

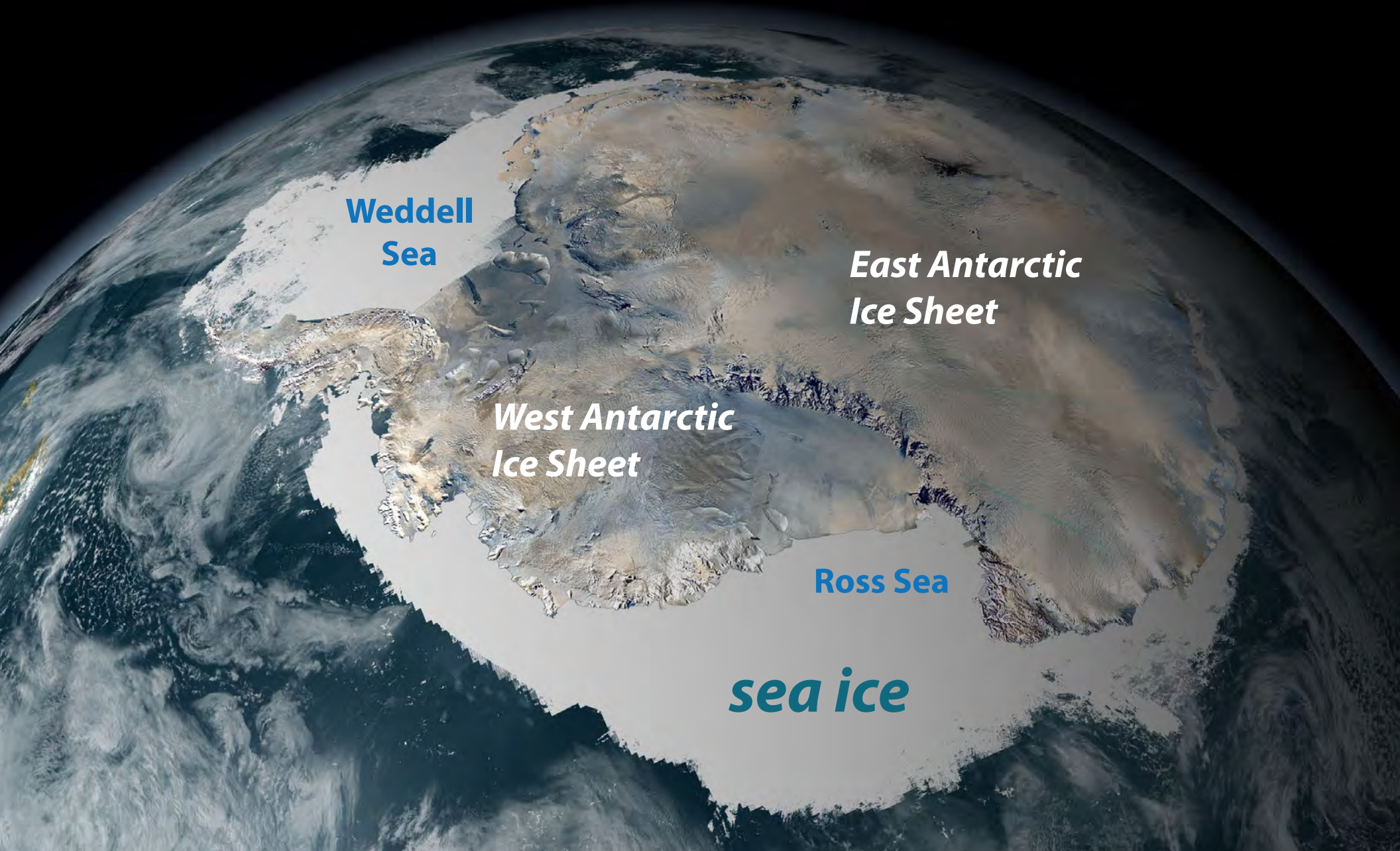
# MODELING SEA ICE *in a changing climate*

**Kenneth M. Golden**  
Department of Mathematics  
University of Utah



# ***ANTARCTICA***

southern cryosphere



**Weddell  
Sea**

***East Antarctic  
Ice Sheet***

***West Antarctic  
Ice Sheet***

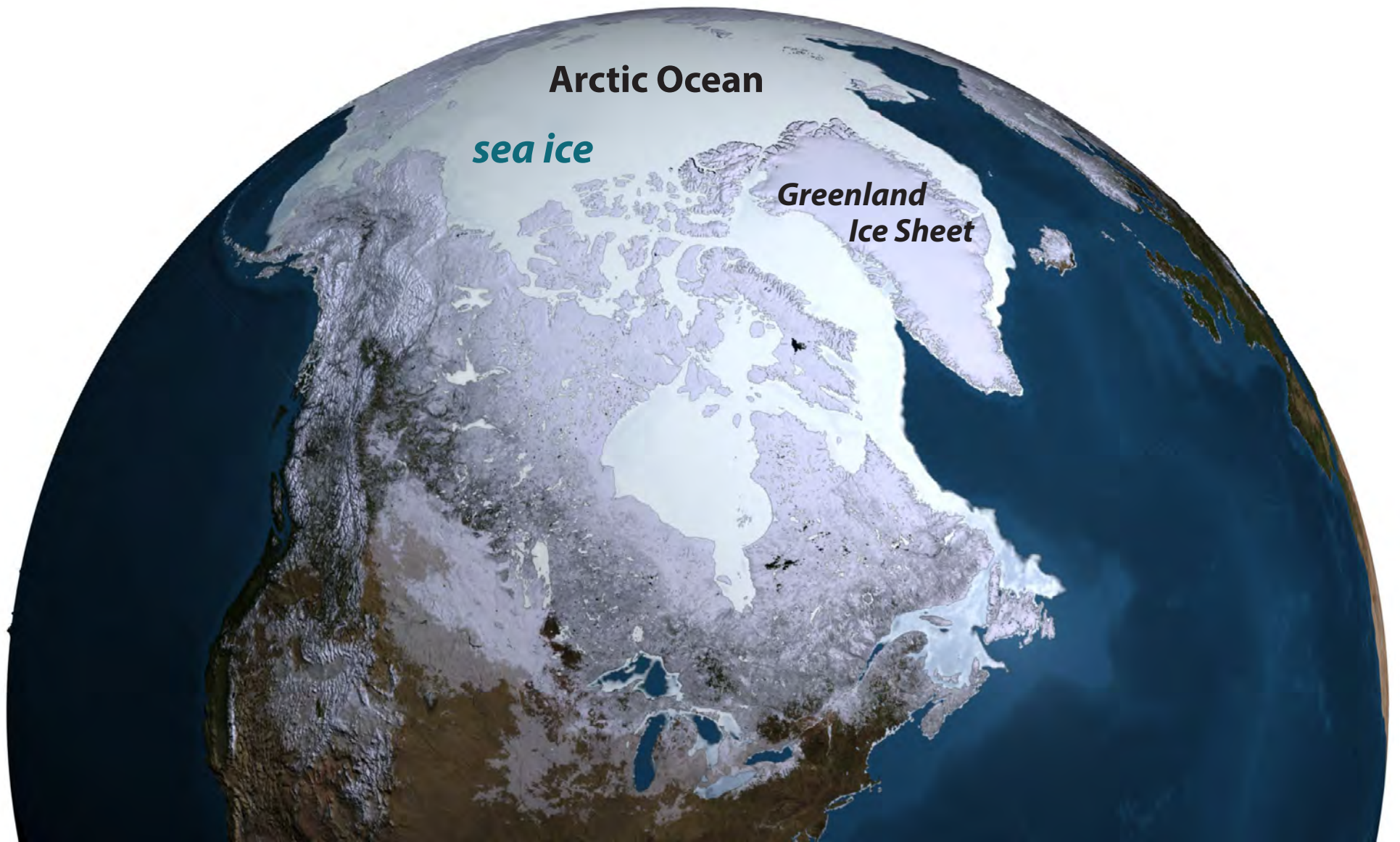
**Ross Sea**

***sea ice***



# ***THE ARCTIC***

## **northern cryosphere**





# SEA ICE covers 7 - 10% of earth's ocean surface

- boundary between ocean and atmosphere
- mediates exchange of heat, gases, momentum
- global ocean circulation
- indicator and agent of **climate change**





# polar ice caps critical to global climate in reflecting incoming solar radiation



white snow and ice  
reflect

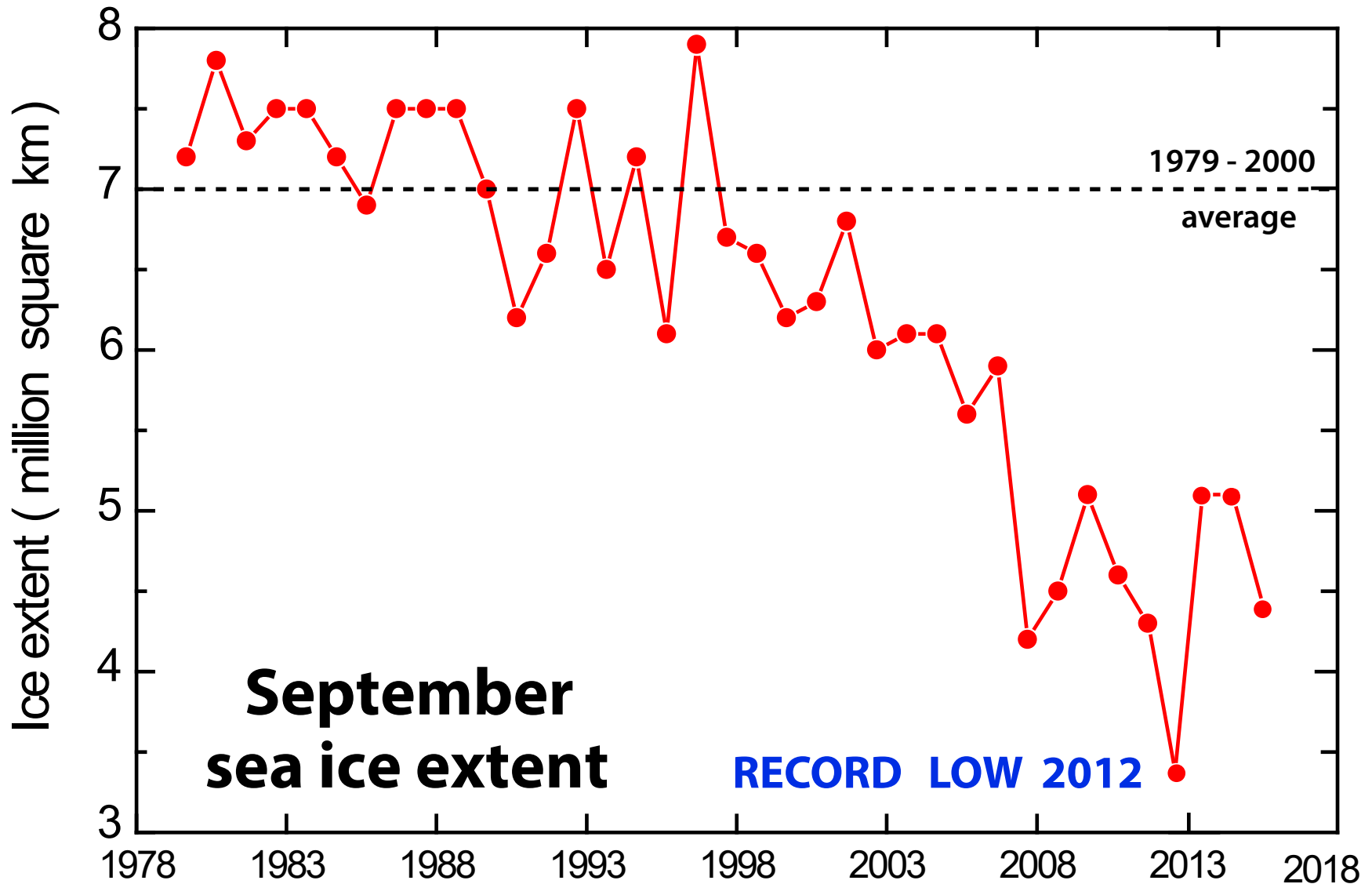


dark water and land  
absorb

$$\text{albedo } \alpha = \frac{\text{reflected sunlight}}{\text{incident sunlight}}$$



# *the summer Arctic sea ice pack is melting*

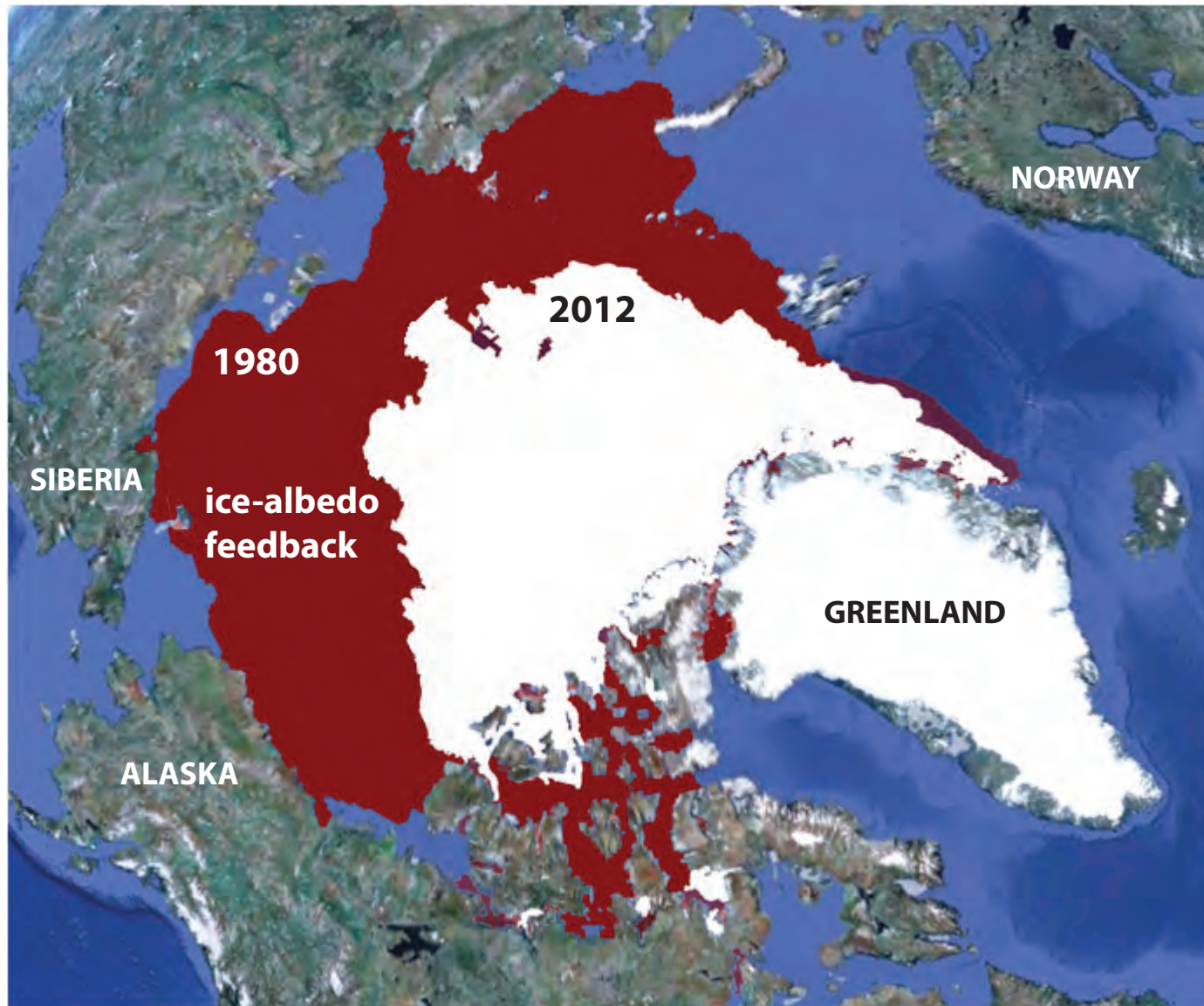




# Change in Arctic Sea Ice Extent

September 1980 -- **7.8** million square kilometers

September 2012 -- **3.4** million square kilometers





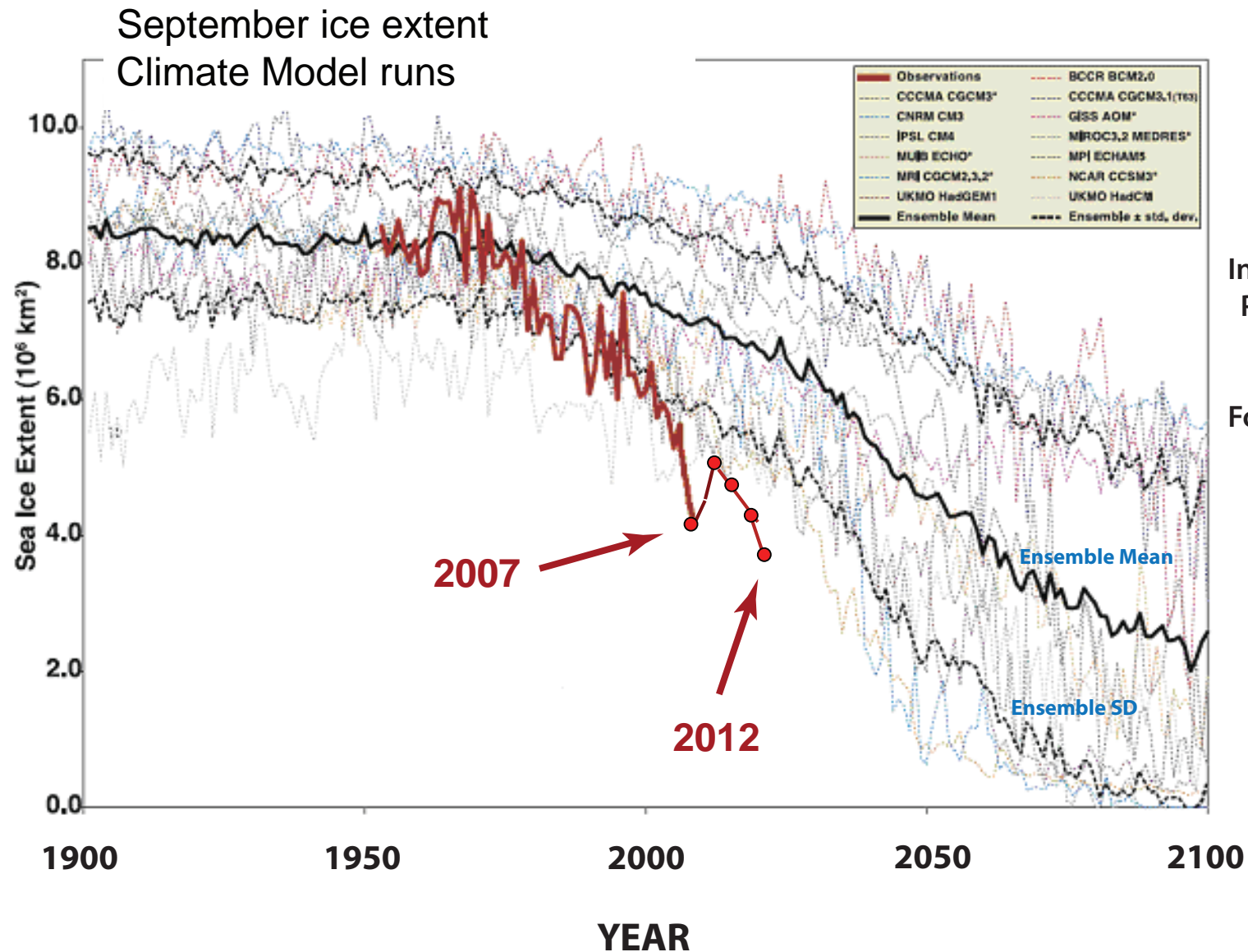


***recent losses  
in comparison to  
the United States***



# Arctic sea ice decline - faster than predicted by climate models

Stroeve et al., GRL, 2007



**IPCC AR4  
Models**

Intergovernmental  
Panel on Climate  
Change (IPCC)

