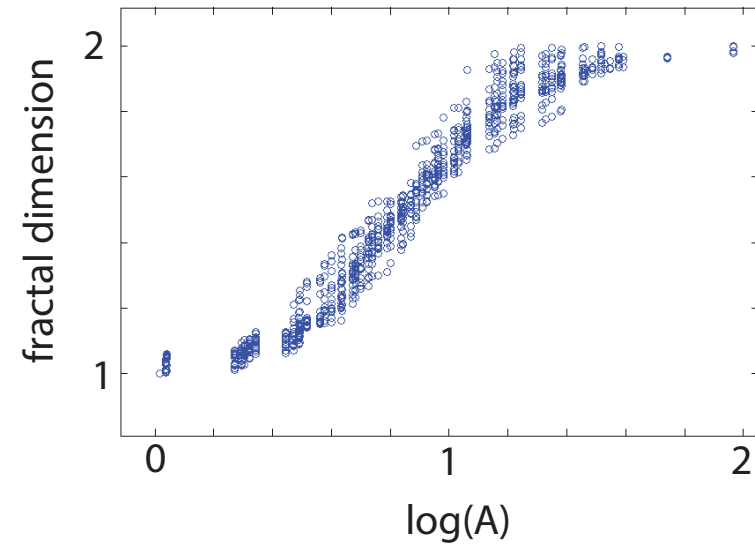
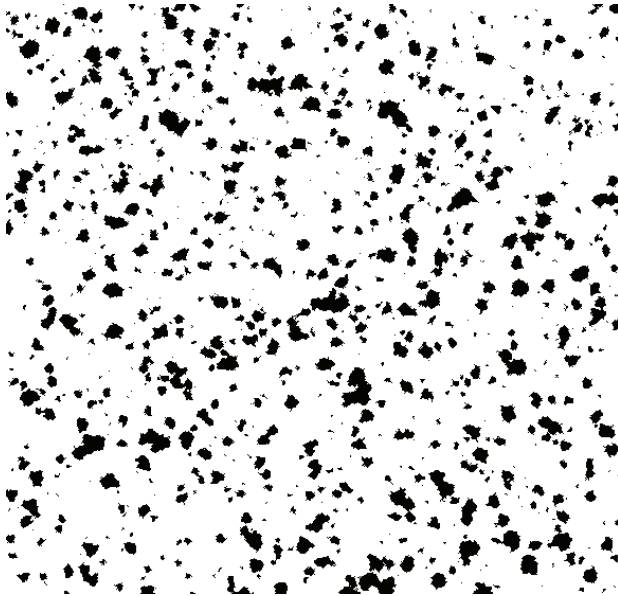


electronic transport in disordered media

diffusion in turbulent plasmas

(Isichenko, Rev. Mod. Phys., 1992)

