

Electrical Detection of Granular Ice

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Abstract

The crystallographic structure of sea ice influences many of the key physical processes in the polar regions all of which play a major role in the Earth's climate system. There has been much recent interest in using electrical methods to remotely monitor temporal variations in the ice pack to aid in improving models of the key processes. Important to these models is the crystallographic structure of the ice and is difficult to determine electrically. In September-October 2012, in conjunction with crystallographic analyses, we made direct measurements of the vertical component of the bulk conductivity of first year Antarctic sea ice as participants in the Sea Ice Physics and Ecosystem Experiment II (SIPEX II) and found higher levels of local variability in the vertical DC conductivity in granular sea ice than in columnar sea ice. This variability is related to the differences in the way vertical connections grow in the two ice types. This work suggests that the vertical component of conductivity may be used as an aid in electrically determining the crystallographic structure of sea ice.

1 Introduction

The polar sea ice packs play a critical role in regulating the Earth's climate system and serve as sensitive indicators of climate change. In particular they play a major role in regulating gas exchange in the polar regions and are an important factor in the Earth's over all albedo. These important large scale processes depend on small scale processes with in the ice. For example, fluid flow through the porous sea ice is a major controlling component in the evolution of melt ponds which in turn affects the ice pack albedo[1], brine drainage and the evolution of salinity profiles [2][3], snow ice formation, where sea water floods the ice surface and then freezes[4][5], ocean ice-atmosphere CO_2 exchanges[6], convection enhanced thermal transport [7][8], and biomass build up fueled by nutrient fluxes[9][10][11,12]. Important properties such as fluid flow exhibit critical behavior which depends on the crystallographic structure of the ice. For

example in columnar ice it has been shown that the ice is effectively impermeable below brine volume fractions of 5% (Golden et al) while granular ice is impermeable for brine volume fractions below 10%(Golden et al). When using small scale models to understand these processes the importance of knowing the crystallographic structure becomes paramount. Recently investigations into using DC resistivity to remotely monitor the growth and evolution of sea ice throughout a season have shown promising results (Malcom ,Worby, Reid, Golden), however most of the studies focus on columnar ice and fail to resolve ice type with the exception of the detection of increased horizontal conductivity at the skeletal/platelet layer at bottom of fast ice(malcom 2014). While columnar ice is the most prevalent ice type in the Arctic, although the upper 10 cm of the Arctic ice is typically granular, the situation in the Antarctic is the drastically different. Nearly 40% of the Antarctic ice pack is made up of granular ice, of which, nearly a quarter is fine grained granular snow ice [4][18][19][20], with even higher fractions in some regions[26]. Given the importance of ice type in relation to important physical processes in the ice, it is thusly important to include a method to detect ice type in any remote sensing scheme.

We view sea ice as a two phase polycrystalline composite material made up of ice and brine, with the brine phase conducting and the ice phase insulating. In this way, the conductivity of the ice depends on the connectivity the brine phase throughout the ice column and exhibits critical behavior similar to fluid flow at the 5% threshold(Golden et al). In studies of polycrystalline composites the crystal orientation plays a major role in the properties of the given material such as electrical permittivity and conductivity(Gully , milton Cherk). Columnar sea ice crystals are typically oriented together with a horizontal c-axis while granular sea ice crystals are randomly oriented.(Omdset 1985 ; Weeks et al) This leads to higher variability of the electrical properties of granular sea ice on small local scales. It is this variability that can be exploited to electrically detect ice type.

During September through November of 2012, we made measurements of the vertical conductivity of first year columnar and granular sea ice off the east coast of Antarctica as participants of in the Australian Sea Ice Physics and Ecosystem Experiment (SIPEXII) aboard the ice breaker Aurora Australis. In this paper we compare our data to some established results as well as present an analysis of local scale variability of the electrical properties of granular ice which differ from that of first year columnar ice.

2 Methods and Measurement

In order to directly measure the vertical conductivity of the ice we employed a Wenner electrode array along 10 cm sections of ice cores, as illustrated in Fig 1. This method is similar to that used in (Golden et al vert cond). To make the measurement we used a AEMC DC resistivity meter. To facilitate the measurement, full length ice cores were extracted and holes were first drilled into the cores at 10 cm intervals and temperature probes inserted along the core. Next, slightly larger diameter holes were drilled into the previous temperature

probe holes with tight fitting nails inserted and used as electrodes for the Wenner array. The nails were slightly smaller than the holes to ensure a good electrical connection with the ice. With a 10 centimeter spacing between electrodes, current was injected by the outer probes and the potential difference measured at the inner two. This gave the resistance for the 10 cm section of the ice between the innermost probes. The cores were then bagged and rushed into a $-22C^{\circ}$ crystallography lab on board the Aurora for later analysis. In the lab the cores were cut into 10cm sections at the measurement holes and vertical thin sections cut from the center of the sections were extracted and placed between two cross-polarizing films showing the crystal structures of the corresponding to the resistance measurements. The outer halves of the sections were bagged and melted for bulk salinity measurements. The crystallography lab was cold enough to completely freeze the cores so that brine leakage was not a serious concern. The temperature(T) C° and salinity (S) PSU can then used to calculate the brine volume fraction ϕ corresponding to the resistance measurement using the Frankenstein-Garner relation shown in eq 1.