Fourth Assessment  
AR4, 2007

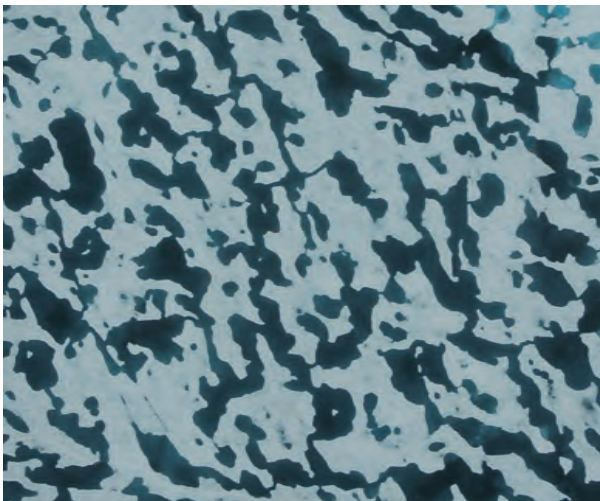


# challenge

represent sea ice more rigorously in climate models

*account for key processes*

*such as melt pond evolution*



Impact of melt ponds on Arctic sea ice  
simulations from 1990 to 2007

Flocco, Schroeder, Feltham, Hunke, *JGR Oceans* 2012

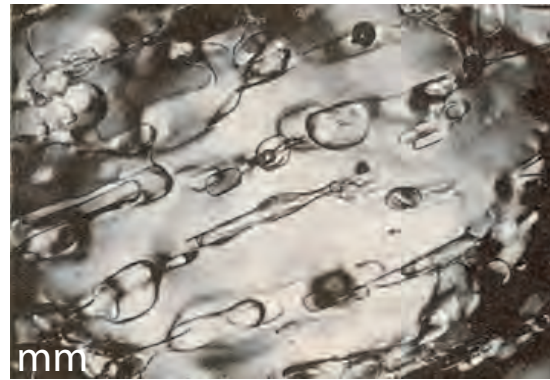
**For simulations with ponds  
September ice volume is nearly 40% lower.**

... and other sub-grid scale structures and processes

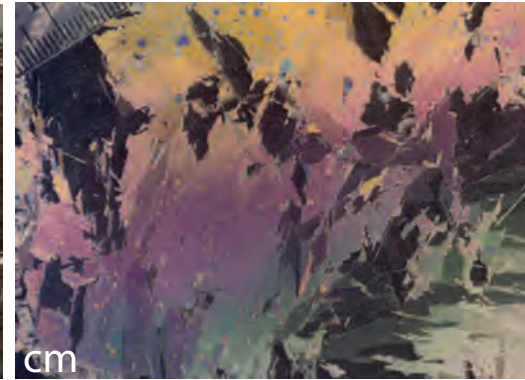
*linkage of scales*

***sea ice is a multiscale composite***  
displaying structure over 10 orders of magnitude

0.1 millimeter



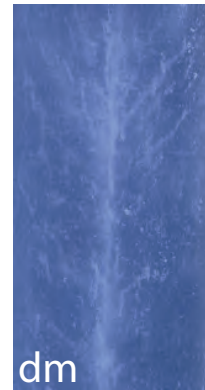
brine inclusions



polycrystals



horizontal

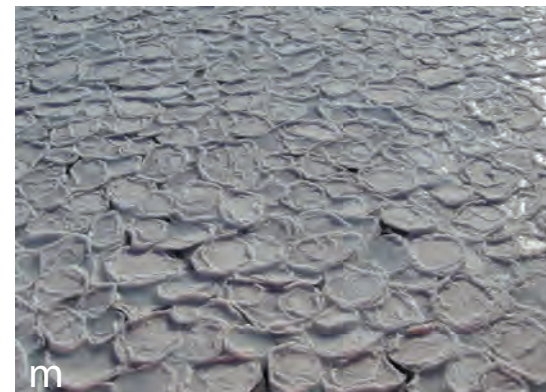


brine channels



vertical

1 meter



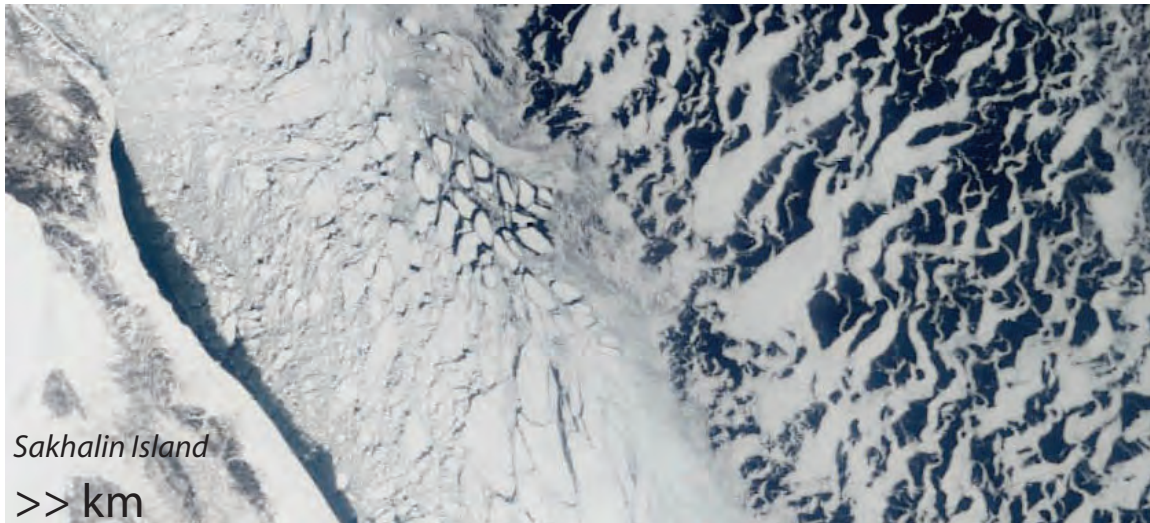
pancake ice



1 meter



100 kilometers



# ***What is this talk about?***

***Using the mathematics of composite materials and statistical physics to study sea ice structures and processes ... to improve projections of climate change.***

1. Global climate models and sea ice components
2. Fluid flow through sea ice, percolation
3. Homogenization for composite media  
remote sensing, inversion, advection-diffusion
4. Ocean waves and the marginal ice zone (MIZ)
5. Arctic and Antarctic field experiments
6. Evolution of Arctic melt ponds, fractal geometry

***critical behavior***

***cross-pollination***



# Global Climate Models

Climate models are systems of partial differential equations (PDE) derived from the basic laws of physics, chemistry, and fluid motion.

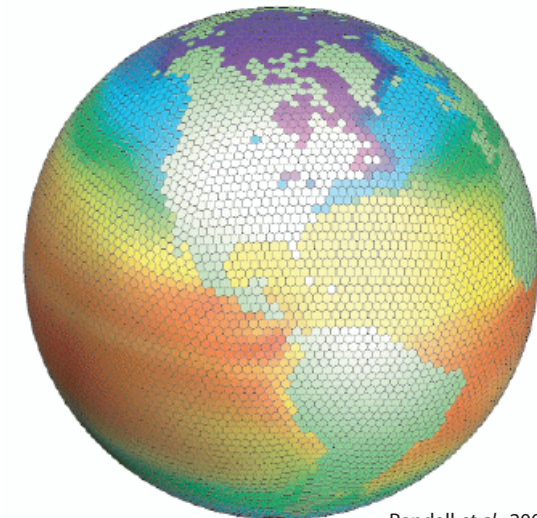
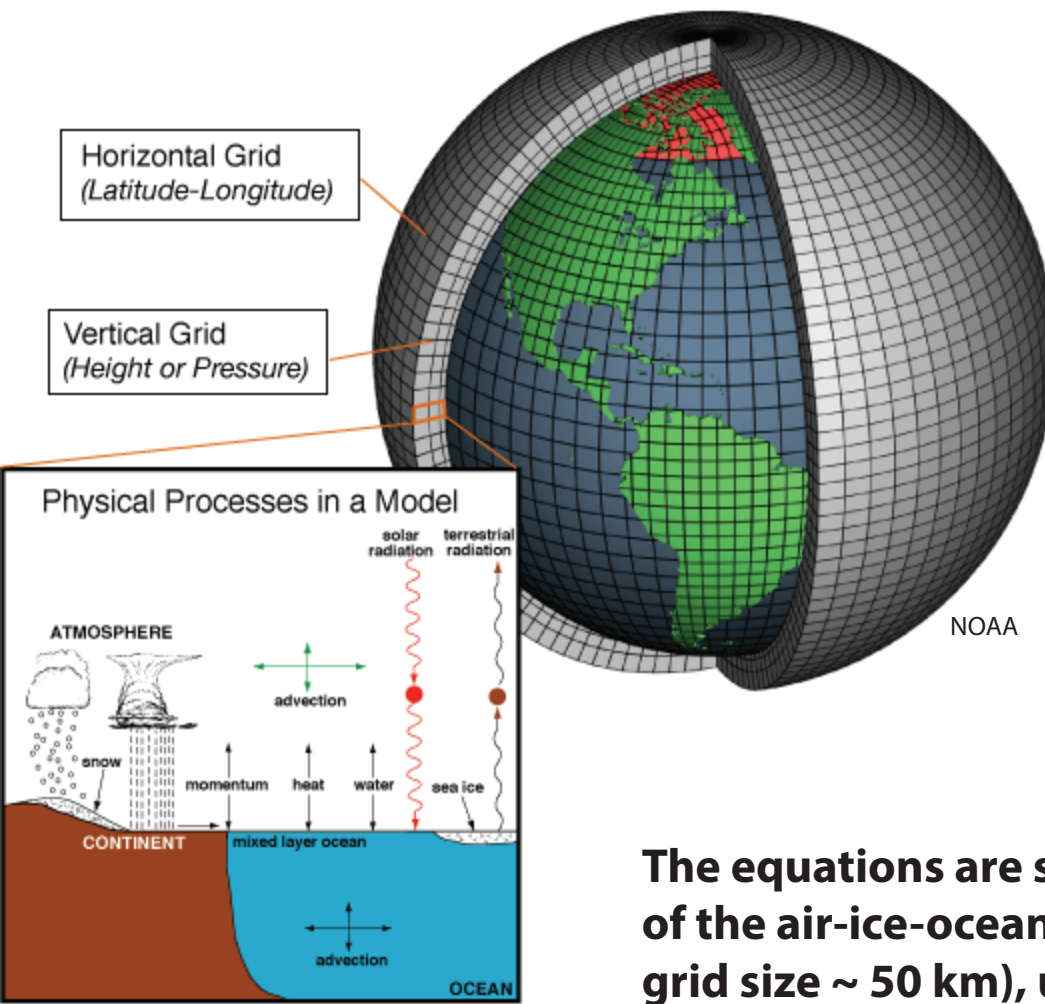
They describe the state of the ocean, ice, atmosphere, land, and their interactions.

The equations are solved on 3-dimensional grids of the air-ice-ocean-land system (with horizontal grid size ~ 50 km), using very powerful computers.

key challenge :

*incorporating sub - grid scale processes*

linkage of scales

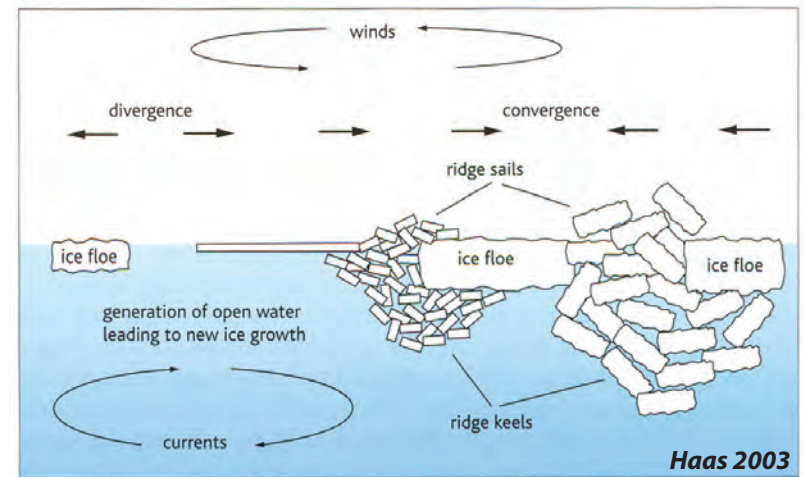


# sea ice components of GCM's

What are the key ingredients -- or **governing equations** that need to be solved on grids using powerful computers?

1. Ice thickness distribution  $g(x, y, h, t)$  evolution equation **dynamics**  
(Thorndike *et al.* 1975) **+ thermodynamics**

**nonlinear PDE incorporating ice velocity field  
ice growth and melting  
mechanical redistribution  
- ridging and opening**



2. Conservation of momentum, stress vs. strain relation (Hibler 1979)

**$F = ma$  for sea ice**

Coriolis, air and water drag,  
floe - floe interactions, ...

**dynamics**

3. Heat equation for sea ice and snow

evolution of temperature field in ice  
brine convection

**thermodynamics**

**+ balance of radiative and  
thermal fluxes on interfaces**

(Maykut and Untersteiner 1971)



***sea ice microphysics***

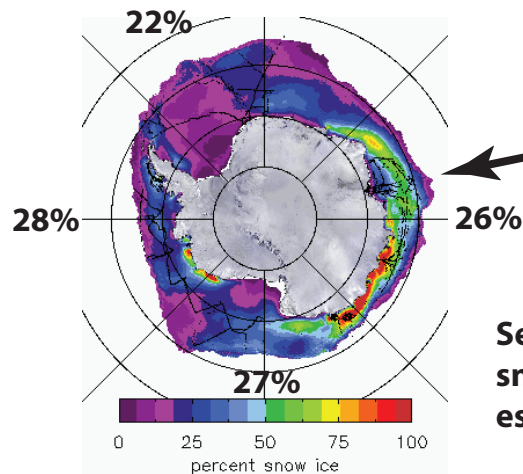
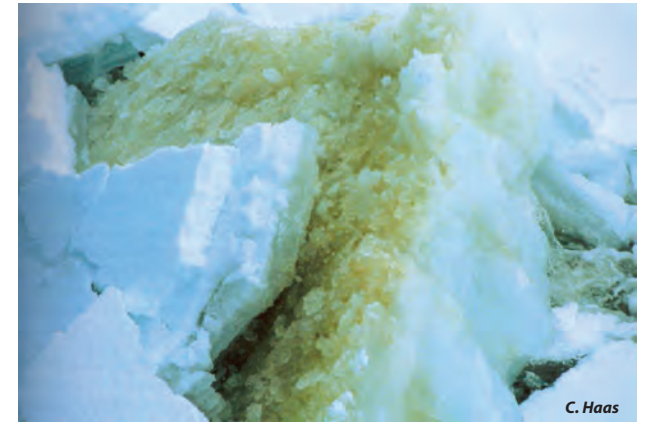
***fluid transport***

# fluid flow through the porous microstructure of sea ice governs key processes in polar climate and ecosystems

*evolution of Arctic melt ponds and sea ice albedo*



*nutrient flux for algal communities*



T. Maksym and T. Markus, 2008

*Antarctic surface flooding  
and snow-ice formation*

September  
snow-ice  
estimates

- *evolution of salinity profiles*
- *ocean-ice-air exchanges of heat, CO<sub>2</sub>*



# sea ice ecosystem



sea ice algae  
support life in the polar oceans

fluid permeability  $k$  of a porous medium

porous  
concrete



how much water  
gets through the  
sample per unit  
time?

## ***HOMOGENIZATION***

*mathematics for analyzing effective behavior of heterogeneous systems*



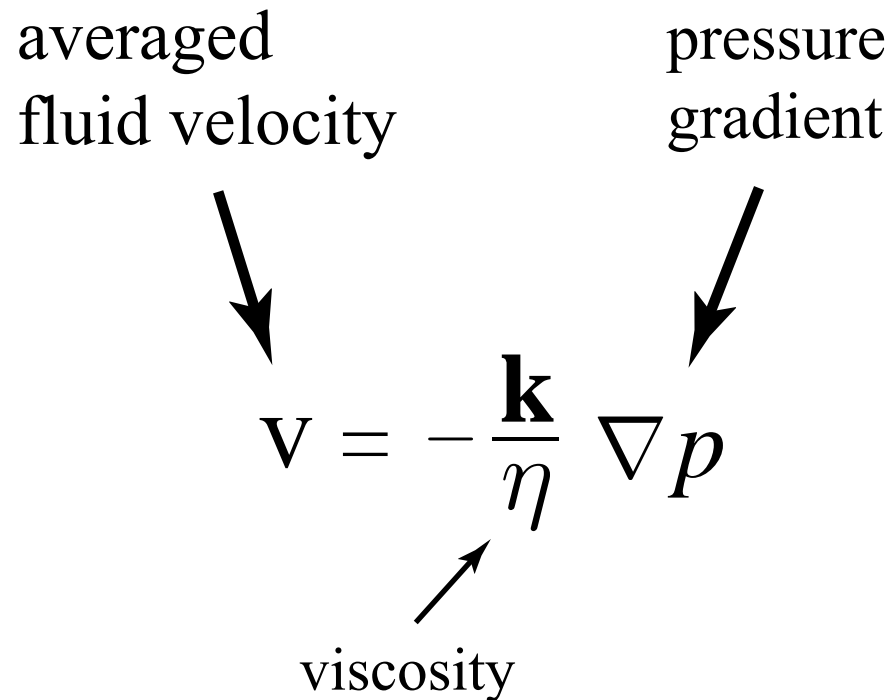
*Darcy's Law* for slow viscous flow in a porous medium

averaged  
fluid velocity

pressure  
gradient

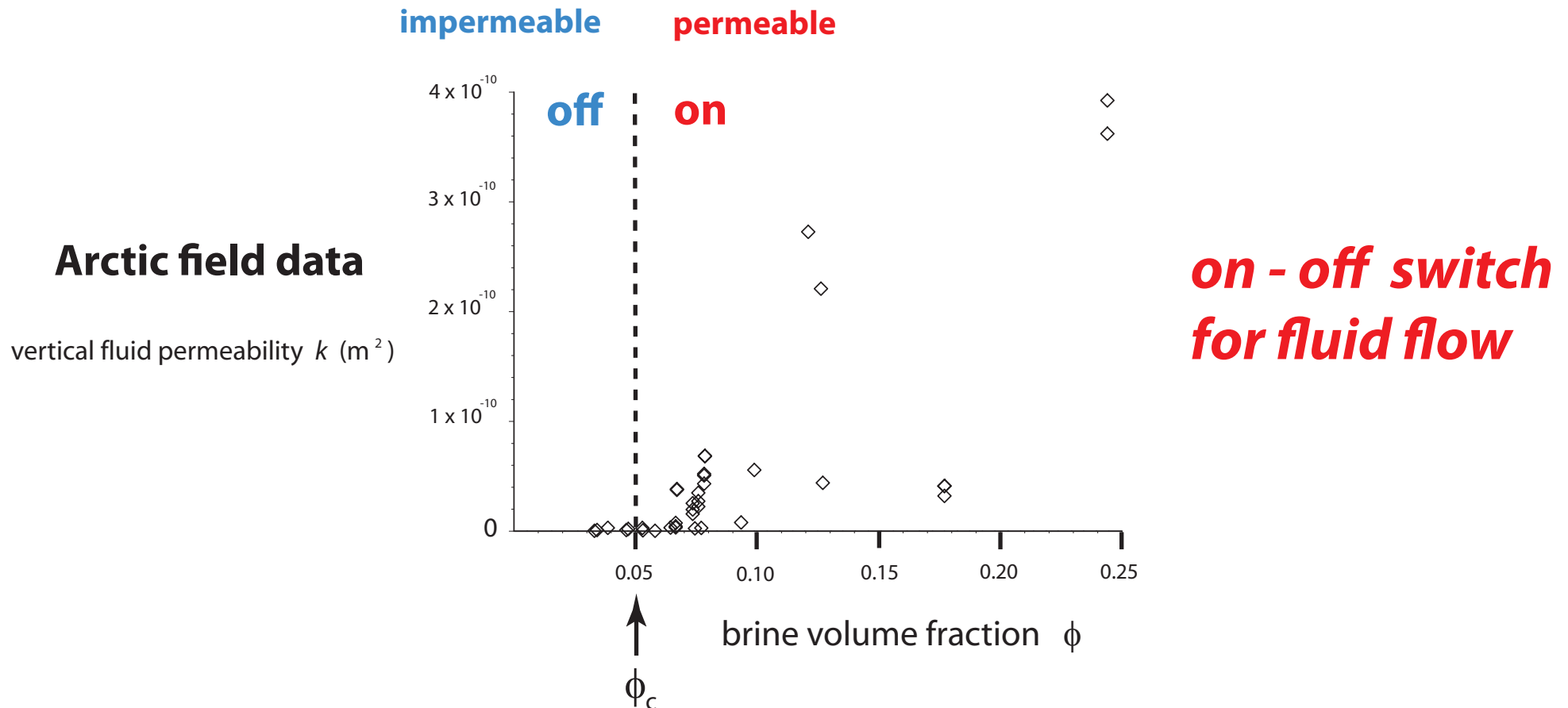
$$\mathbf{v} = -\frac{\mathbf{k}}{\eta} \nabla p$$

viscosity

The diagram shows the equation  $\mathbf{v} = -\frac{\mathbf{k}}{\eta} \nabla p$  centered on the slide. Three labels with arrows point to parts of the equation: 'averaged fluid velocity' points to  $\mathbf{v}$ , 'pressure gradient' points to  $\nabla p$ , and 'viscosity' points to  $\eta$ .

