

**3.2.** Let  $\Omega = \mathbf{N} = \{1, 2, \dots\}$  denote the numerals. For all  $n = 1, 2, \dots$  define  $\mathcal{F}_n$  to be the  $\sigma$ -algebra generated by  $\{1\}, \dots, \{n\}$ . For example,  $\mathcal{F}_1 = \{\emptyset, \mathbf{N}, \{1\}, \mathbf{N} \setminus \{1\}\}$ ,  $\mathcal{F}_2 = \{\emptyset, \mathbf{N}, \{1\}, \{2\}, \{1, 2\}, \mathbf{N} \setminus \{1\}, \mathbf{N} \setminus \{2\}, \mathbf{N} \setminus \{1, 2\}\}$ , and so on. Evidently,  $\mathcal{F}_n \subset \mathcal{F}_{n+1}$ . However,  $\{1, 3, 5, \dots\} \notin \cup_{i=1}^{\infty} \mathcal{F}_i$ .