$$\phi = \frac{S}{1000} \left(\frac{49.185}{|T|} + 0.532 \right) \quad (1)$$

The vertical conductivity of a 10 cm section can be found using the measured resistance R . The vertical resistivity ρ_v and corresponding conductivity σ_v are obtained via $\rho_v = AR/L$, $\sigma_v = 1/\rho_v$ where A is the cross sectional area and L the length.

3 Theory

3.1 Conductivity in Columnar and Granular ice

As sea water begins to freeze the first ice crystals to form create a slush referred to as frazil ice. As this slush freezes granular ice forms which has crystals with random c-axis orientations that trap brine in between them. As further growth progresses crystals which have their c-axes aligned in the horizontal plane grow downward leading to the formation of vertical columns of ice dubbed columnar ice. An example of this ice can be seen in Fig 1a. In this type of ice brine inclusions and vertical tubes form between the subgrains of the ice aligned with the growth directions of the crystals (Meinen et al 2000, Meinen et al 1992). At low temperatures the brine inclusions are smaller and isolated from each other but as the sea ice warms they begin to connect up forming long vertical pathways in the ice (Meinen 2000 Golden xray). This vertical alignment leads to anisotropy in the conductivities of the ice as current flows preferentially along the elongated brine inclusions yielding an increased vertical conductivity. In addition, sea ice is typically transversely isotropic (Reid 2006, Sampson) yielding the same conductivities in all horizontal directions. The electrical anisotropy in transversely isotropic materials like sea ice can be quantified using the factor of anisotropy defined as $f = \sqrt{\sigma_h/\sigma_v}$ (Malet 1947 Reid 2006). One

can quantify the level of crystallographic anisotropy using the crystal anisotropy factor. This is defined as $A = \Sigma C_v / \Sigma C_h$, where C_v and C_h are the size of the vertical and horizontal projections of each individual c-axis measurement from a thin section. For both parameters a value of 1 indicates isotropy while $A = 0$ indicates that all c-axes lie in the horizontal plane. Examples of values of A are $A = 0.23$ and 0.14 for columnar ice and $A = 0.67$ for platelet ice. (Jones et al 2012) Typical values of f range from 0.2 to 0.7 with the higher values possibly indicating granular ice (reid 2006 Sampson)

In contrast to columnar ice, granular frazil and granular snow ice are comprised of crystals with isotropically distributed c-axes which trap the conductive brine between them. Given its structure one might expect granular ice to have an isotropic bulk conductivity, however this is not the case. The conductivity in the vertical direction remains larger does not differ much from that of columnar ice. This may suggest that anisotropic secondary pores (such as brine tubes and channels which form as the ice warms and gravity pulls the brine down) control the resistivity structure rather than the isotropic primary pore space (Jones et al 2010). This is consistent with our findings as well as we see no clear difference in the over all vertical conductivities of our granular and columnar measurements as a whole. However the horizontal conductivity of granular ice is typically higher. This has been observed in Jones et al 2012 using cross-borehole tomography to measure the horizontal and vertical conductivities of first year Antarctic sea ice. They found increased horizontal conductivities near the upper granular layer of the ice as well as near the bottom platelet layers due to a the larger number of horizontal connections that result from the platelet crystal structure of the ice. Jones et al. were also able to show that as crystallographic anisotropy increased factor of electrical anisotropy f increased as well. This implies that as the crystal structure of the ice becomes more isotropic the bulk conductivity does as well.

3.2 Thermal Evolution of Columnar and Granular ice

Given the electrical anisotropy of sea ice and the apparent control of its resistivity structure by the connectivity of the brine inclusions it is important to understand how these structures evolve with increases in temperature and porosity. In particular we are interested in the how vertical connectivity of the pore space changes as it is the controlling factor in the vertical conductivity of sea ice.