simple stochastic growth model of melt pond evolution



voter
model

*a square is more likely to melt
if its neighbors have melted*

Ising model for ferromagnets



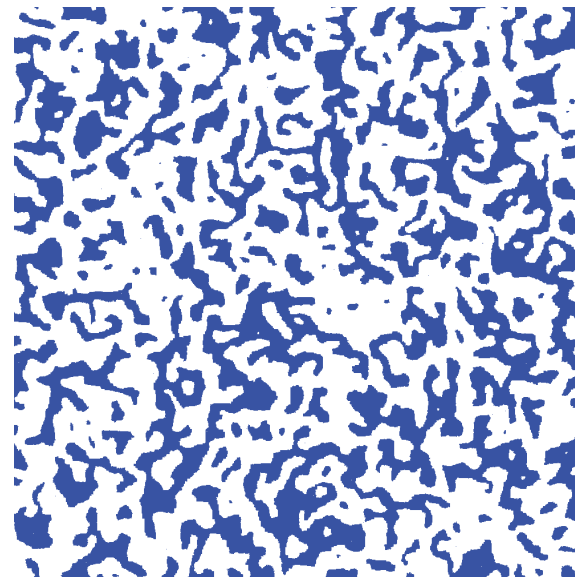
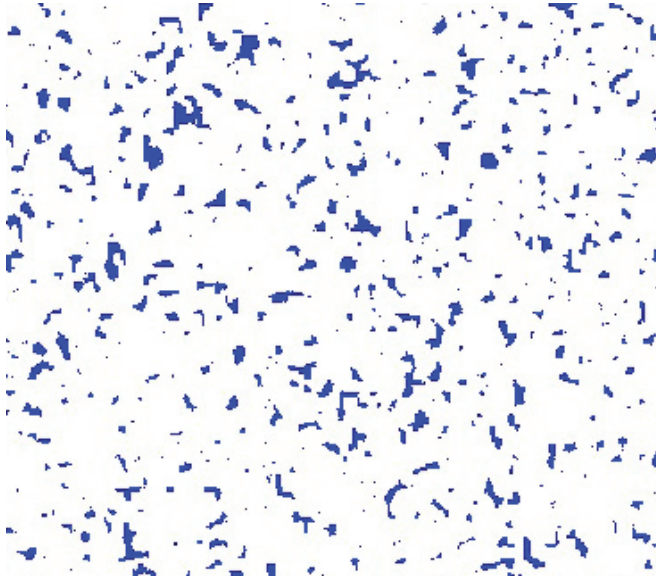
Ising model for melt ponds

$$\mathcal{H}_\omega = -J \sum_{\langle i,j \rangle}^N s_i s_j - H \sum_i^N s_i$$

$$s_i = \begin{cases} \uparrow & +1 & \text{water} & (\text{spin up}) \\ \downarrow & -1 & \text{ice} & (\text{spin down}) \end{cases}$$

magnetization $M = \lim_{N \rightarrow \infty} \frac{1}{N} \left\langle \sum_j s_j \right\rangle$

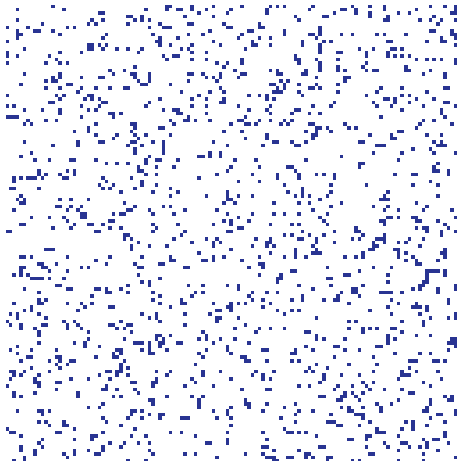
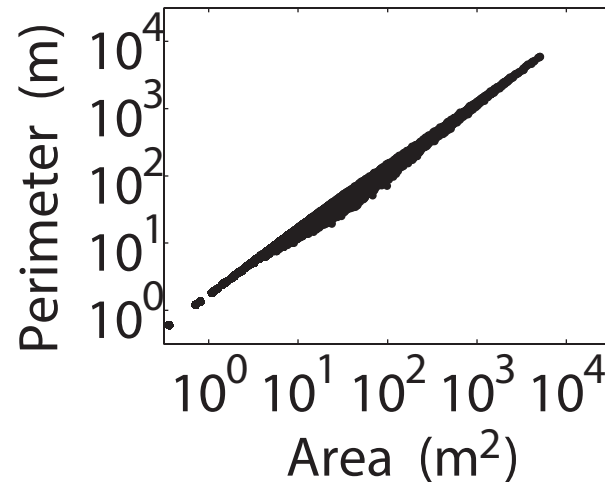
pond coverage $\frac{(M+1)}{2}$



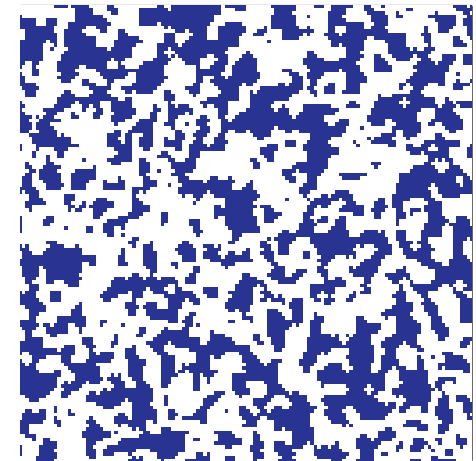
“melt ponds” are clusters of magnetic spins that align with the applied field

