

1.8. Evidently, the distribution is

$$P\{X = k\} = \frac{\binom{r}{k} \binom{b}{n-k}}{\binom{r+b}{n}}, \quad k = 0, \dots, n.$$

Now

$$\begin{aligned} EX &= \sum_{k=0}^n k \frac{\binom{r}{k} \binom{b}{n-k}}{\binom{r+b}{n}} = \binom{r+b}{n}^{-1} \sum_{k=1}^n k \binom{r}{k} \binom{b}{n-k} = \binom{r+b}{n}^{-1} \sum_{k=1}^n \frac{r!}{(r-k)!(k-1)!} \binom{b}{n-k} \\ &= \frac{r}{\binom{r+b}{n}} \sum_{k=1}^n \binom{r-1}{k-1} \binom{b}{\{n-1\} - \{k-1\}} = \frac{r}{\binom{r+b}{n}} \binom{b+r-1}{n-1} = \frac{rn!(b+r-n)!}{(b+r)!} \frac{(b+r-1)!}{(b+r-n)!(n-1)!} \\ &= \frac{nr}{b+r}. \end{aligned}$$

To compute variance we first compute $E(X^2)$, viz.,

$$E(X^2) = \sum_{k=0}^n k^2 \frac{\binom{r}{k} \binom{b}{n-k}}{\binom{r+b}{n}} = \binom{r+b}{n}^{-1} \sum_{k=1}^n k^2 \binom{r}{k} \binom{b}{n-k}.$$