The evolution of connectivity in columnar ice has received more attention than that of granular ice (Eiken et al 2000 , golden et al xray) how ever it is clear in these studies that as the temperature of columnar sea ice increases, and thus porosity, the pore space connections that form are oriented primarily in the vertical direction and reside between the vertically aligned columnar ice crystals. It is only at high brine volume fractions that more complicated geometry is observed. In a NMR study (Bock and Eicken 2005) of the thermal evolution of pore space connectivity of samples of winter columnar and granular sea ice taken near Barrow Alaska, it was observed the connections which formed in the

granular samples, as temperature was increased, had a more complex morphology with a combination of horizontal and vertical connections. Those of the columnar sea ice were primarily vertical and constrained within the lamellar plane of the columnar ice crystals. This difference in the evolution of connectivity has implications for behavior of the vertical conductivity of a localized region of granular or columnar sea ice. We see evidence of this in our thin sections as well illustrated in figure 2. The two granular sections are from core 99 and have brine volume fractions of $\phi = 0.834$ and $\phi = 0.836$ but differ with vertical formation factors of $F_v = 0.02$ and $F_v = 0.011$ respectively with the higher conductivity corresponding to the sample with the elongated vertical connection. In (Golden et al. 2007) it was observed that the fractional connectivity, defined as the proportion of inclusions at the upper surface which are also connected to the lower surface, for a cylindrical sample of lab grown columnar sea ice with a height of 8mm and diameter of 21mm, increased linearly with increasing porosity for brine volume fractions above $\phi_c = 5\%$. (Figure?) While no similar data for granular ice was found, we would expect different behavior. Due to the random distribution of the c-axes of the ice crystals in granular ice, there is less to constrain the direction of the pore space expansion with an increase temperature. This would imply a variety of levels of vertical connectivity for a given brine volume fraction in granular ice and thusly a wider variation in values of vertical conductivity.

3.3 Percolation Theory and Critical Behavior

Percolation theory for both lattice and continuum models applies to materials where the connectedness of one phase dominates the effective behavior of the material as a whole. In sea ice it is the connectedness of the brine phase which dominates the effective electrical properties of the ice as a whole (Golden et al.).

Consider the infinite square ($d = 2$) or cubic ($d = 3$) network of bonds joining nearest neighbor sites on the integer lattice \mathbb{Z}^d . The bonds are assigned conductivities of $\sigma_0 > 0$ (open) or 0 (closed) with probabilities p and $1 - p$ respectively. There is a critical probability p_c called the *percolation threshold* where an infinite, connected set of open bonds first appears. In $d = 2$ $p_c = 1/2$ and in $d = 3$ $p_c \approx 1/4$. Let $\sigma(p)$ be the conductivity of this random network of bonds in the vertical direction. For $p < p_c$, $\sigma(p) = 0$. For $p > p_c$, near the threshold $\sigma(p)$ exhibits power law behavior,

$$\sigma(p) \sim \sigma_0(p - p_c)^t \quad \text{as} \quad p \rightarrow p_c^+, \quad (2)$$

where t is the conductivity critical exponent. In $d = 3$, it is believed that $t \approx 2$ (Torquato 2002 perm) and there is a rigorous bound (Golden 1990) that $t \leq 2$.

In (Golden et al not out) it was observed that the vertical conductivity of columnar sea ice exhibits critical behavior at a critical brine volume fraction $\phi_c \approx 5\%$. This corresponds to the volume fraction in the *rule of fives* (Refs) where the brine channels first begin to connect on large scales. Below this percolation threshold the vertical conductivity, while not zero, shows little growth

while after this threshold, when the brine phase begins to connect on a large scale, the conductivity increases more rapidly and can be modeled by percolation theory according to the model

$$F(\phi) = F_0(\phi - 0.05)^2 = 8.6(\phi - 0.05)^2, \quad (3)$$

where $F(\phi) = \frac{\sigma_v}{\sigma_b}$ is the vertical formation factor defined as the ratio of the vertical conductivity σ_v and the conductivity of the brine σ_b . The conductivity of the brine can be calculated from the temperature T via (Stogryn and Desargant, 1985)

$$\sigma_b = -T \exp(0.5193 + .08755T) \Omega^{-1}m^{-1}, \quad T \geq -22.9^\circ C. \quad (4)$$

The scaling factor F_0 is estimated in (Golden et al) to fall in a range of $6 \leq F_0 \leq 24$ using critical path analysis(Need ref). The factor $F_0 = 8.6$ comes from a statistical best fit of vertical conductivity data from the SIPEX I cruise in 2007.

3.4 Archie's Law

Archie's law(Archie, 1942) is an empirical equation relating the bulk conductivity σ^* of a porous medium to its porosity and the conductivity σ_f of the fluid occupying the pore space,

$$\sigma^* = a\sigma_f\phi^m. \quad (5)$$

In this relation ϕ is the relative volume fraction of the fluid volume, or porosity, and a is a scaling factor often taken to be 1, which yields the correct limiting behavior as $\phi \rightarrow 1$. In sea ice where we expect different behavior in different volume fraction and crystallographic regimes there is no particular reason for a to be taken as 1. The exponent m depends on the geometry of the solid phase of the porous medium, such as the shape of the grains in porous rock or sand.