$\mathbf{k}$  = fluid permeability tensor

# Critical behavior of fluid transport in sea ice



critical brine volume fraction  $\phi_c \approx 5\%$   $\longleftrightarrow$   $T_c \approx -5^\circ \text{C}$ ,  $S \approx 5$  ppt

## RULE OF FIVES

Golden, Ackley, Lytle *Science* 1998

Golden, Eicken, Heaton, Miner, Pringle, Zhu, *Geophys. Res. Lett.* 2007

Pringle, Miner, Eicken, Golden *J. Geophys. Res.* 2009





# sea ice algal communities

D. Thomas 2004

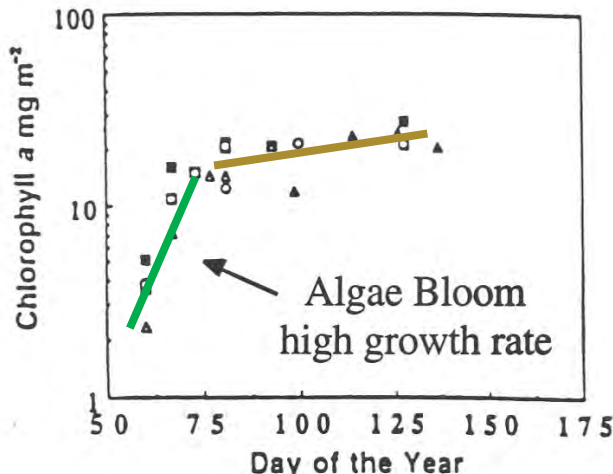
nutrient replenishment  
controlled by ice permeability

biological activity turns on  
or off according to  
*rule of fives*

*Golden, Ackley, Lytle      Science 1998*

*Fritsen, Lytle, Ackley, Sullivan      Science 1994*

## critical behavior of microbial activity



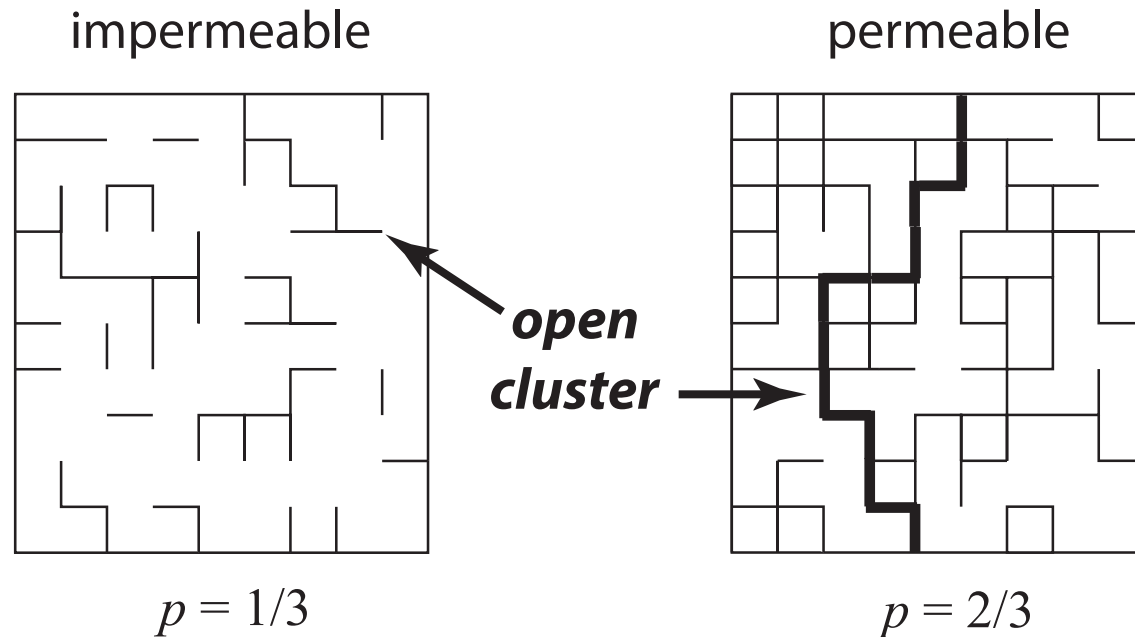
Convection-fueled algae bloom  
Ice Station Weddell

***Why is the rule of fives true?***



# percolation theory

## *probabilistic theory of connectedness*



bond  $\longrightarrow$  *open* with probability  $p$   
*closed* with probability  $1-p$

## percolation threshold

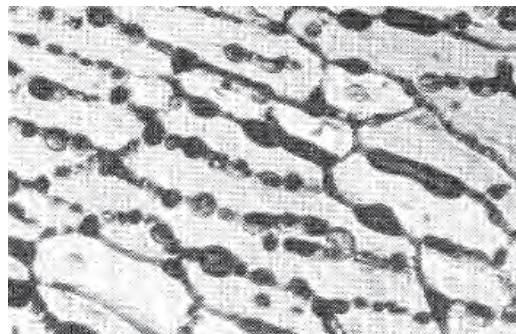
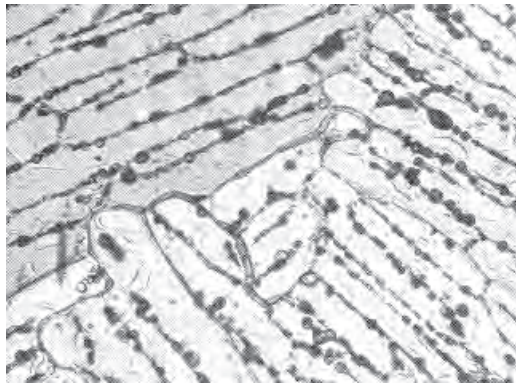
$$p_c = 1/2 \quad \text{for } d = 2$$

smallest  $p$  for which there is an infinite open cluster

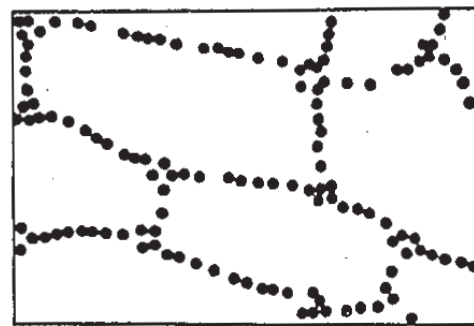
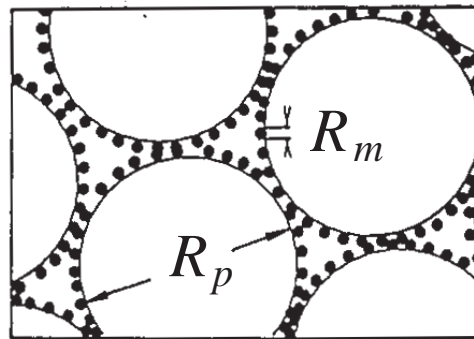
*Continuum* percolation model for **stealthy** materials applied to sea ice microstructure explains **Rule of Fives** and Antarctic data on **ice production** and **algal growth**

$$\phi_c \approx 5 \%$$

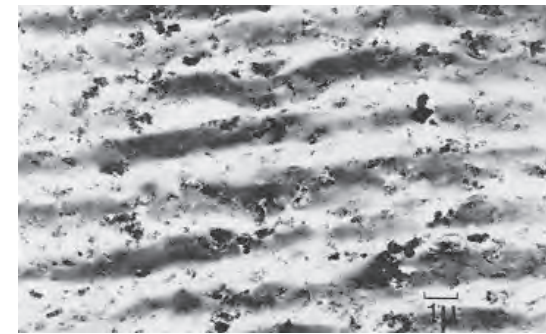
Golden, Ackley, Lytle, *Science*, 1998



sea ice



compressed  
powder



radar absorbing  
composite

**sea ice is radar absorbing**





***rigorous bounds  
percolation theory  
hierarchical model  
network model***

***field data***

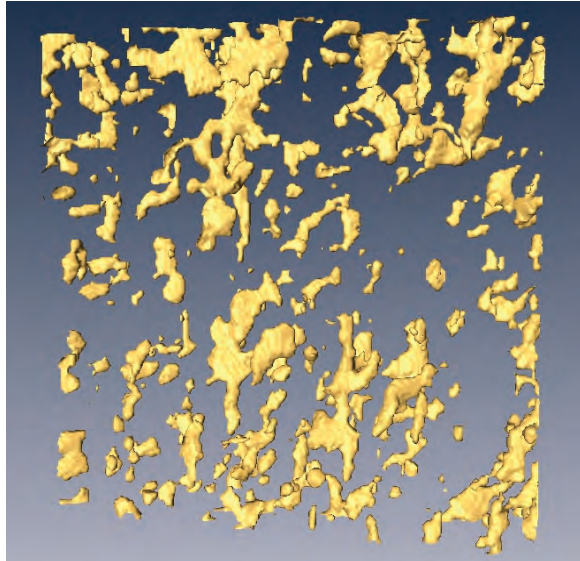
**X-ray tomography for  
brine inclusions**

***unprecedented look  
at thermal evolution  
of brine phase and  
its connectivity***

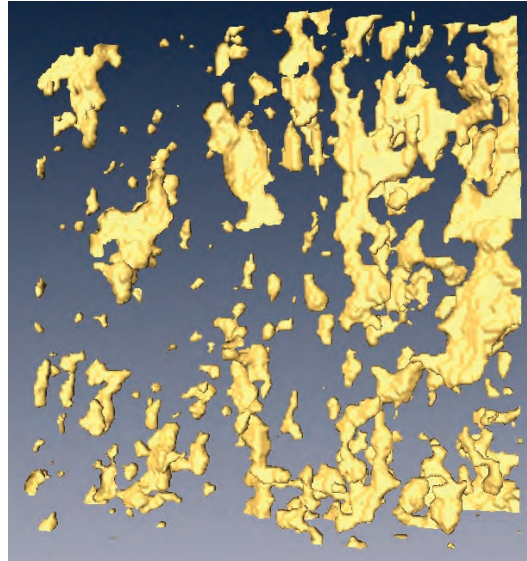
micro-scale  
controls  
macro-scale  
processes

# brine connectivity (over cm scale)

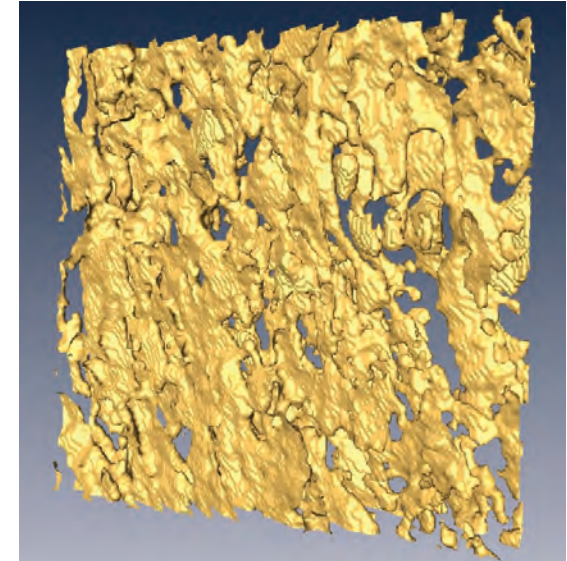
8 x 8 x 2 mm



-15 °C,  $\phi = 0.033$



-6 °C,  $\phi = 0.075$



-3 °C,  $\phi = 0.143$

## X-ray tomography confirms percolation threshold

3-D images  
pores and throats



3-D graph  
nodes and edges

***analyze graph connectivity as function of temperature and sample size***

- ***use finite size scaling techniques to confirm rule of fives***
- ***order parameter data from a natural material***

# lattice and continuum percolation theories yield:

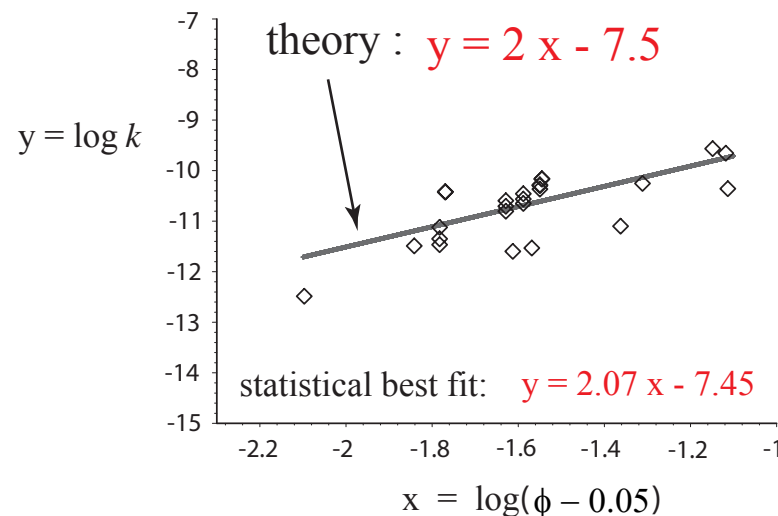
$$k(\phi) = k_0 (\phi - 0.05)^2$$

critical  
exponent

$$k_0 = 3 \times 10^{-8} \text{ m}^2$$

*t*

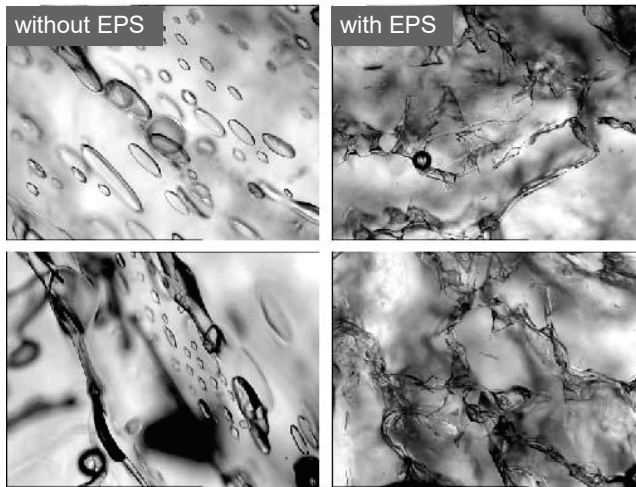
- exponent is **UNIVERSAL** lattice value  $t \approx 2.0$
- **sedimentary rocks** like sandstones also exhibit universality
- **critical path analysis** -- developed for electronic hopping conduction -- yields scaling factor  $k_0$



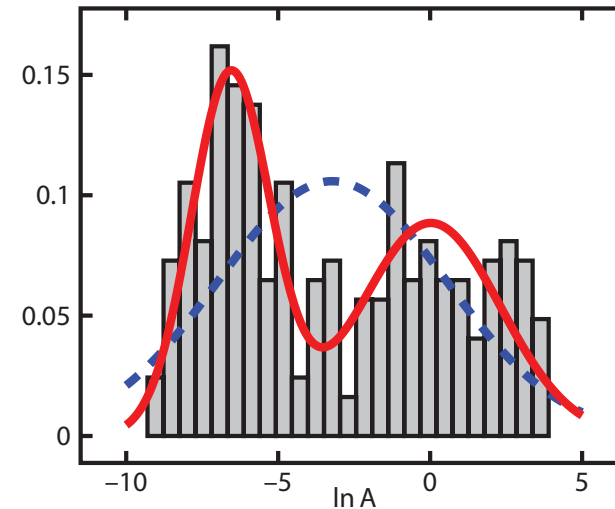


Sea ice algae secrete extracellular polymeric substances (EPS).

