

- <u>Half-life</u> is the time it takes for half of a population to vanish if it decreases by the same percent each time period.
- EX 1: If a city of 1000 people is decreasing by 10% each year, when will there be half as many people?

Year	Number of people

After a time, *t*, an exponentially decaying quantity with a half life of  $T_{half}$  decreases in size by a factor of  $(1/2)^{t/T}$ . The new value is related to the initial value by *new value* = *initial value* ×  $(1/2)^{t/T}$ .

## Approximate Half-life

For a quantity decaying exponentially at a rate of P% per time period  $T_{half} \approx \frac{70}{P}$ 

This works best for small rates and breaks down for rates over about 15%.

EX 2: Radioactive carbon-14 has a half-life of about 5700 years. It collects in organisms only while they are alive. Once they are dead, it only decays. What fraction of carbon-14 in an animal bone still remains 800 years after the animal has died?

- EX 3: A clean-up project is reducing the concentration of a pollutant in the water supply, with a 3.5% decrease per week.
  - a) What is the approximate half-life of the concentration of the pollutant?

b) What fraction of the original will remain after one year?

Exact half-life formula:

 $T_{half} = - \frac{log_{10}(2)}{log_{10}(1+r)}$  where *r* is a decimal and negative.

Note: The units of time for *r* and *T* must be the same (per month, year, etc.)

EX 4: Suppose the Russian ruble is falling in value against the dollar at 11% per year.

a) Approximately how long will it take the ruble to lose half its value?

b) Exactly how long will it take the ruble to lose half its value?