Melt Pond Ising Model

- Minimize an Ising Hamiltonian
random magnetic field represents the initial ice topography
interaction term represents horizontal heat transfer
- Ice-albedo feedback incorporated by taking coupling constant in interaction term to be proportional to the pond coverage



*predicted length scale
of fractal transition
agrees well with data*



The Conundrum of Melt Pond Formation: *How can ponds form on top of sea ice that is highly permeable?*

C. Polashenski, K. M. Golden, E. Skyllingstad, D. K. Perovich

2014 Study of Under Ice Blooms in the Chuckchi Ecosystem (SUBICE)
aboard USCGC Healy



Hypothesis – Freshwater re-seals ice

Borehole test with varying salinity

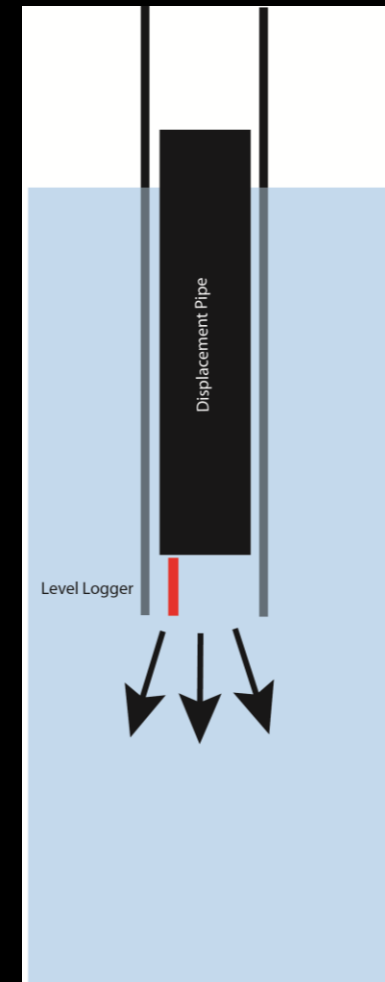
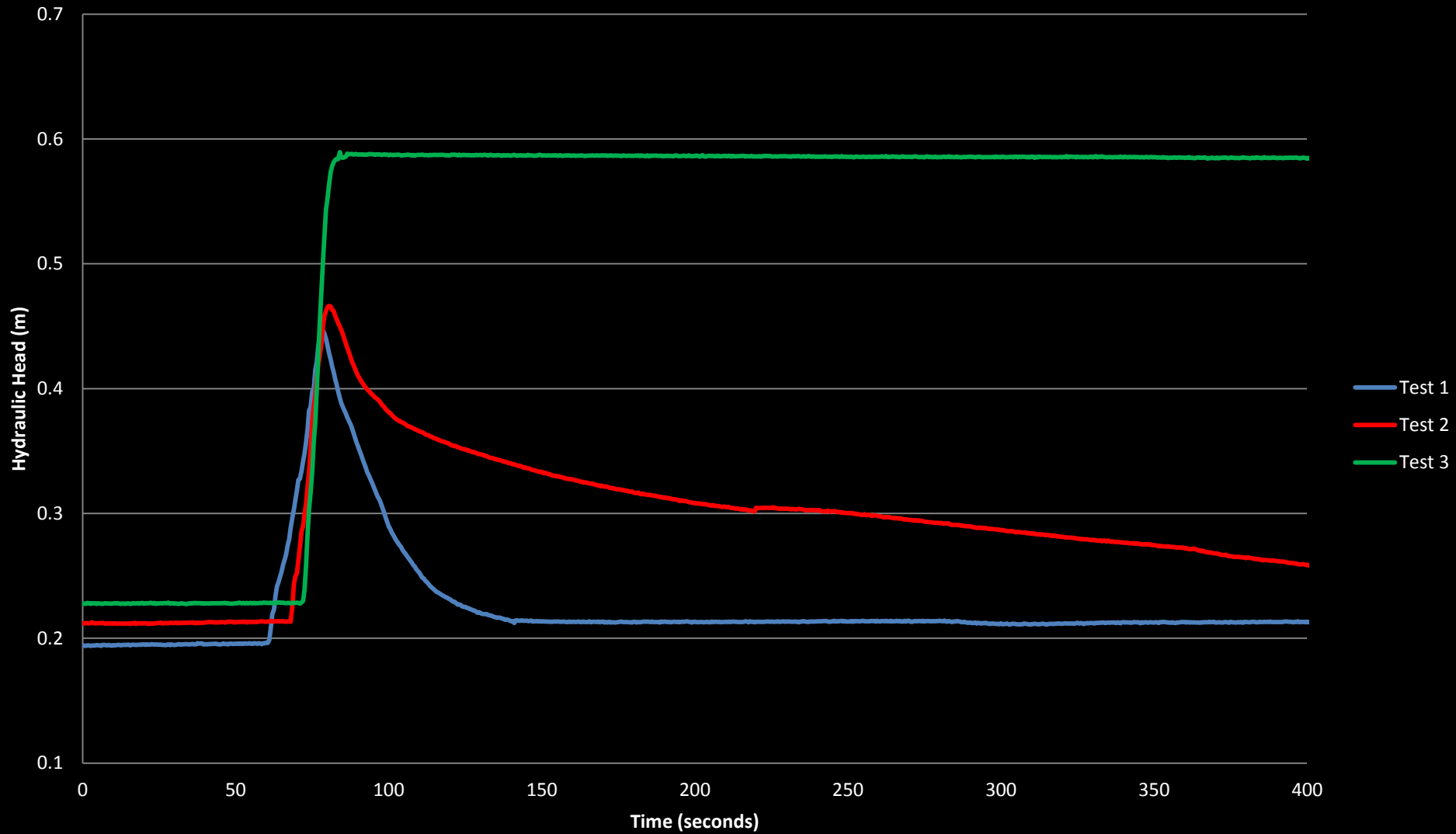