## How does EPS affect fluid transport?



Krembs, Eicken, Deming, PNAS 2011

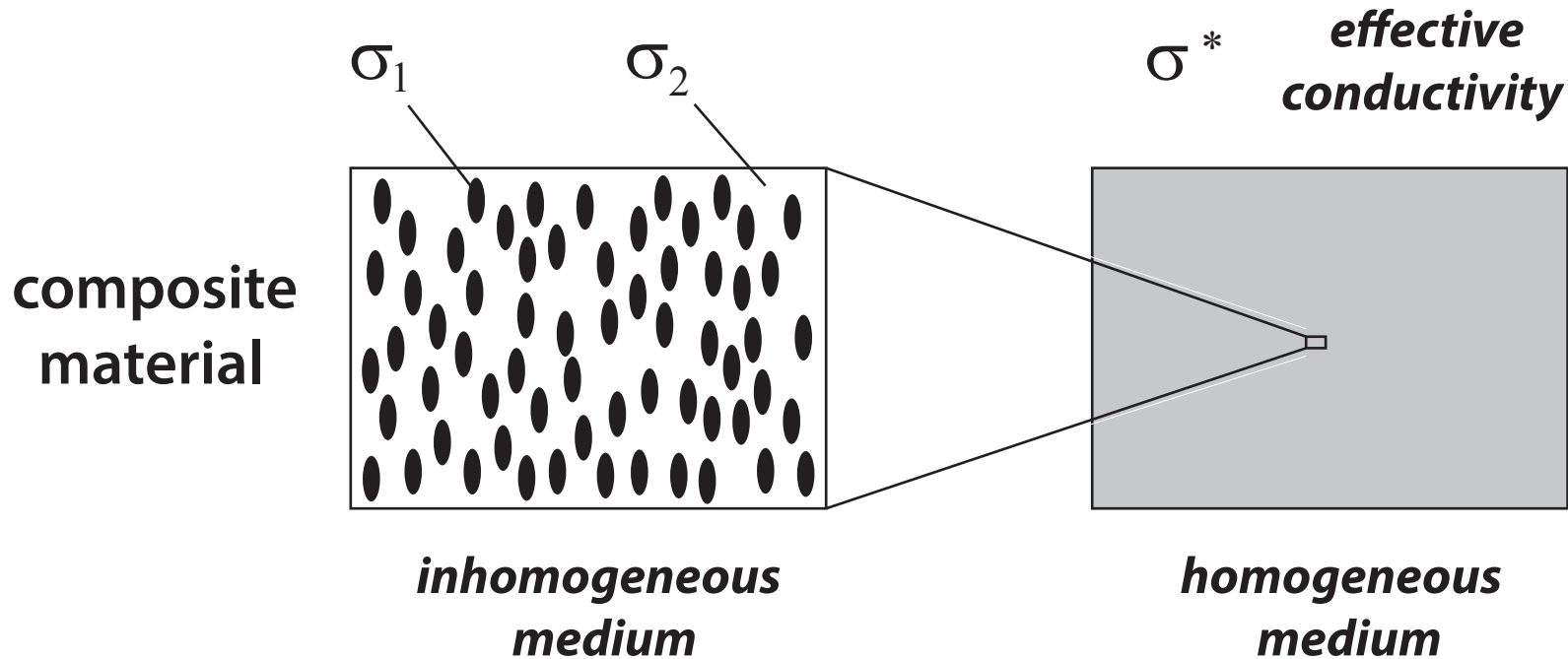


- **Bimodal** lognormal distribution for brine inclusions
- Develop new random pipe network with bimodal distribution; Update numerical methods to handle larger variances in sizes.
- Results predict observed drop in fluid permeability  $k$ .
- Rigorous bound on  $k$  for bimodal distribution of pore sizes

*Steffen, Epshteyn, Zhu, Bowler, Deming, Golden 2017*

**How does the biology affect the physics?**

# HOMOGENIZATION



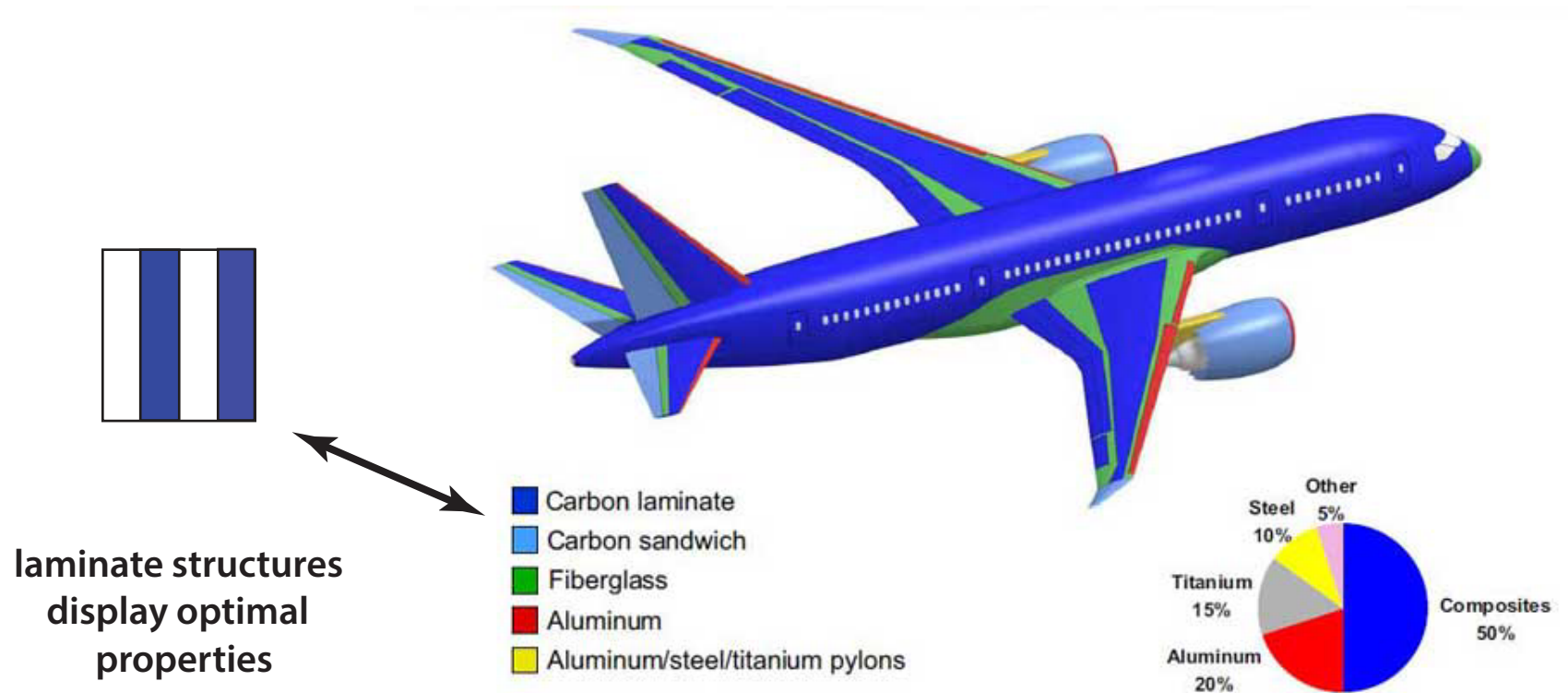
**find the homogeneous medium which  
behaves macroscopically the same as  
the inhomogeneous medium**

*Maxwell 1873 : effective conductivity of a dilute suspension of spheres*

*Einstein 1906 : effective viscosity of a dilute suspension of rigid spheres in a fluid*

**widespread use of composites in late 20th century due in large part  
to advances in mathematically predicting their effective properties**

# Composite materials in the Boeing 787 Dreamliner



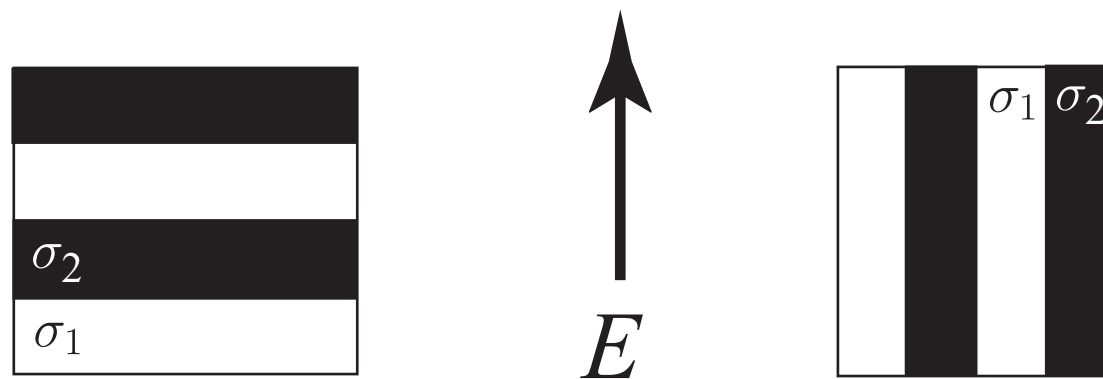


# arithmetic and harmonic mean bounds on transport properties

effective electrical conductivity  $\sigma^*$  for two phase composite of  $\sigma_1$  and  $\sigma_2$

*optimal bounds* on  $\sigma^*$  for known volume fractions  $p_1$  and  $p_2$  :

$$\frac{1}{\frac{p_1}{\sigma_1} + \frac{p_2}{\sigma_2}} \leq \sigma^* \leq p_1\sigma_1 + p_2\sigma_2$$

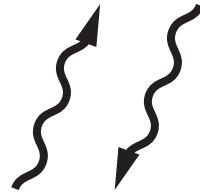
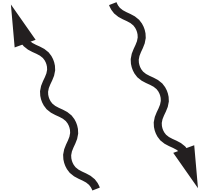


applied electric field

*optimal designs are laminates*

Wiener 1912, ....

# Remote sensing of sea ice



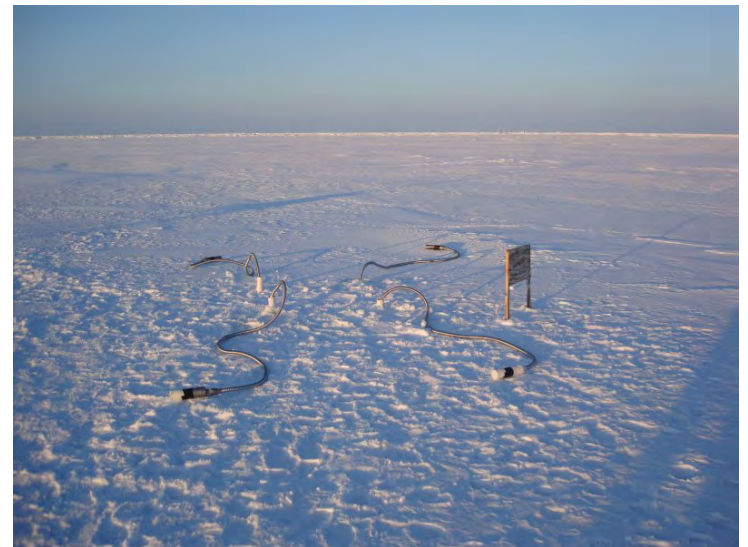
*sea ice thickness*  
*ice concentration*

## **INVERSE PROBLEM**

Recover sea ice  
properties from  
electromagnetic  
(EM) data

$$\epsilon^*$$

effective complex permittivity  
(dielectric constant, conductivity)

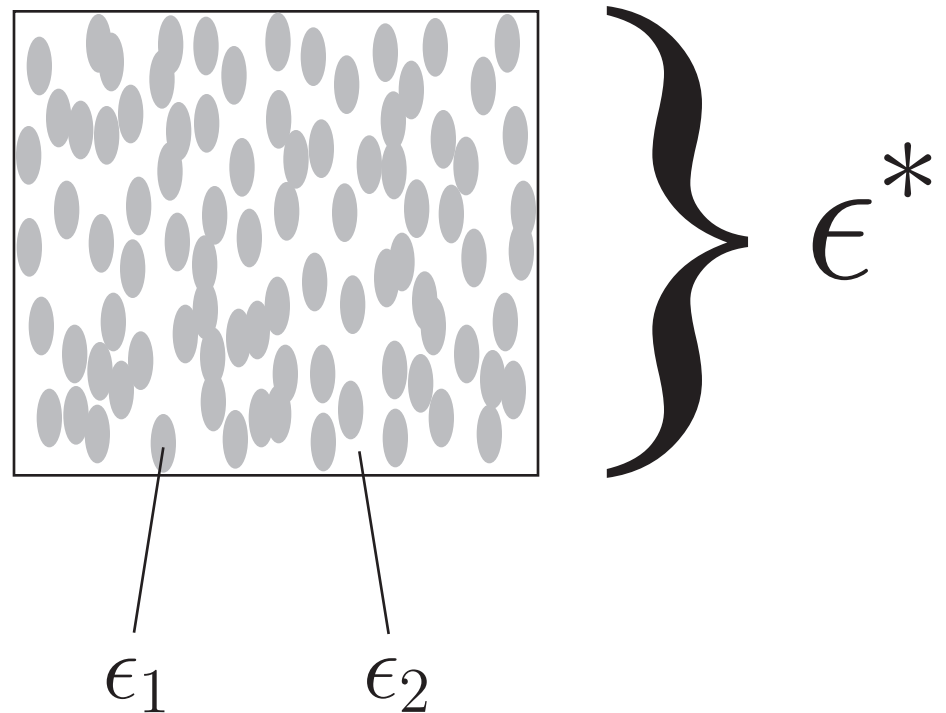


*brine volume fraction*  
*brine inclusion connectivity*

Effective complex permittivity of a two phase composite  
in the quasistatic (long wavelength) limit

**What are the effective propagation characteristics  
of an EM wave (radar, microwaves) in the medium?**

***HOMOGENIZATION***



$p_1, p_2$  = volume fractions of brine and ice



# Theory of Effective Electromagnetic Behavior of Composites

## analytic continuation method

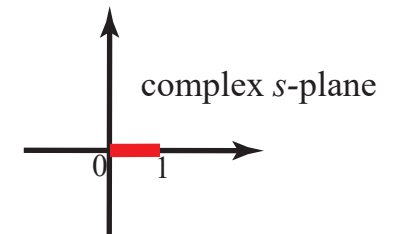
**Forward Homogenization** Bergman (1978), Milton (1979), Golden and Papanicolaou (1983)  
*Theory of Composites*, Milton (2002)

**composite geometry**  
 (spectral measure  $\mu$ )  $\longrightarrow \epsilon^*$

## Stieltjes integral representation

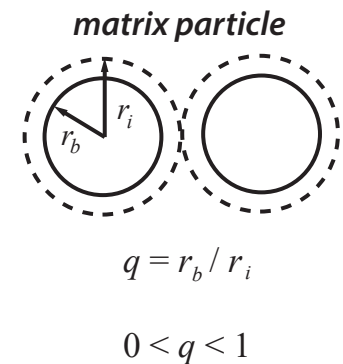
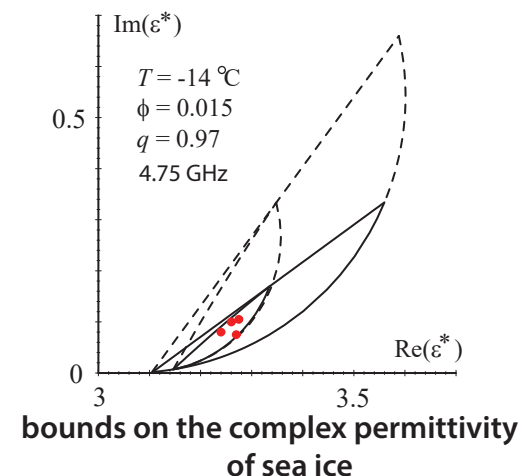
$$F(s) = 1 - \frac{\epsilon^*}{\epsilon_2} = \int_0^1 \frac{d\mu(z)}{s - z}$$

$$s = \frac{1}{1 - \epsilon_1 / \epsilon_2}$$



- $\mu$  /
- spectral measure of self adjoint operator  $\chi \Gamma \chi$
  - mass =  $p_1$
  - higher moments depend on  $n$ -point correlations

Golden and Papanicolaou 1983

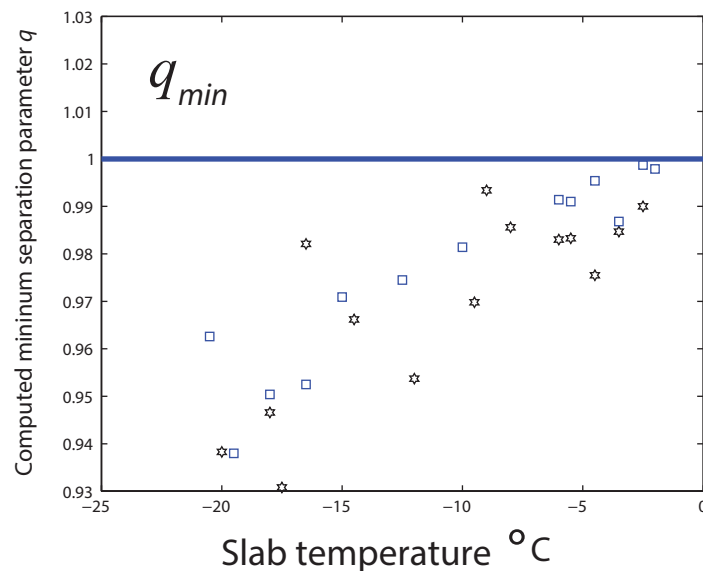


**Golden 1995, 1997**

# **Inverse Homogenization** Cherkaev and Golden (1998), Day and Thorpe (1999), Cherkaev (2001) McPhedran, McKenzie, Milton (1982), *Theory of Composites*, Milton (2002)



recover brine volume fraction, brine connectivity, etc.



**Orum, Cherkaev, Golden**  
*Proc. Roy. Soc. A*, 2012

**inversion for brine inclusion  
separations in sea ice from  
measurements of effective  
complex permittivity  $\varepsilon^*$**

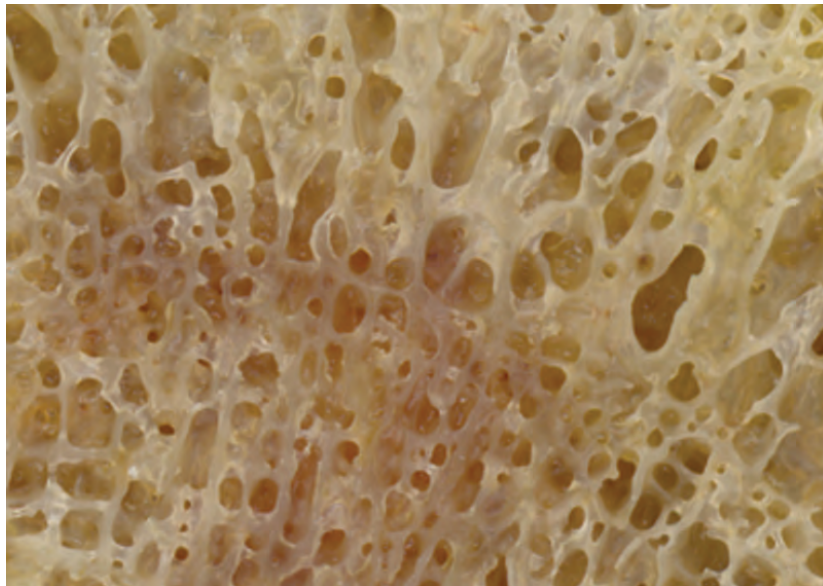
**rigorous inverse bound  
on spectral gap**

**inverse bounds and  
recovery of brine porosity**

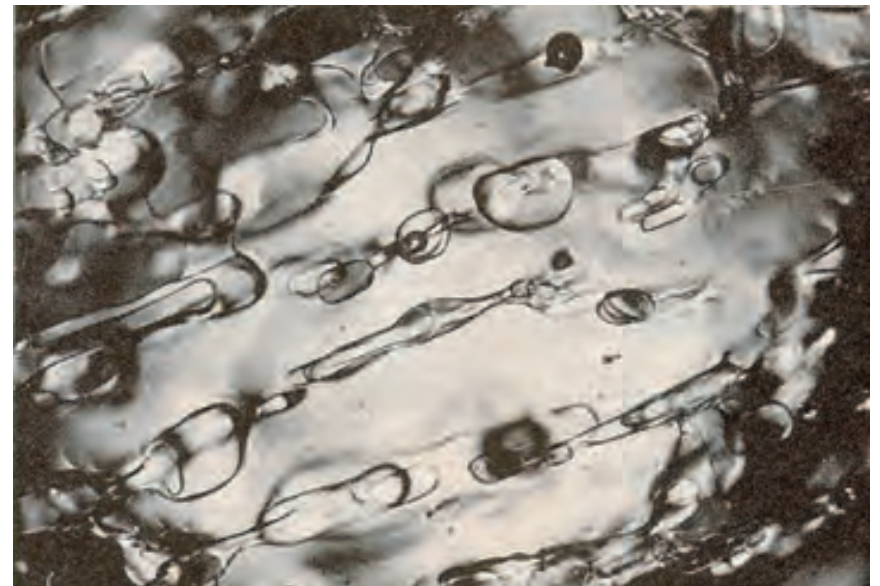
**Gully, Backstrom, Eicken, Golden**  
*Physica B*, 2007

***the math doesn't care if it's sea ice or bone!***

**HUMAN BONE**



**SEA ICE**



***apply spectral measure analysis of brine connectivity and spectral inversion to electromagnetic monitoring osteoporosis***

***Golden, Murphy, Cherkaev, J. Biomechanics 2011***



# direct calculation of spectral measure

- depends only on the composite geometry
- discretization of microstructural image gives binary network
- fundamental operator becomes a random matrix
- spectral measure computed from eigenvalues and eigenvectors

once we have the spectral measure  $\mu$   
it can be used in Stieltjes integrals for other transport coefficients:

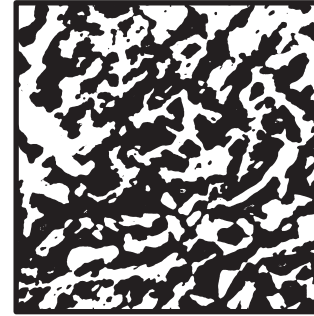
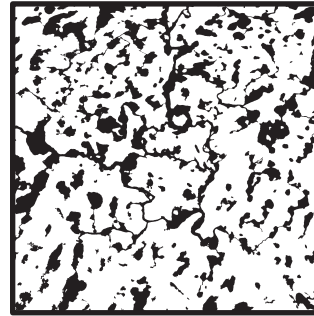
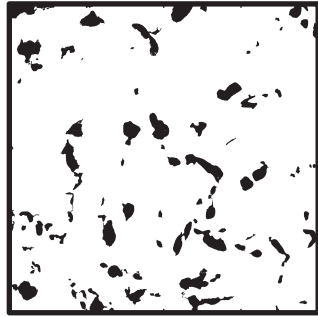
electrical and thermal conductivity, complex permittivity,  
magnetic permeability, effective diffusion

→ *cross-property relations and inversions; spectral statistics*

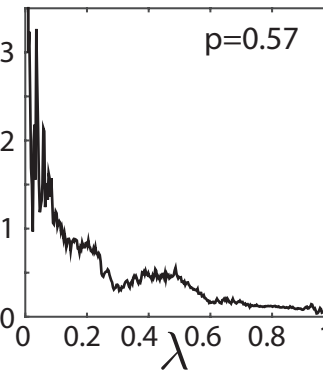
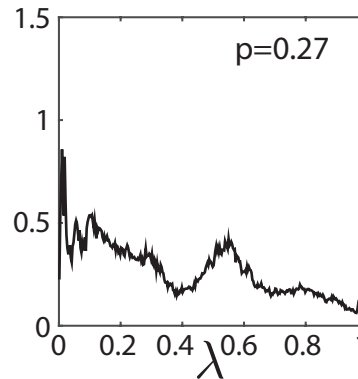
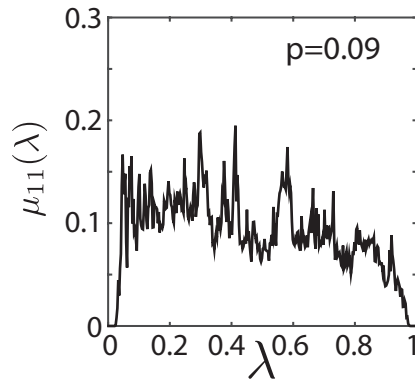
earlier studies of spectral measures

Day and Thorpe 1996  
Helsing, McPhedran, Milton 2011

# Spectral computations for Arctic melt ponds

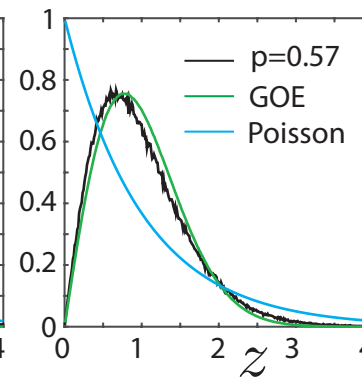
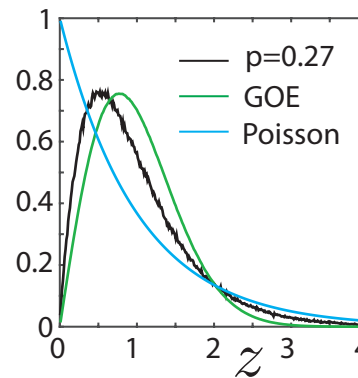
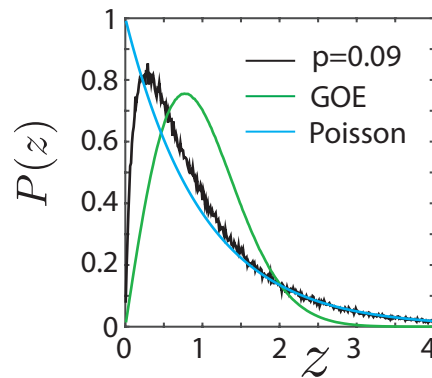


spectral  
measures



Ben Murphy  
Elena Cherkaev  
Ken Golden  
2016

eigenvalue  
spacing  
distributions



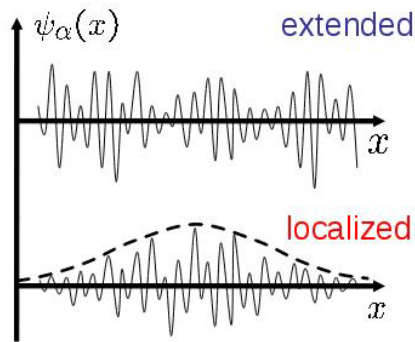
uncorrelated



level repulsion

**TRANSITION**

*eigenvalue statistics  
for transport tend  
toward the  
**UNIVERSAL**  
**Wigner-Dyson**  
**distribution**  
as the “conducting”  
phase percolates*



## metal / insulator transition **localization**

*Anderson 1958*  
*Mott 1949*  
*Shklovshii et al 1993*  
*Evangelou 1992*

**Anderson transition in wave physics:  
quantum, optics, acoustics, water waves, ...**

**we find a surprising analog**

***Anderson transition for classical transport in composites***

*Murphy, Cherkaev, Golden Phys. Rev. Lett. 2017*

**PERCOLATION  
TRANSITION**



**transition to universal  
eigenvalue statistics (GOE)  
extended states, mobility edges**

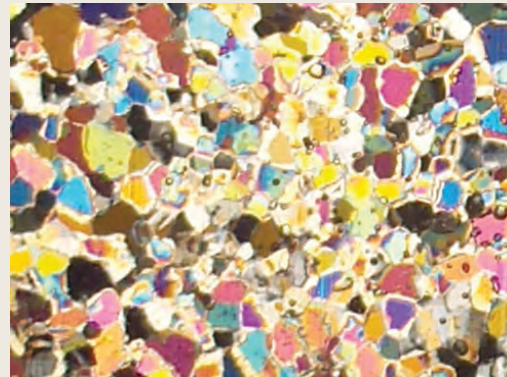
**-- but without wave interference or scattering effects ! --**



# Bounds on the complex permittivity of polycrystalline materials by analytic continuation

Adam Gully, Joyce Lin,  
Elena Cherkaev, Ken Golden

- **Stieltjes integral representation for effective complex permittivity**  
Milton (1981, 2002), Barabash and Stroud (1999), ...
- **Forward and inverse bounds**
- **Applied to sea ice using two-scale homogenization**
- **Inverse bounds give method for distinguishing ice types using remote sensing techniques**



## PROCEEDINGS A

350 YEARS  
OF SCIENTIFIC  
PUBLISHING

An invited review  
commemorating 350 years  
of scientific publishing at the  
Royal Society

A method to distinguish  
between different types  
of sea ice using remote  
sensing techniques

A computer model to  
determine how a human  
should walk so as to expend  
the least energy

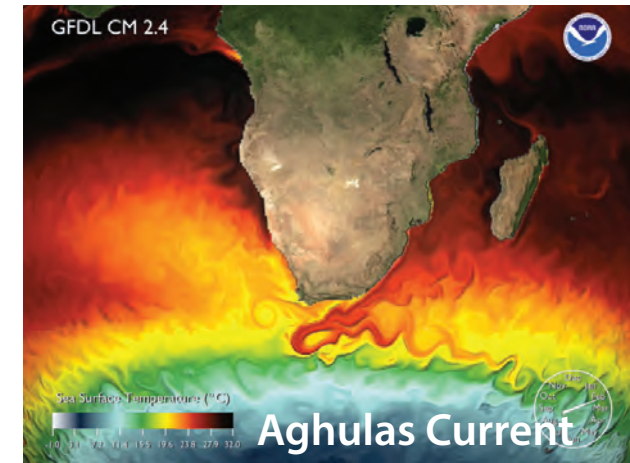
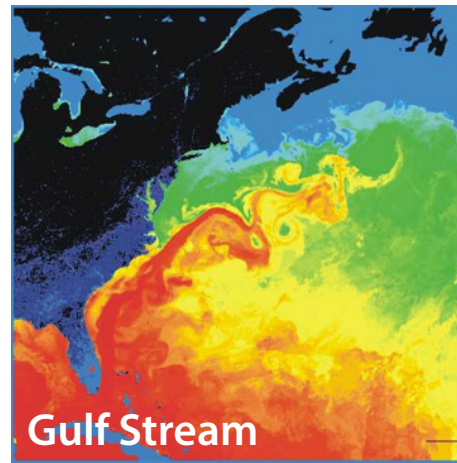




# advection enhanced diffusion

## effective diffusivity

tracers, buoys diffusing in ocean eddies  
diffusion of pollutants in atmosphere  
salt and heat transport in ocean  
heat transport in sea ice with convection



advection diffusion equation with a velocity field  $\vec{u}$

$$\frac{\partial T}{\partial t} + \vec{u} \cdot \vec{\nabla} T = \kappa_0 \Delta T$$

$$\vec{\nabla} \cdot \vec{u} = 0$$

homogenize

$$\frac{\partial \bar{T}}{\partial t} = \kappa^* \Delta \bar{T}$$

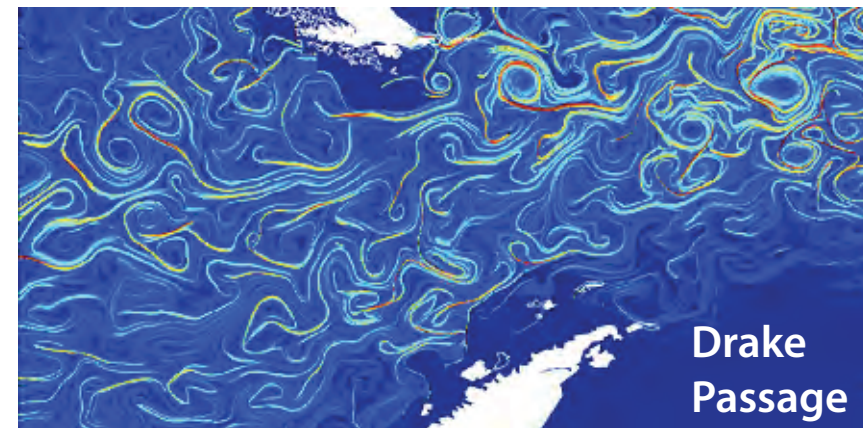
$\kappa^*$  effective diffusivity

**Stieltjes integral for  $\kappa^*$  with spectral measure**

Avellaneda and Majda, PRL 89, CMP 91

Murphy, Cherkaev, Xin, Zhu, Golden, Ann. Math. Sci. Appl. 2017

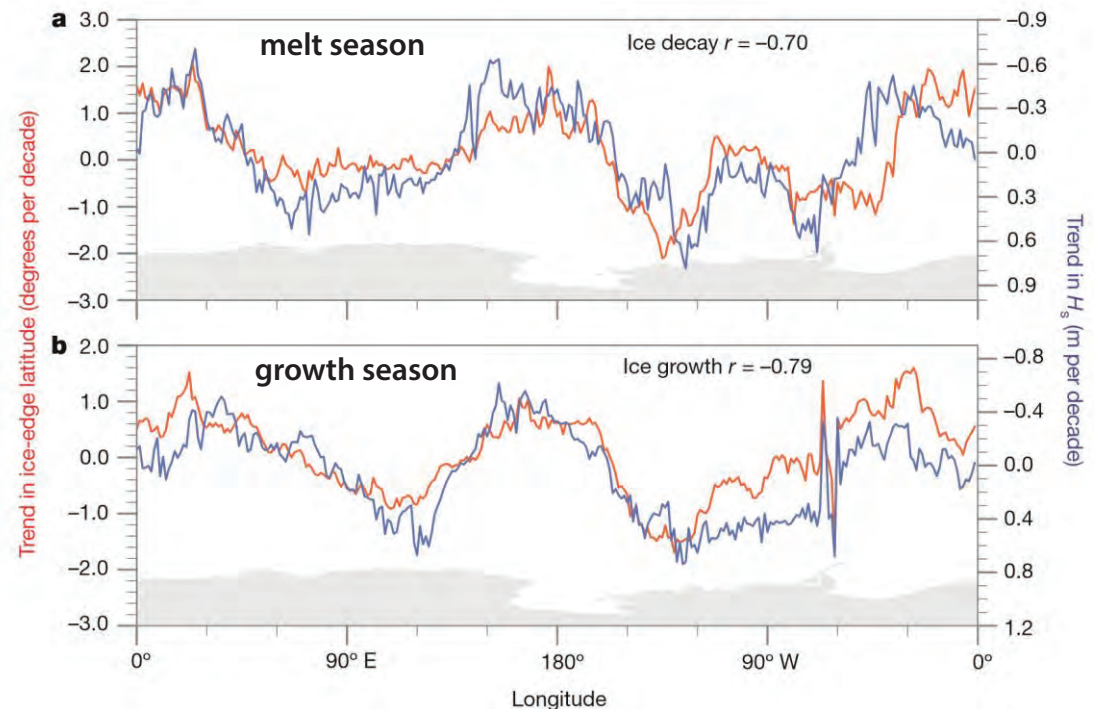
Murphy, Cherkaev, Zhu, Xin, Golden, 2017



# Storm-induced sea-ice breakup and the implications for ice extent

Kohout et al., *Nature* 2014

- during three large-wave events, significant wave heights did not decay exponentially, enabling large waves to persist deep into the pack ice.
- large waves break sea ice much farther from the ice edge than would be predicted by the commonly assumed exponential decay



*ice extent compared with significant wave height*

**Waves have strong influence on both the floe size distribution and ice extent.**



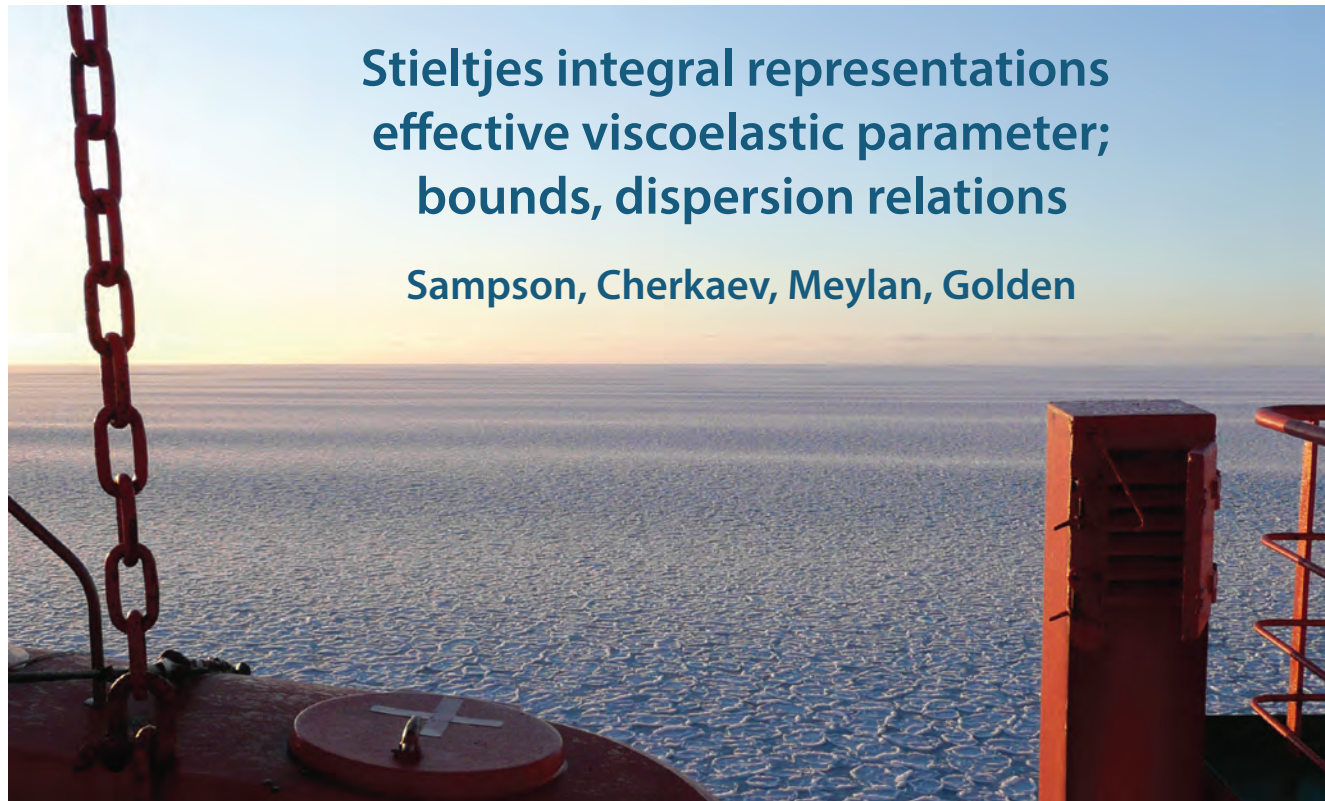
*ocean swells propagating through a vast field of pancake ice*

**HOMOGENIZATION:** long wave sees an effective medium, not individual floes





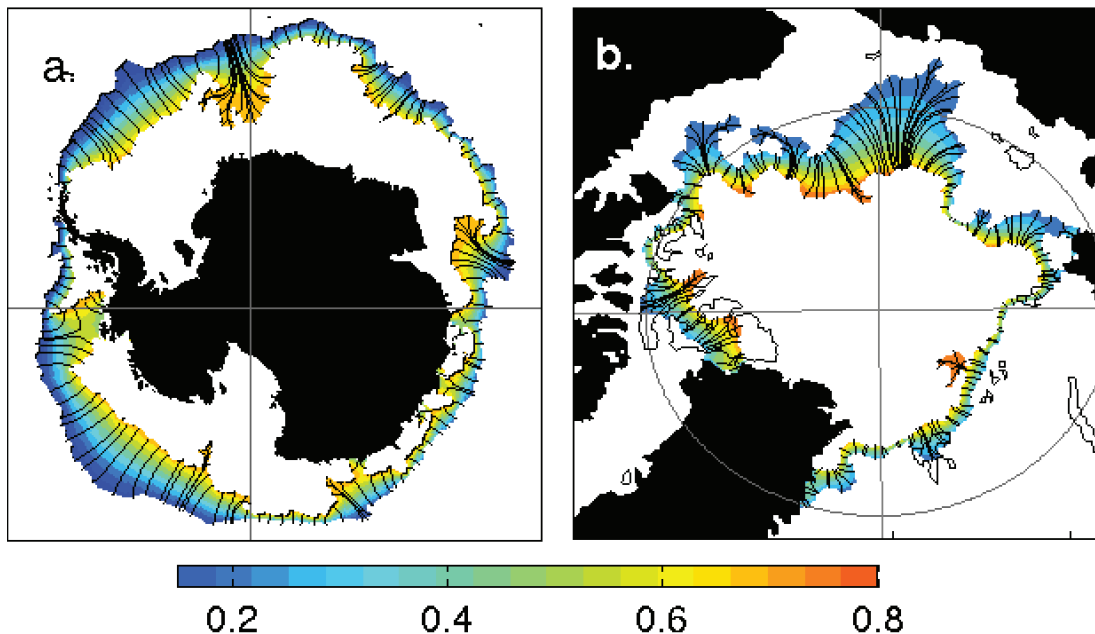
# wave propagation in the marginal ice zone



# Marginal Ice Zone

## MIZ

- biologically active region
- intense ocean-sea ice-atmosphere interactions
- region of significant wave-ice interactions



