

# MATH 1220-90 Fall 2011

## Second Midterm Exam

INSTRUCTOR: H.-PING HUANG

LAST NAME \_\_\_\_\_

FIRST NAME \_\_\_\_\_

ID NO. \_\_\_\_\_

**INSTRUCTION:** SHOW ALL OF YOUR WORK. MAKE SURE YOUR ANSWERS ARE CLEAR AND LEGIBLE. USE **SPECIFIED** METHOD TO SOLVE THE QUESTION. IT IS NOT NECESSARY TO SIMPLIFY YOUR FINAL ANSWERS.

PROBLEM 1 20 \_\_\_\_\_

PROBLEM 2 20 \_\_\_\_\_

PROBLEM 3 20 \_\_\_\_\_

PROBLEM 4 20 \_\_\_\_\_

PROBLEM 5 20 \_\_\_\_\_

TOTAL 100 \_\_\_\_\_

2

## PROBLEM 1

(20 pt) Find the integral

$$\int x \ln(2x) dx.$$

## PROBLEM 2

(20 pt) Show that

$$\int_1^{\infty} \frac{1}{x^p} dx$$

diverges for  $p \leq 1$  and converges for  $p > 1$ .

4

### PROBLEM 3

(20 pt) Find

$$\int \sin^5 x \, dx.$$

## PROBLEM 4

(20 pt) **Distinct Linear Factors** Decompose

$$\frac{1}{x^2 + x - 6}$$

and then find its indefinite integral.

6

## PROBLEM 5

(20 pt) Find

$$\lim_{x \rightarrow 0} \frac{\sin x - x}{x^3}$$