

Section 4.2: LINEAR SYSTEMS IN TWO VARIABLES

Objectives:

- ✦ Solve systems of equations by elimination.
- ✦ Use systems of equations to solve real life problems.

$$\begin{aligned}3 \text{ drinks} + 4 \text{ doughnuts} &= \$10.00 \\2 \text{ drinks} + 2 \text{ doughnuts} &= \$ 6.00\end{aligned}$$

How much is 1 doughnut?

The method of elimination

1. Obtain coefficients for x (or y) that are opposites by multiplying all terms of one or both equations by suitable constants.
2. Add the equations to eliminate one variable and solve the resulting equation.
3. Back-substitute the value obtained in step 2 in either of the original equations and solve for the other variable.
4. Check your solution in both of the original equations.

$$\begin{aligned}4x - 5y &= 13 \\3x - y &= 7\end{aligned}$$

$$\begin{aligned}3x + 9y &= 8 \\2x + 6y &= 7\end{aligned}$$

① EXAMPLE:

Solve these systems by elimination.

a) $-x + 2y = 9$
 $x + 3y = 16$

b) $3y = 2x + 21$
 $\frac{2}{3}x = 50 + y$

c) $4x = 6 + 5y$
 $8x = 12 + 10y$

② EXAMPLE:

Solve these applications by an appropriate method.

- a) An SUV costs \$26,445 and an average of \$0.18 per mile to maintain.
A hybrid model of the SUV costs \$31,910 and \$0.13 to maintain.

After how many miles will the cost of the SUV exceed the cost of the hybrid?

- b) A total of \$1790 was made by selling 200 adult tickets and 316 children's tickets to a charity event. The next night a total of \$937.50 was made by selling 100 adult tickets and 175 children's tickets.

Find the price of each type of ticket.