### MIZ WIDTH

fundamental length scale of  
ecological and climate dynamics

Strong, *Climate Dynamics* 2012

Strong and Rigor, *GRL* 2013

transitional region between  
dense interior pack ( $c > 80\%$ )  
sparse outer fringes ( $c < 15\%$ )

**How to objectively  
measure the “width”  
of this complex,  
non-convex region?**



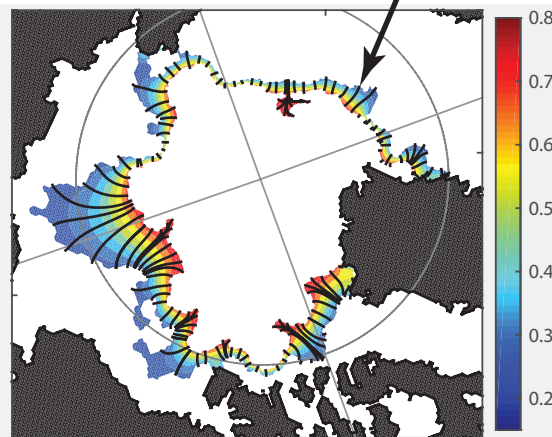
# Objective method for measuring MIZ width motivated by medical imaging and diagnostics

Strong, *Climate Dynamics* 2012

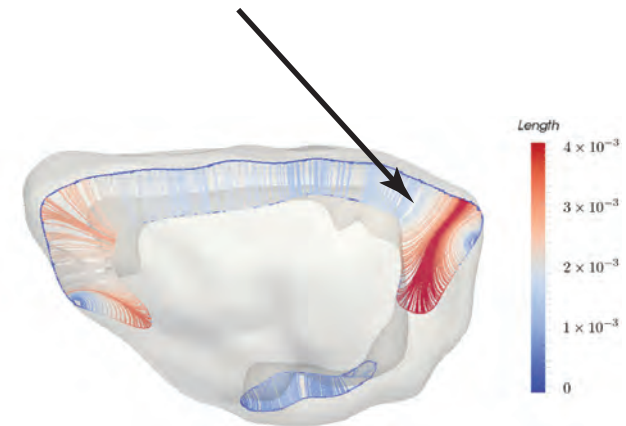
Strong and Rigor, *GRL* 2013

**“average” lengths of streamlines**

**streamlines of a solution  
to Laplace’s equation**



**Arctic Marginal Ice Zone**



**crosssection of the  
cerebral cortex of a rodent brain**

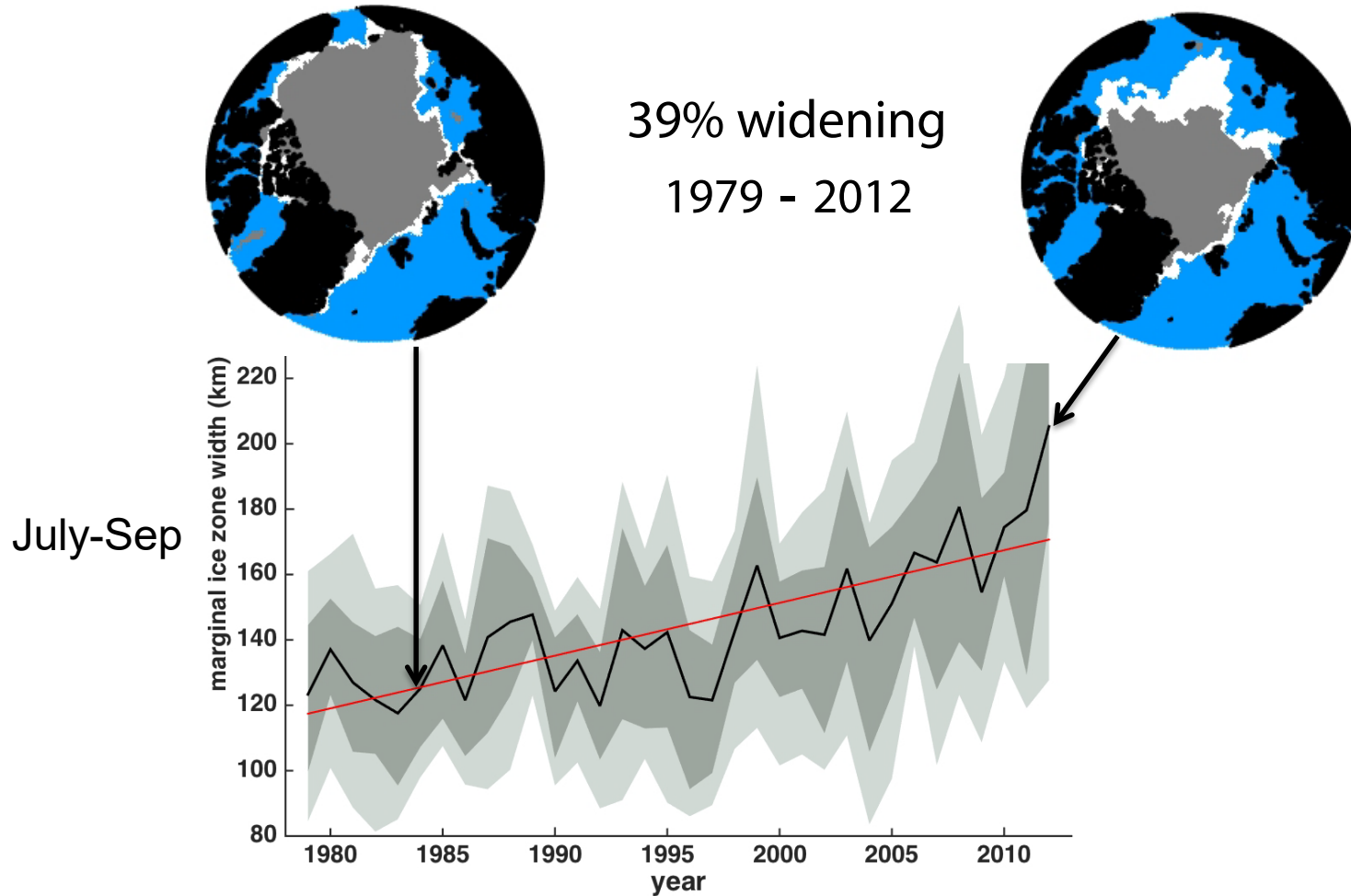
## ***analysis of different MIZ WIDTH definitions***

Strong, Foster, Cherkaev, Eisenman, Golden  
*J. Atmos. Oceanic Tech.* 2017

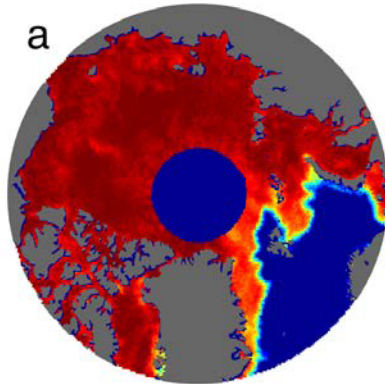
Strong and Golden

*Society for Industrial and Applied Mathematics News*, April 2017

# MIZ width increasing

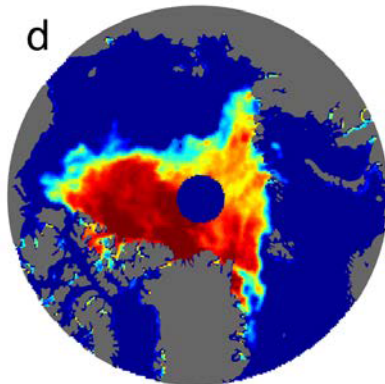


# Filling the polar data gap



Gap radius: 611 km  
06 January 1985

Examples of  
“polar data gap”  
where orbiting  
satellites do not  
measure sea ice  
concentration



Gap radius: 311 km  
30 August 2007

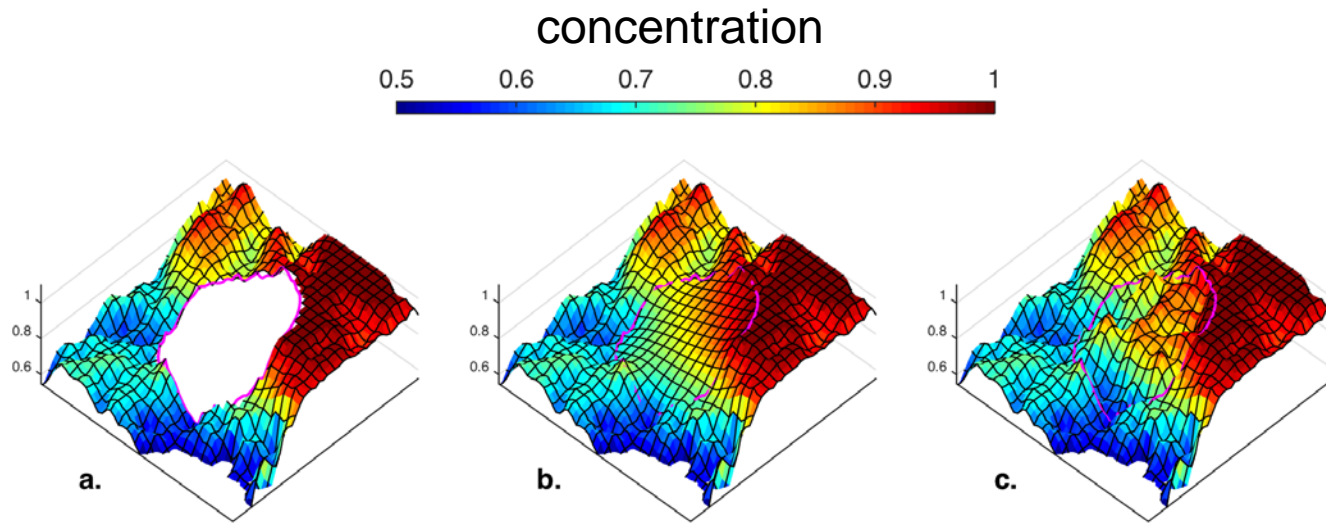
gap region conventionally  
assumed ice-covered for  
sea ice extent calculations



***given recent losses this assumption  
may no longer be valid***



# Filling the polar data gap



polar data gap  
30 August 2007

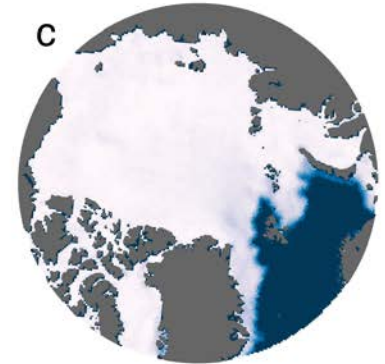
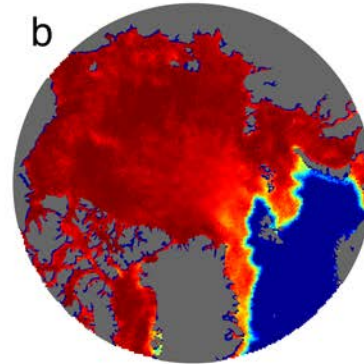
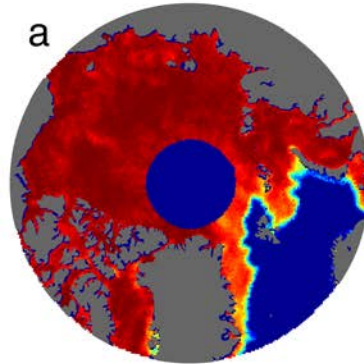
$$\nabla^2 \psi = 0$$

$$f(\lambda, \phi) = \psi(\lambda, \phi) + \Omega(\lambda, \phi)$$

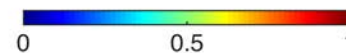
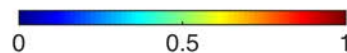
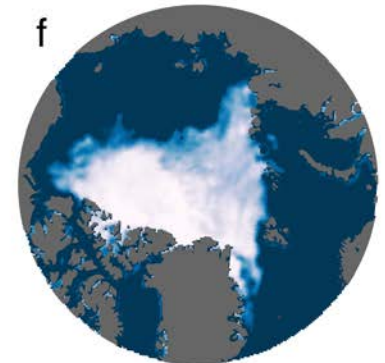
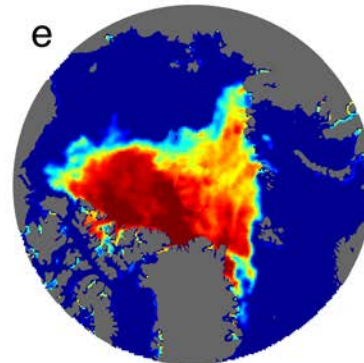
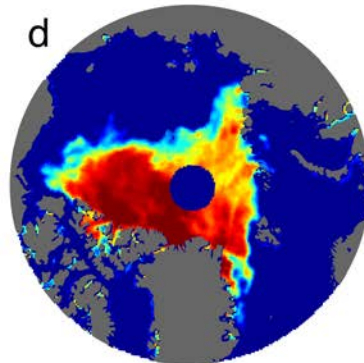
$\Omega$  simulates realistically autocorrelated deviations from  $\psi$  via convolution of random noise with a Gaussian function

# Filling the polar data gap

Gap radius: 611 km  
06 January 1985



Gap radius: 311 km  
30 August 2007



# Arctic and Antarctic field experiments

*develop electromagnetic methods  
of monitoring fluid transport and  
microstructural transitions*

extensive measurements of fluid and  
electrical transport properties of sea ice:

**2007    Antarctic    SIPEX**

**2010    Antarctic    McMurdo Sound**

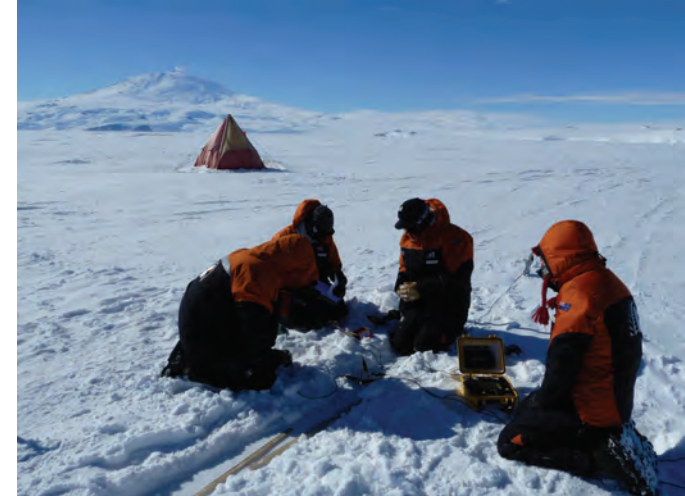
**2011    Arctic        Barrow AK**

**2012    Arctic        Barrow AK**

**2012    Antarctic    SIPEX II**

**2013    Arctic        Barrow AK**

**2014    Arctic        Chukchi Sea**





# Notices

of the American Mathematical Society

May 2009

Volume 56, Number 5

Climate Change and  
the Mathematics of  
Transport in Sea Ice

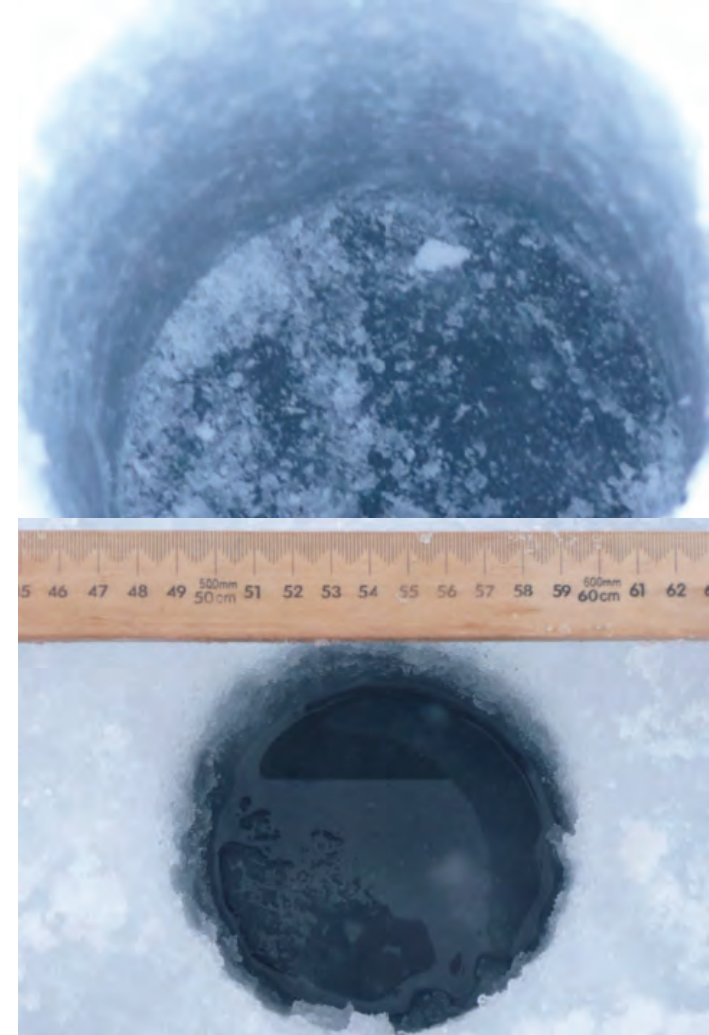
page 562

Mathematics and the  
Internet: A Source of  
Enormous Confusion  
and Great Potential