While percolation theory describes conductivities for $\phi > 5\%$, Archie's Law is useful as it can describe the conductivity for systems with connectivity all the way down to $\phi = 0$. For our purpose we take $\sigma^* = \sigma_v$, $\sigma_w = \sigma_b$ and ϕ to be the brine volume fraction of the ice. We can then look at the formation factor

$$F = \frac{\sigma_v}{\sigma_b} = a\phi^m, \quad (6)$$

where σ_b depends on temperature via eq 4. Archie's law has been employed to model the vertical conductivity of ice successfully by many others(Thysen et al, 1974; Reid et al 2006; Ingham et al, 2008 Jones et al 2010). These previous results find $m = 1.75$ for the vertical conductivity σ_v of the ice and were measured indirectly. In (Golden et al), which represents the first direct measurements of the vertical component of the bulk conductivity, an exponent of $m = 1.9$ was found using a least squares inversion. This data set however had very few points below $\phi = 5\%$, the point at which the ice begins to connect at large scales. When analyzing our data set as a whole we find good agreement

with the exponent $m = 1.75$ using statistical best fits and enforcing a condition of $a = 1$. However when a is allowed to be determined by the data we obtain $F = .36\phi^{1.38}$, the values for a and m remain close for both the granular and columnar sets when analyzed separately.

One of the underlying assumptions in Archie’s Law is that porosity and connectivity vary continuously. If we wish to apply Archie’s Law to the vertical conductivity of sea ice we must assume that small changes in porosity will give rise to small changes in vertical connectivity. This is certainly true in columnar ice due to the preferential alignment of the crystals and growth of vertical connectivity mentioned above. However, in granular ice and in particular fine grained granular ice, where the crystal c-axes are isotropically distributed small changes in porosity may lead to increases in horizontal connectivity rather than simply vertical connectivity. Depending on how the crystals are distributed one would expect a larger variation in the vertical formation factor of granular ice at a given brine volume fraction. Indeed, when considering the vertical fluid permeability of granular ice, it is shown in (Golden et al perm) that the ice is effectively impermeable for brine volume fraction below $\phi_c = 10\%$. In contrast, in (Golden et al 2007) it is shown that columnar ice becomes vertically permeable at a lower critical volume fraction of $\phi_c = 5\%$. This illustrates that vertical connections grow more slowly in granular ice than columnar as brine volume increases. For these reasons we expect that granular ice will show more variation in F_v with brine volume fraction on the local scale than columnar ice. We also expect to see less of a power law behavior at the local scale due to the increased variability.

4 Results and Discussion

4.1 Comparison to Established Results

In this section we will simply compare our data to established results. In relation to Archie’s Law for the vertical formation factor $F_v = \phi^m$, we performed statistical best fits on our data sets separated by ice type as well as the combined data set. We performed fits forcing the scaling parameter $a = 1$ and obtained $m = 1.76$ for our granular ice and $m = 1.71$ for the columnar ice. When combining the data sets we obtain $m = 1.75$ all in close agreement with the value of $m = 1.75$ measured for the vertical conductivity in previous results(Reid 2006 and Jones 2010).

When considering percolation theory for $\phi > 5\%$ we observe good agreement at high brine volume fractions and it should be noted that percolation theory does not apply to volume fractions below $\phi_c = 5\%$. We do note that much of the data taken during SIPEX 2 in 2012 resides above that the data taken during SIPEX I. The full data sets are shown in Fig 3

4.2 Local Variability

As discussed above, we expect to see larger variability in the vertical formation factor F_v on local scales in granular ice than in columnar ice. In fact this is what we see when comparing the F_v vs ϕ on a core by core basis. Examples of this data are summarized in Fig 4. For samples of columnar ice it is apparent that F_v varies continuously with ϕ with the exception of 1 data point in cores 50 and 51, which incidentally occurs at the cusp of the typical c-curve of brine volume fraction vs depth. For the samples of granular ice no clear relationship is immediately apparent. In core 98, for example, there are 5 data points with $\phi \approx 8\%$ which take on different values of F_v between $F_v = 0.01$ and $F_v = 0.024$ more than doubling the conductivity. This is presumed to be a result in differences in vertical connectivity at the same brine volume fractions in granular ice.

In order to quantify this we assume a power law behavior in accordance with Archie's Law eq 6 and perform linear best fits of the linearized log-log data. In the first set of fits we do not assume $a = 1$ as a way to test for local linear dependence. The results are summarized in table 4.2. When comparing the R^2 statistics for the columnar vs granular samples, we see higher values for columnar ice than for granular ice indicating a higher likelihood of linear correlation. In the columnar samples R^2 ranges from $R^2 = 0.43$ to $R^2 = 0.92$ while the range for the granular samples is $R^2 = 0.014$ to $R^2 = 0.28$ with only 3 of the 7 above 0.05. Core 54 was a mix of mostly columnar and some large grain granular ice and also shows strong correlation with an R^2 value of 0.74. We would expect columnar ice to be the controlling factor in a mixed sample as it should be the vertical connections which dominate the behavior of the F_v .