Figure 3a - Hydraulic Head vs. Time, Freshwater Percolation Seals Ice



Conclusions

- 1. Summer Arctic sea ice is melting rapidly.**
- 2. Fluid flow through sea ice mediates many processes of importance to understanding climate change and the response of polar ecosystems.**
- 3. Mathematics of composite materials, statistical physics and dynamical systems help us understand sea ice, and suggest rigorous frameworks for representing sea ice in climate models .**
- 4. Sea ice ecology is rich in interesting mathematics and bio-physics.**
- 5. This research will help to improve projections of climate change and the fate of Earth's sea ice packs and their ecosystems.**

THANK YOU

National Science Foundation

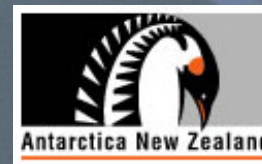
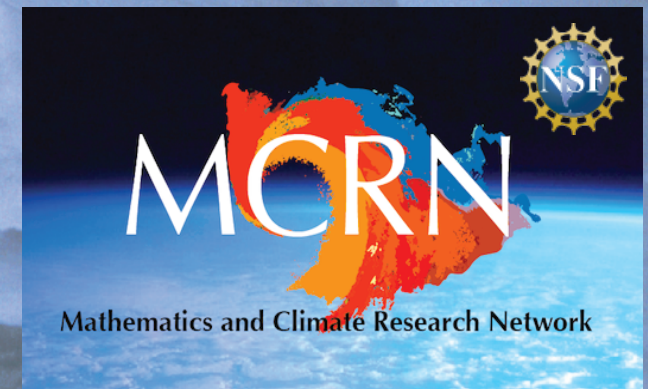
Division of Mathematical Sciences

Division of Polar Programs

Office of Naval Research

Arctic and Global Prediction Program

Applied and Computational Analysis Program



Buchanan Bay, Antarctica Mertz Glacier Polynya Experiment July 1999