page 586

*photo by Jan Lieser*

*Real analysis in polar coordinates (see page 613)*



***measuring  
fluid permeability  
of Antarctic sea ice***

***SIPEX 2007***

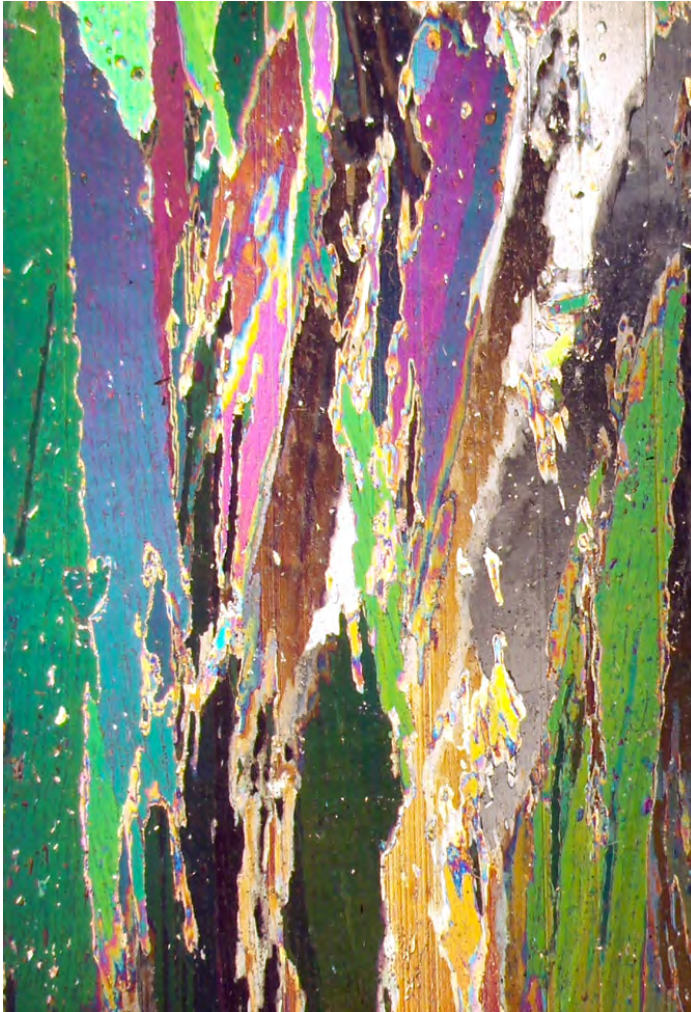


# ***higher threshold for fluid flow in Antarctic granular sea ice***

columnar

granular

**5%**



**10%**



***Golden, Sampson, Gully, Lubbers, Tison 2016***

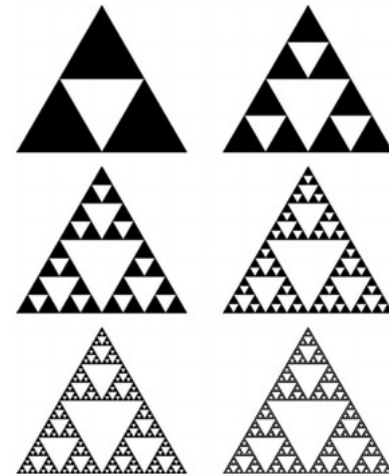


# tracers flowing through inverted sea ice blocks





# ***fractals and multiscale structure***



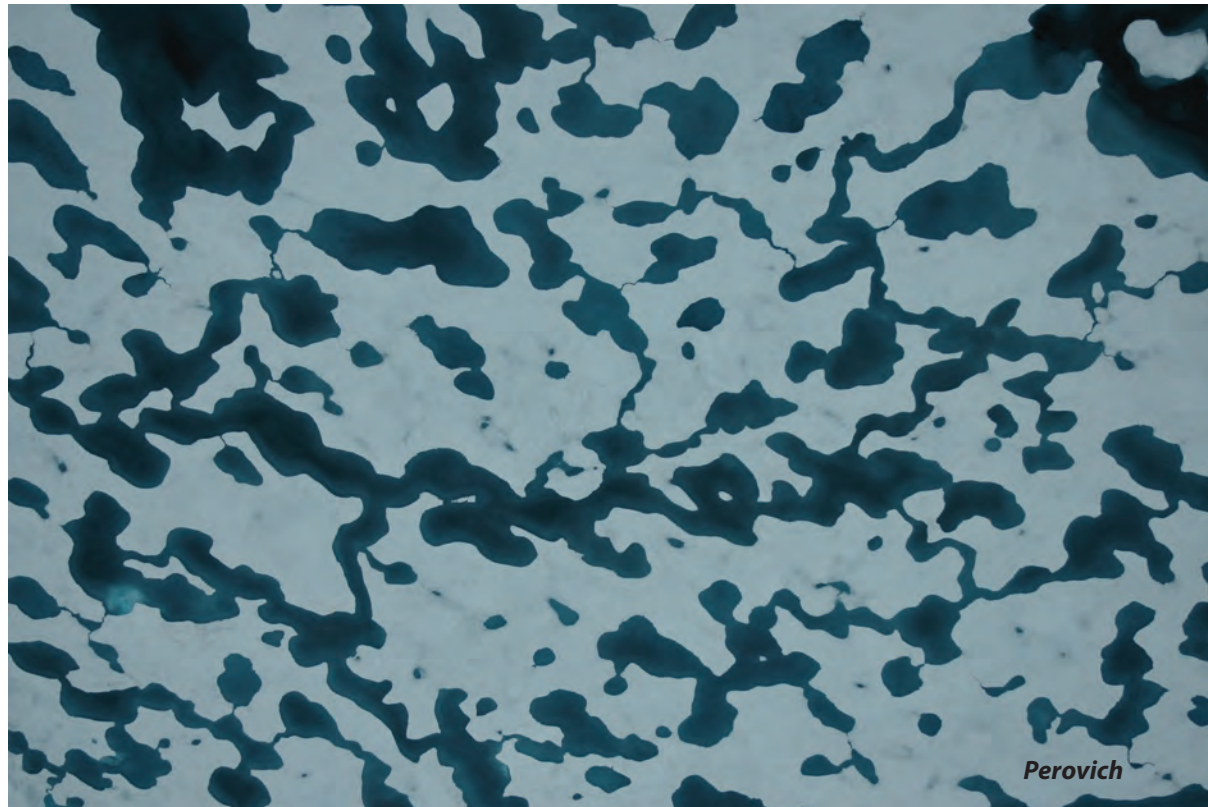
# *melt pond formation and albedo evolution:*

- *major drivers in polar climate*
- *key challenge for global climate models*

**numerical models of melt pond evolution, including topography, drainage (permeability), etc.**

Lüthje, Feltham,  
Taylor, Worster 2006  
Flocco, Feltham 2007

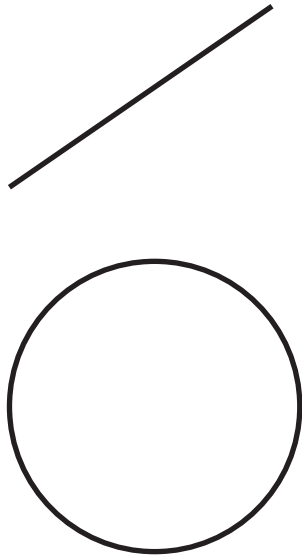
Skyllingstad, Paulson,  
Perovich 2009  
Flocco, Feltham,  
Hunke 2012



**Are there universal features of the evolution similar to phase transitions in statistical physics?**

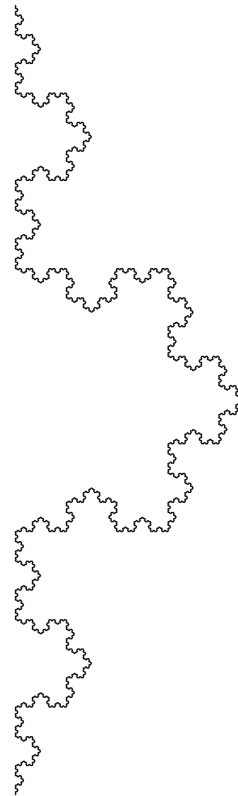
# *fractal curves in the plane*

*they wiggle so much that their dimension is  $>1$*



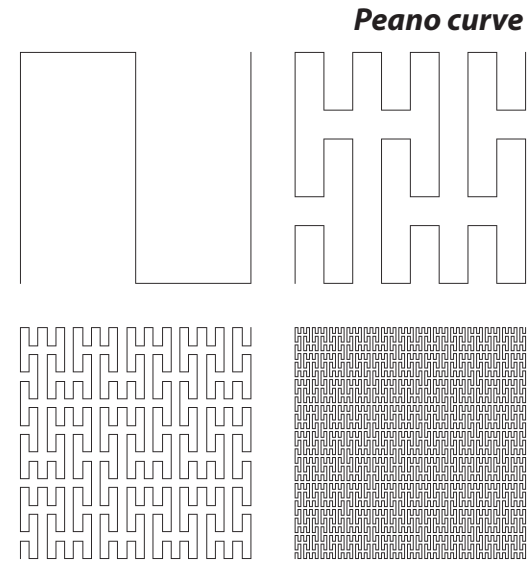
*simple curves*

$$D = 1$$



*Koch snowflake*

$$D = 1.26$$



*Peano curve*

*Brownian motion*

*space filling curves*

$$D = 2$$



# clouds exhibit fractal behavior from 1 to 1000 km

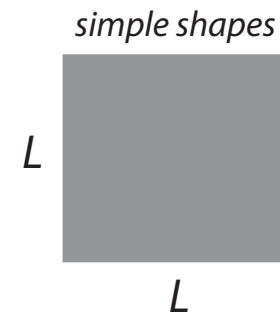
use **perimeter-area** data to find that cloud and rain boundaries are fractals

$$D \approx 1.35$$

*S. Lovejoy, Science, 1982*

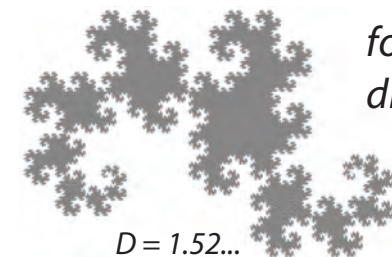


$$P \sim \sqrt{A}$$



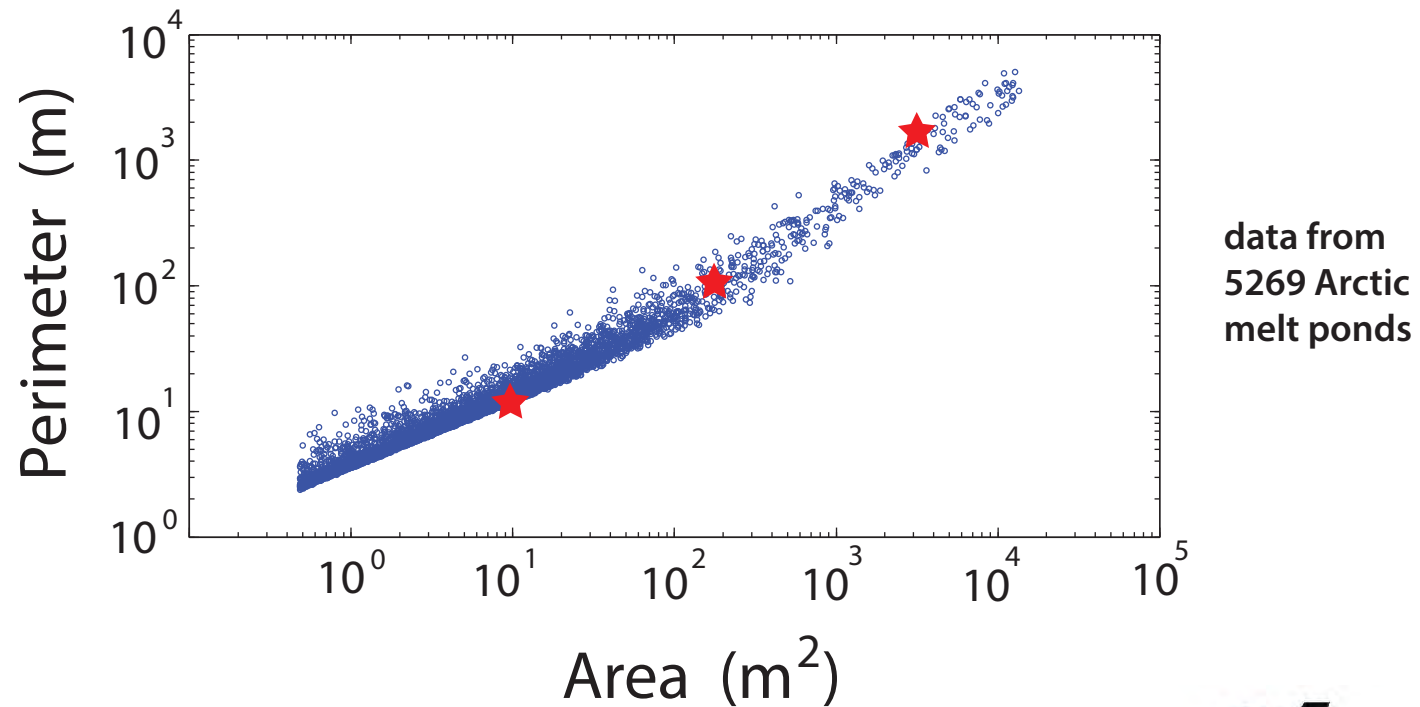
$$A = L^2$$
$$P = 4L = 4\sqrt{A}$$

$$P \sim \sqrt{A}^D$$



for fractals with dimension  $D$

Christel Hohenegger, Bacim Alali, Kyle Steffen, Don Perovich, Ken Golden



***simple pond***



~ 30 m

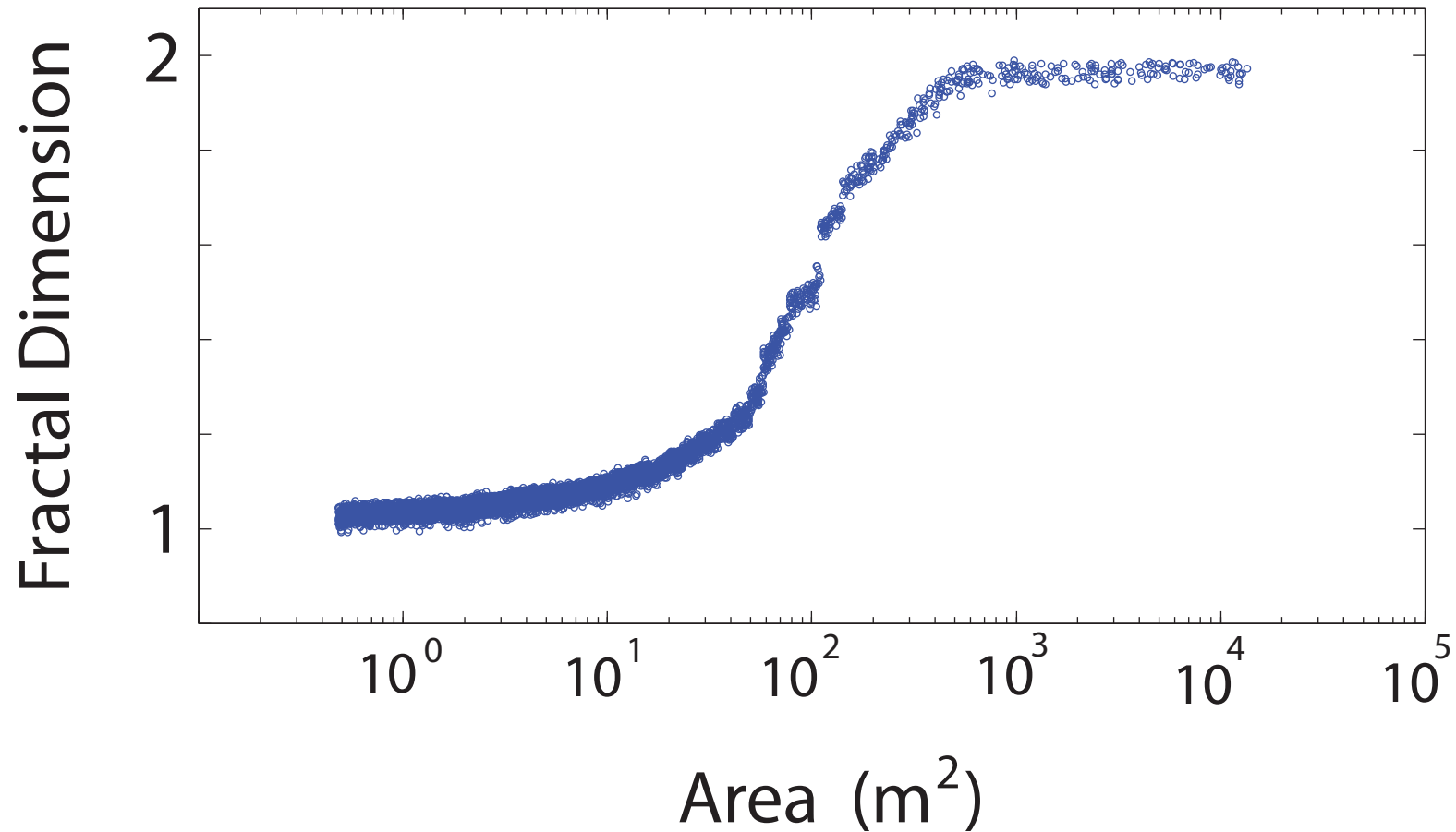
***transitional pond***



***complex pond***

## *transition in the fractal dimension*

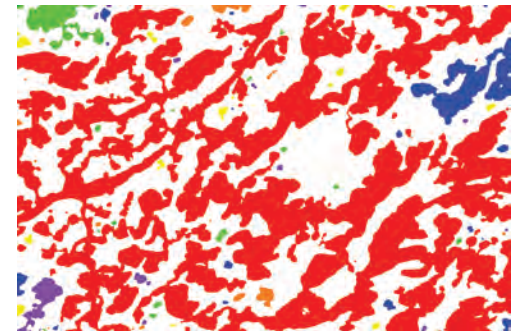
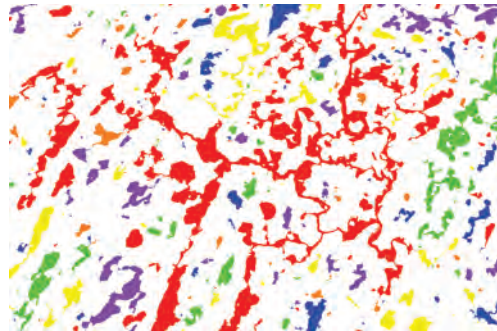
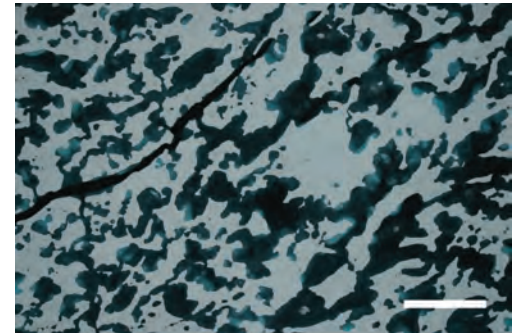
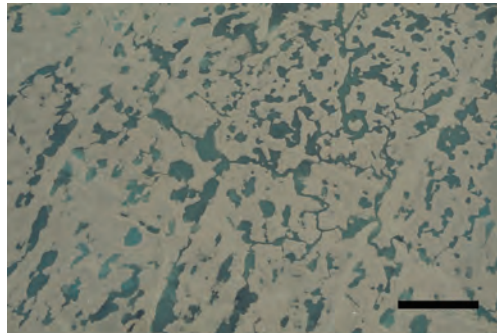
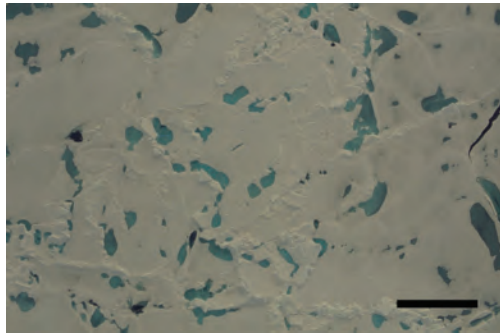
complexity grows with length scale



compute “derivative” of area - perimeter data



***small simple ponds coalesce to form  
large connected structures with complex boundaries***



**melt pond percolation**

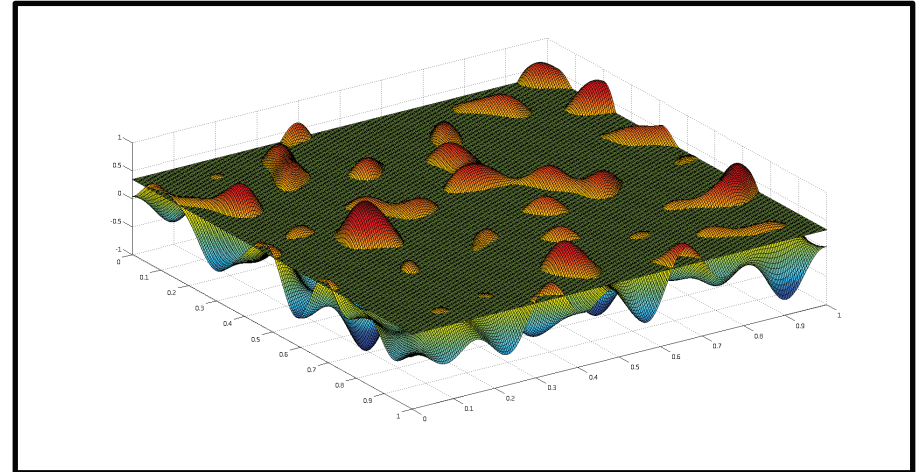
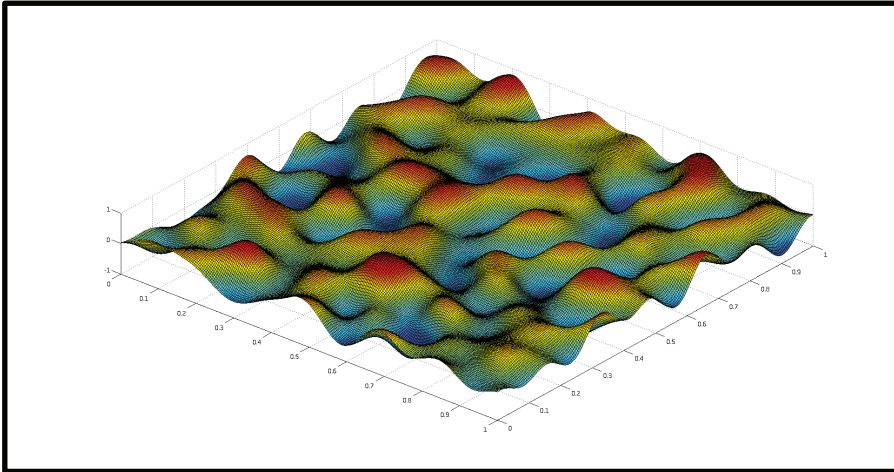
**results on percolation threshold, correlation length, cluster behavior**