When comparing the P-values for slope of columnar vs granular ice, we see much lower P-values for columnar ice than for granular ice. In this case a low P-value implies a rejection of the null hypothesis of no correlation, while a high P-value implies no linear correlation. Typically, a P-value above 0.5 is considered grounds to accept the null hypothesis of no correlation. In the columnar samples all of the P-values fall below this threshold with values ranging from $P = 0.008$ to $P = .15$ for the slopes while in the granular ice 4 of the 7 cores have P-values above 0.7 with the other 3 ranging from $P = 0.21$ to $P = 0.35$. When comparing the standard errors of the slope for the two data sets, we find that the columnar samples vary less from the model than granular samples with standard errors varying from $S = 0.30$ to $S = 0.88$. The range for granular samples is $S = .87$ to $S = 2.12$. All of these statistics point to a higher variation in the vertical conductivity of granular sea ice in a local region.

Assuming Archie's Law with $m = 1.75$ and $a = 1$ (Reid 2006 Jones et al 2010) is a good model for the vertical conductivity we would expect to obtain a linear fit with a slope close to the exponent 1.75 and intercept close to zero. For our columnar ice samples we obtain Archie exponents ranging from $m = 1.56$ to $m = 1.90$ and y intercepts ranging from $b = -0.24$ to $b = 0.25$ corresponding to range of scaling factors of $a = 0.60$ to $a = 1.80$. In the granular ice samples we see drastically different results with exponents ranging from $m = 0.43$ to

Core	Ice Type	R^2	Slope	Std. Error	P-value	Intercept	Std. Error	P-Value
44	Col	0.92	1.90	0.3	0.008	0.25	0.37	0.54
50	Col	0.44	1.56	0.88	0.14	-0.21	0.98	0.83
51	Col	0.43	1.38	0.8	0.15	-0.24	0.99	0.82
54	Mix	0.74	2.41	0.58	0.006	0.65	0.72	0.39
69	Gra	0.02	0.43	1.42	0.71	-1.65	1.12	0.28
75	Gra	0.05	-0.36	0.96	0.78	-2.60	1.26	0.18
77	Gra	0.28	2.99	2.12	0.21	1.57	2.60	0.57
79	Gra	0.018	0.55	1.81	0.77	1.40	2.30	0.50
98	Gra	0.014	0.07	0.97	0.95	-1.90	1.19	0.20
99	Gra	0.22	01.20	1.28	0.35	-0.44	1.28	0.70
108	Gra	0.17	0.96	0.87	0.31	-1.02	1.10	0.39

Table 1: Here we present the results of the linear regression analysis where the scaling factor a in Archie’s Law was allowed to be chosen by the data. We see strong linear correlation and less variability in columnar ice than in granular ice.

$m = 2.99$ with 5 of the 7 all less than 1. The y intercepts range from $b = -2.60$ to $b = 1.57$ with 6 of the 7 having magnitude larger than 1. This corresponds to a range of scaling factors of $a = 0.003$ to $a = 37.2$. However as shown in Fig 3 we find that for the data set as a whole, both columnar and granular ice are well represented by the model $F_v = \phi^{1.75}$. It is thus useful to repeat our analysis of the log-log linearized data forcing the scaling factor to be $a = 1$, summarized in table 4.2. When we do this we see excellent agreement with the model for both ice types suggesting that on average Archie’s Law is indeed a good model.

5 Conclusion

In all, over 81 direct measurements of the DC vertical conductivity of Antarctic sea ice were made and matched to their crystallographic structure. The measurements compare well to a number of established results (Golden et al ; Reid et al 2006 ; Jones et al 2010 and 2014). While no detectable difference in the vertical conductivity was found between the ice types on average, a higher degree of local variability of the vertical formation factor F_v was found in granular ice. This is most likely related to effect the crystallographic structure has on the way in which vertical connections form in the pore spaces of the two ice types. This implies that measurements of F_v could be used to distinguish between ice types. This is paramount when considering the remote monitoring of sea ice through out a season. The vertical fluid permeability in particular is sensitive to crystallographic structure and exhibits different critical behavior depending on the ice type. Columnar ice is effectively impermeable for brine volume fractions below $\phi_c = 5\%$ (Golden et al 2007) while for granular ice there is a critical threshold of closer to $\phi_c = 10\%$ (Golden et al perm). This has

Core	Ice Type	R^2	Slope	Std. Error	P-value
44	Col	0.999	1.73	0.02	9×10^{-8}
50	Col	0.995	1.75	0.07	2×10^{-6}
51	Col	0.990	1.57	0.06	1×10^{-6}
54	Col	0.990	1.88	0.02	4×10^{-11}
69	Gra	0.990	1.75	0.06	2×10^{-8}
75	Gra	0.997	1.69	0.05	6×10^{-5}
79	Gra	0.993	1.69	0.06	8×10^{-8}
98	Gra	0.995	1.65	0.06	8×10^{-6}
99	Gra	0.994	1.68	0.05	6×10^{-7}
108	Gra	0.996	1.76	0.06	6×10^{-9}

Table 2: Here we present the results of the linear regression analysis with the scaling factor $a =$ for Archie’s law. In this case we strong correlation in both columnar and granular data.

severe implications for the biological and physical processes in the ice and thus any models used to understand them. This makes a determination of the crystal structure extremely important. This work demonstrates that that the vertical component of the bulk conductivity could be used to aid in the determination of crystallographic structure of sea ice using electrical methods.

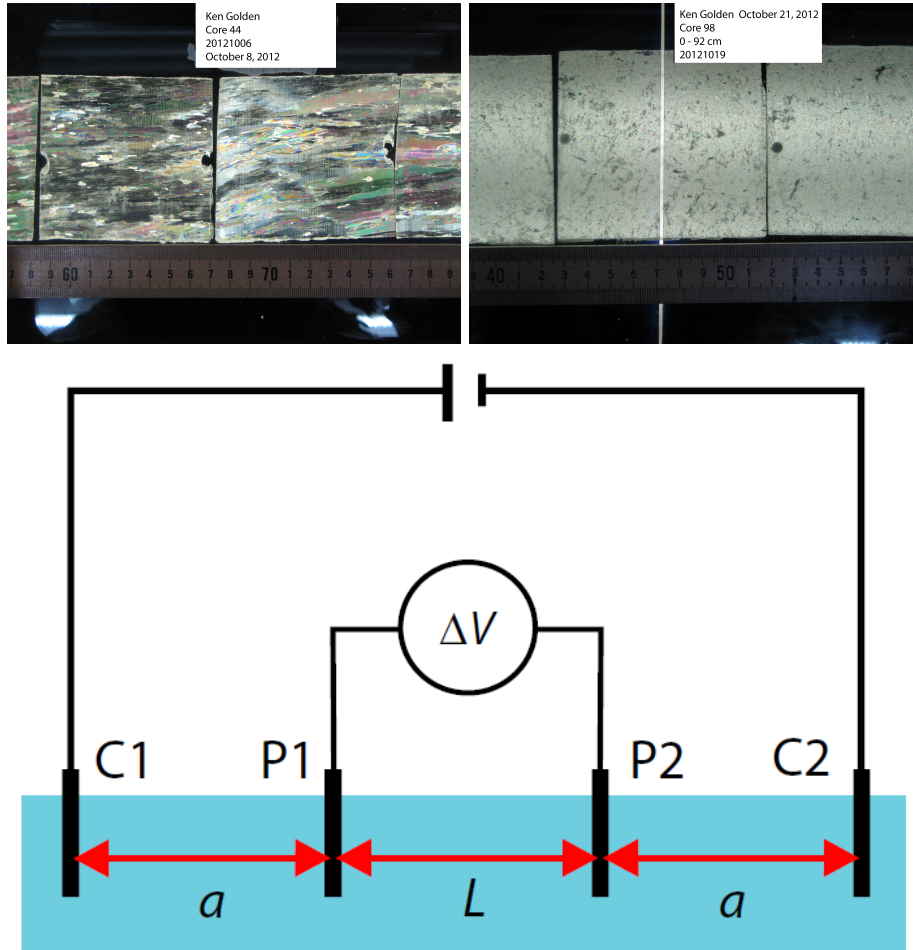


Figure 1: Top: Images of columnar ice and granular in the measured 10 cm sections. Bottom: Illustration of our direct measurement set up. Current is injected through the outer probes and the potential difference measured between the inner two yielding a resistivity measurement.