*Anthony Cheng (Hillcrest HS), Dylan Webb (Skyline HS), Court Strong, Ken Golden*

# Continuum percolation model for melt pond evolution

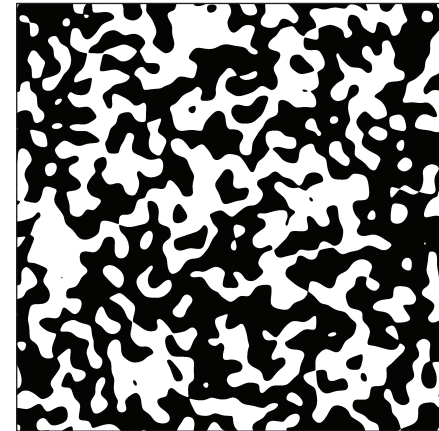
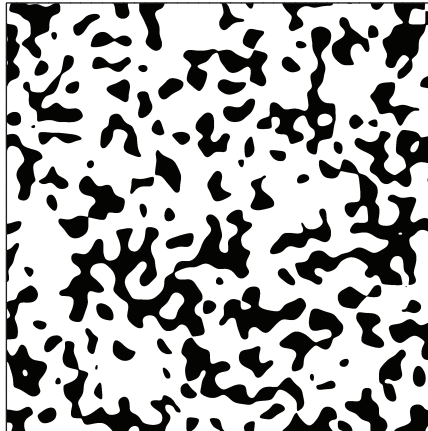
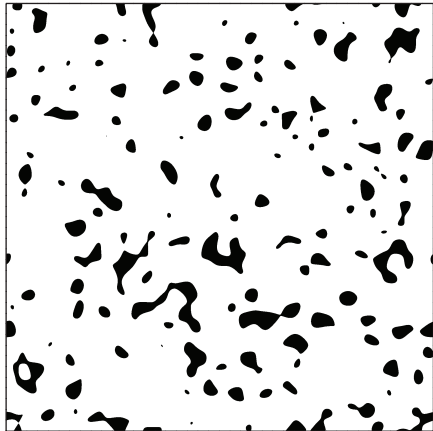
## *level sets of random surfaces*

*Brady Bowen, Court Strong, Ken Golden, J. Fractal Geometry 2017*



random Fourier series representation of surface topography

intersections of a plane with the surface define melt ponds



*electronic transport in disordered media*

*diffusion in turbulent plasmas*

*Isichenko, Rev. Mod. Phys., 1992*



**melt pond evolution depends also on large-scale “pores” in ice cover**

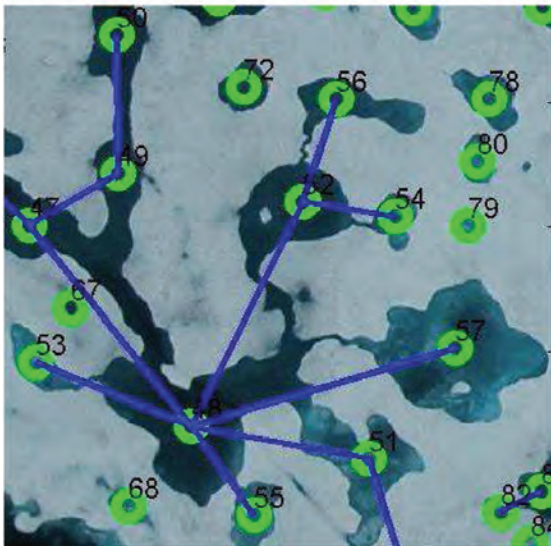
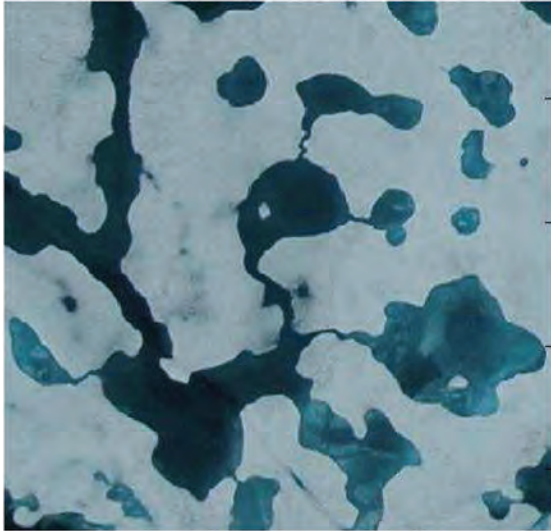


**Melt pond connectivity enables vast expanses of melt water to drain down seal holes, thaw holes, and leads in the ice.**



# Network modeling of Arctic melt ponds

Barjatia, Tasdizen, Song, Sampson, Golden  
*Cold Regions Science and Tecnology*, 2016



**develop algorithms to map  
images of melt ponds onto**

**random resistor networks**

**graphs of nodes and edges  
with edge conductances**

edge conductance  $\sim$  neck width

***compute effective  
horizontal fluid conductivity***

Ising model for ferromagnets

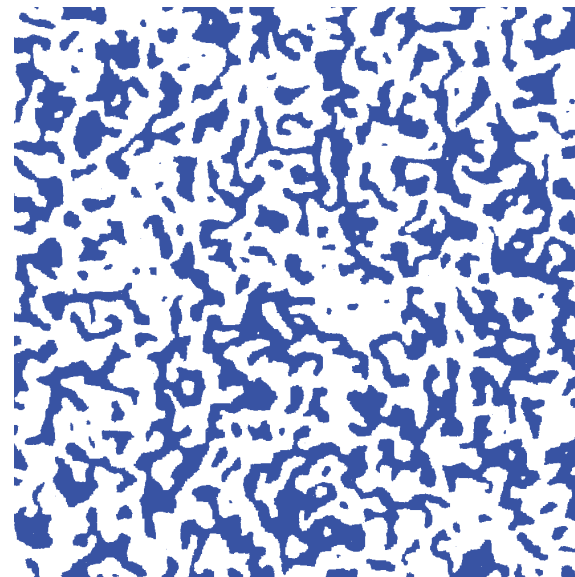
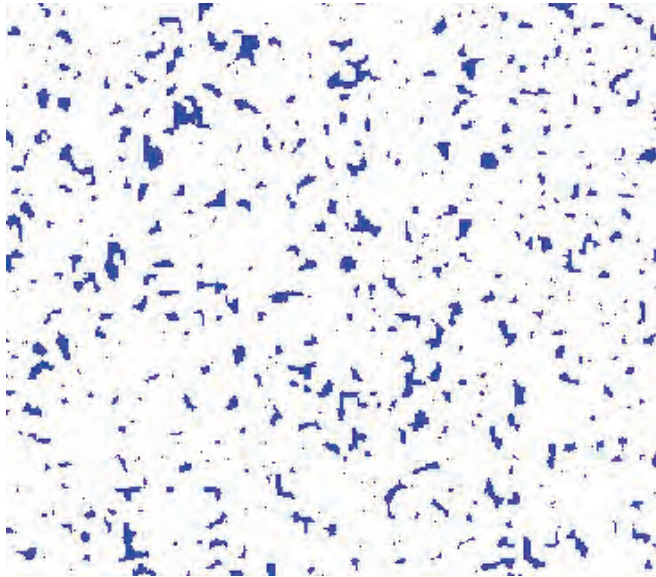


Ising model for melt ponds

$$\mathcal{H}_\omega = -J \sum_{\langle i,j \rangle}^N s_i s_j - H \sum_i^N s_i \quad s_i = \begin{cases} \uparrow & +1 & \text{water} & (\text{spin up}) \\ \downarrow & -1 & \text{ice} & (\text{spin down}) \end{cases}$$

magnetization  $M = \lim_{N \rightarrow \infty} \frac{1}{N} \left\langle \sum_j s_j \right\rangle$

pond coverage  $\frac{(M+1)}{2}$



***“melt ponds” are clusters of magnetic spins that align with the applied field***

predictions of fractal transition, pond size exponent Ma, Sudakov, Strong, Golden 2017



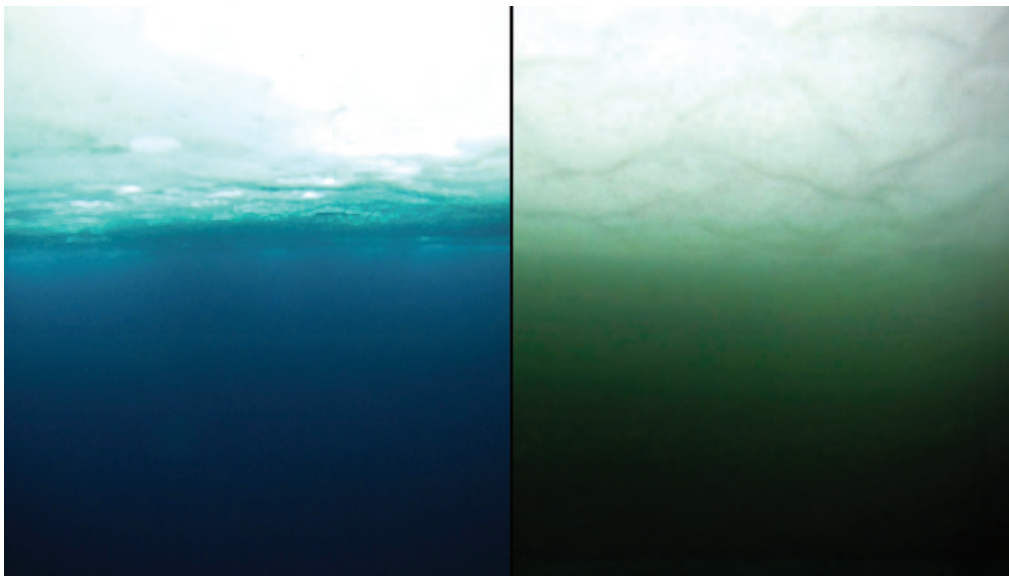
# 2011 massive under-ice **algal bloom**

Arrigo et al., *Science* 2012

melt ponds act as

**WINDOWS**

allowing light  
through sea ice



no bloom

bloom

***Have we crossed into a  
new ecological regime?***



# The Melt Pond Conundrum:

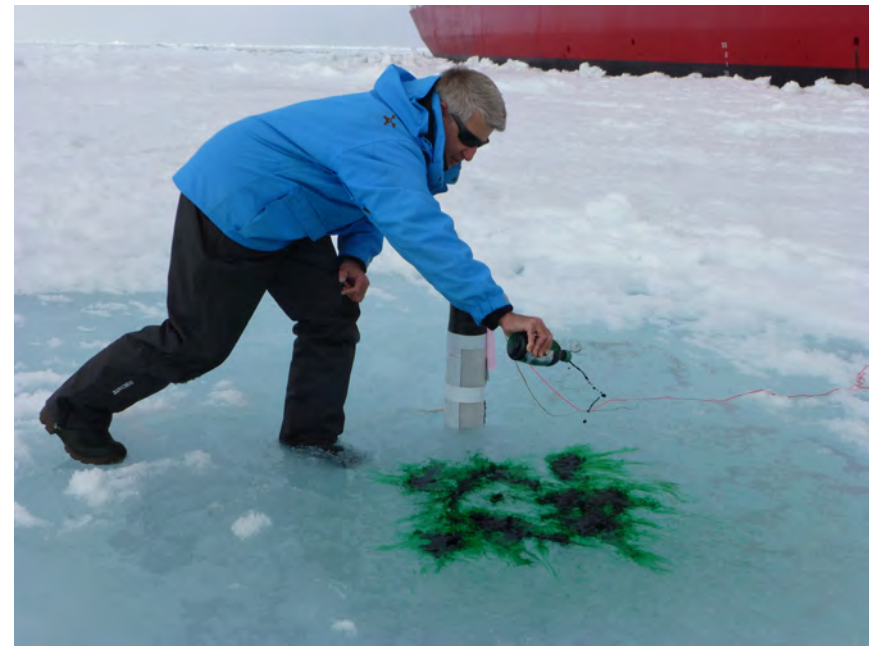
*How can ponds form on top of sea ice that is highly permeable?*

C. Polashenski, K. M. Golden, D. K. Perovich, E. Skyllingstad, A. Arnsten, C. Stwertka, N. Wright

**Percolation Blockage: A Process that Enables Melt Pond Formation on First Year Arctic Sea Ice**

*J. Geophys. Res. Oceans 2017*

*2014 Study of Under Ice Blooms in the Chuckchi Ecosystem (SUBICE)  
aboard USCGC Healy*



# ***Conclusions***

1. Summer Arctic sea ice is **melting rapidly**, and **melt ponds** and other processes must be accounted for in order to predict melting rates.
2. **Fluid flow** through sea ice mediates **melt pond evolution** and many processes important to climate change and polar ecosystems.
3. **Statistical physics and homogenization help link scales**, provide rigorous methods for finding effective behavior, and advance how sea ice is represented in climate models.
4. Critical behavior (in many forms) is inherent in the climate system.
5. Field experiments are essential to developing relevant mathematics.
6. Our research will help to **improve projections of climate change**, the fate of Earth's sea ice packs, and the ecosystems they support.



# THANK YOU

## National Science Foundation

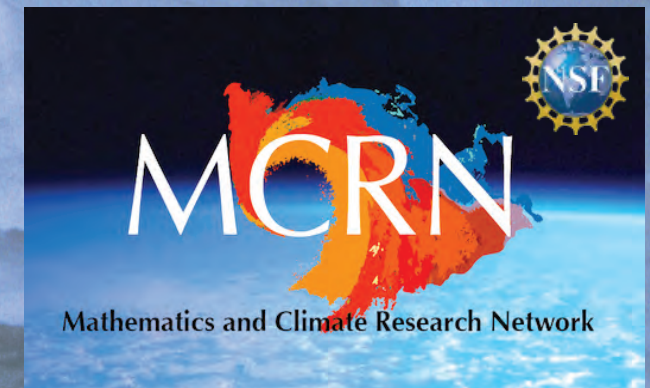
Division of Mathematical Sciences

Division of Polar Programs

## Office of Naval Research

Arctic and Global Prediction Program

Applied and Computational Analysis Program



***Buchanan Bay, Antarctica    Mertz Glacier Polynya Experiment    July 1999***



# Fire endangers Hobart's ice ship

By DAVID CARRIGG

AN engine-room fire has left the Hobart-based Antarctic research ship *Aurora Australis* without power in dangerous sea ice off the Antarctic coast.

None of the 79 people on board was injured in the blaze, which broke out early yesterday morning while the ship was in deep water 185km off the coast.

The extent of the damage is not known.

Australian Antarctic Division director Rex Moncur said the fire was extinguished by flooding the engine room with an inert gas.

The gas had to be cleared before crew wearing breathing apparatus could enter and assess the situation.

He said it could be some time before the extent of damage was known.

The 25 crew and 54 expeditioners, mostly from Hobart, would wear thermal clothing and stay below decks to keep warm.

"There is always a risk of becoming ice-bound in these waters at this time of the year but at this stage we don't expect to launch a rescue mission from Hobart," Mr Moncur said.

The ship was in regular radio contact with the Antarctic Div-



A file photo of the *Aurora Australis* in Antarctica.

ision's Hobart office.

He expected the expeditioners and crew to abandon the pioneering winter voyage and return the ship to Hobart for repairs in about a week.

The Antarctic Division, which hires the ship from P&O Australia, would not be hiring another vessel for the expedition.

"It's a pretty specialist vessel so you couldn't get the sort of research capability that this ship has got readily available," Mr Moncur said.

"We hope the next voyage can still proceed on schedule, which is early September."

The *Aurora Australis* is owned by P&O Australia and chartered by the Antarctic Div-

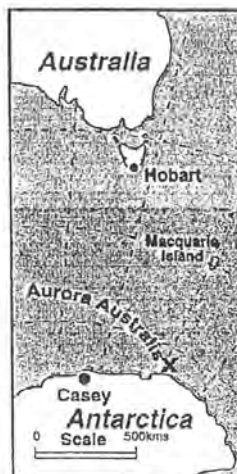
ision for about \$11 million a year.

P&O Australia managing director Richard Hein said yesterday the company was assessing the situation and a number of rescue options were being considered.

It was too early to say whether P&O would be liable for the cost of the aborted mission.

The vessel left Hobart last Wednesday for a seven-week voyage mainly to study a polynya, an area where savage winds break up the sea ice and cause heavy, salt-laden water to sink to the bottom.

The ship was nearing the polynya when the fire broke out.



Oceanographers believe a closer study of the phenomenon will lead to a better understanding of climate change.

CSIRO Marine Research oceanographer Steve Rintoul said the dense bottom water, created only in a few places in Antarctica and to a lesser extent in the North Atlantic, was critical to the chemistry and biology of the world's oceans.

## Fire strands Antarctic ship in sea ice

AN engine room fire has disabled the icebreaker *Aurora Australis* in sea ice, deep in Antarctic waters.

There were no injuries and the ship was not in danger after Tuesday night's fire.

Australian Antarctic Division director Mr Rex Moncur said. But Mr Moncur said he expected it would have to abandon its pioneering mid-winter voyage to the edge of the Ant-

arctic continent and return to Hobart for repairs.

The cause of the fire was not known but the engines have been turned off, with the ship 100 nautical miles from the Antarctic coast.

### THE CANBERRA TIMES

Thursday 23 July 1998

Page 4

## Antarctic voyage stopped by fire

HOBART: An engine room fire has disabled the Australian icebreaker *Aurora Australis* in sea ice, deep in Antarctic waters.

Australian Antarctic Division director Rex Moncur said there were no injuries and the ship was not in danger after Tuesday night's fire.

But Mr Moncur said he expected *Aurora Australis* would have to abandon its pioneering mid-winter voyage to the edge of the Antarctic continent to return to Hobart for repairs.

The fire had been extinguished and the engines were turned off, leaving the ship in sea ice about 100 nautical miles from the Antarctic coast, he said. The weather was good.

Crew had to wear breathing apparatus to enter the engine room and it was likely to be 24 hours before the damage could be fully assessed.

The *Aurora*, with 54 expeditioners and 25 crew, left Hobart last Wednesday for a seven-week voyage which was to have focused on a polynya, an area where savage winds break up the sea ice and cause heavy, salt-laden water to sink to the bottom.

Mr Moncur said, the cause of the fire was not yet known.

2:45 am July 22, 1998

"Please don't be alarmed but we have an uncontrolled fire in the engine room ...."

about 10 minutes later ...

"Please don't be alarmed but we're lowering the lifeboats ...."

*Sydney Morning Herald*  
23 July, 1998

### ICEBREAKER BURNS

A pioneering \$2-million Australian scientific voyage to the mid-winter Antarctic polynya is expected to be scrapped following an engine room fire on the *Aurora Australis* yesterday. The 54 people on board were forced on deck in the