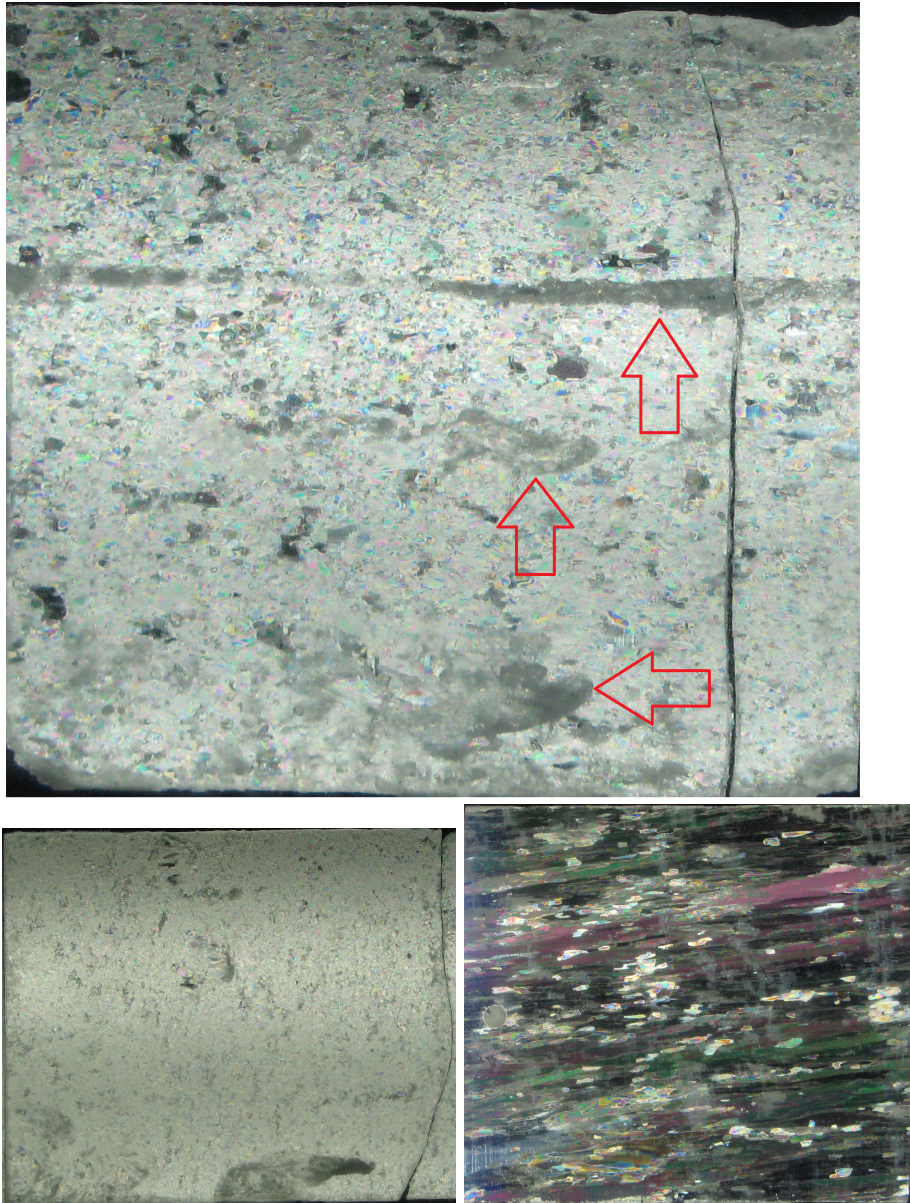


Figure 2: A: 10 cm section of granular ice from core 99. Arrows indicate pore spaces which show differences in the shape of pore space connectivity in granular ice. B: 10 cm section of granular ice from core 99 with a similar brine volume fraction to the section shown in A, but with little to no vertical connectivity. C: 10 cm section of columnar ice from Core 44 showing the vertical alignment of the pore spaces.

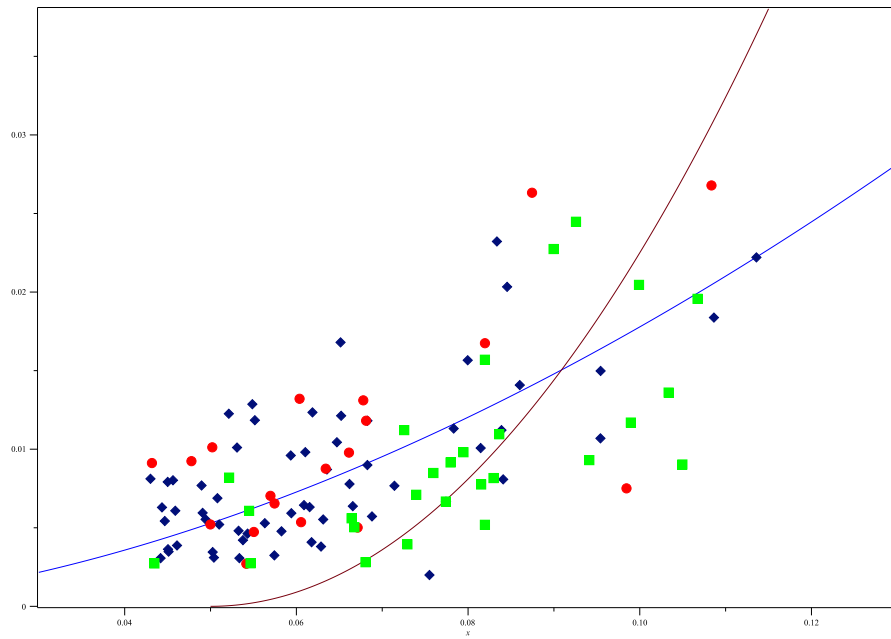


Figure 3: Here we display all of our granular and columnar data in comparison with predictions from Archie's law with $m = 1.75$ (Blue curve) and Percolation Theory (red curve). Diamonds represent granular ice, circles columnar ice from SIPEX II and squares columnar ice from SIPEX I in 2007.

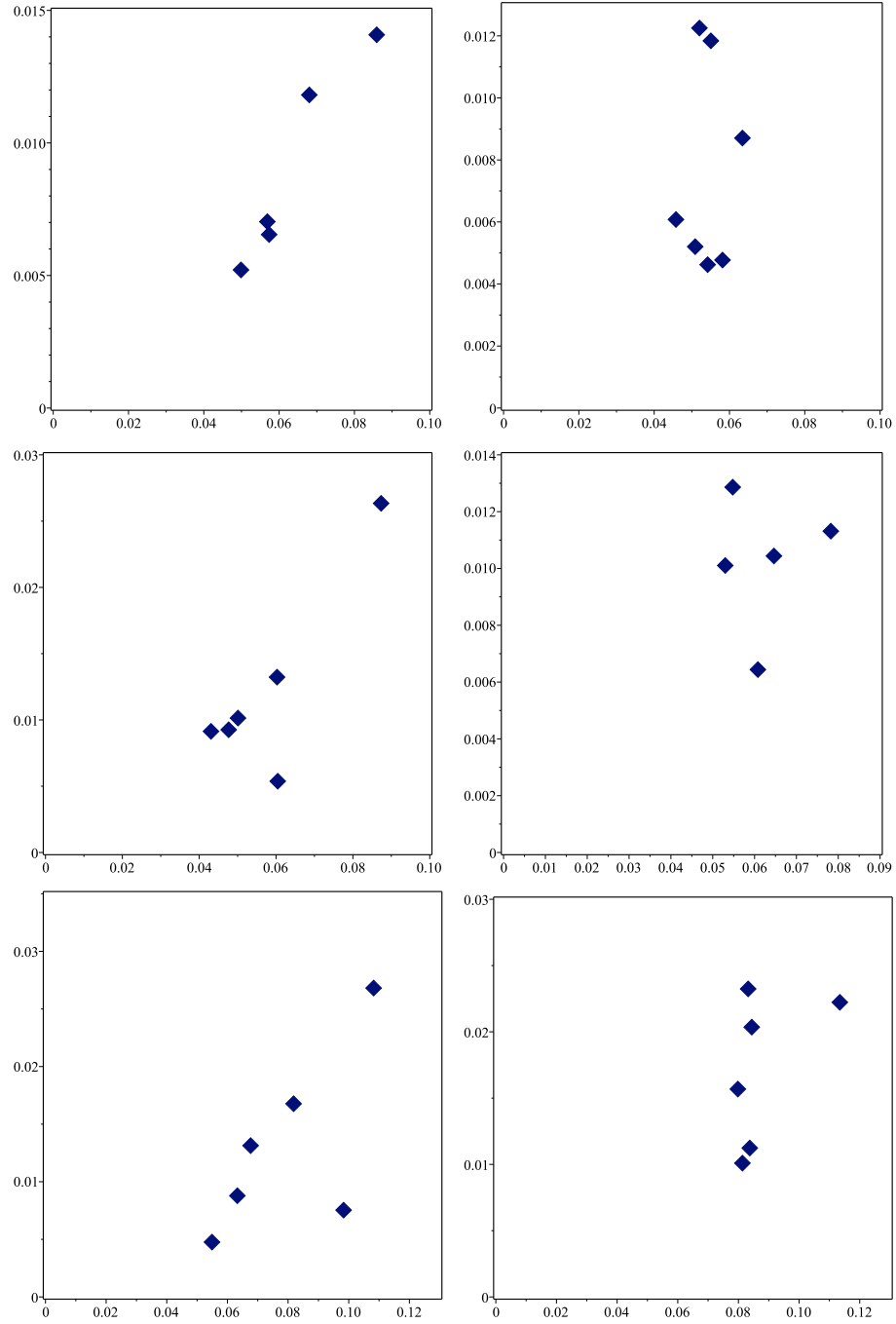


Figure 4: Left Column: Three plots from Cores 44,50,51 of F_v vs ϕ for columnar ice showing continuous behavior. Right Column: Three plots of Cores 77, 79, 99 showing high variability