Math 3070 § 1. Probabilistic Computations Name: Example Treibergs Five Card Stud Poker Hands May 24, 2011

Rⓒ can do probabilistic computations, using its built in combinations function. We build a table that has the counts of various poker hands and their probabilities. We add labels and adjust the format to make a nicer presentation.

## R Session:

```
R version 2.11.1 (2010-05-31)
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[R.app GUI 1.34 (5589) i386-apple-darwin9.8.0]
[Workspace restored from /home/1004/ma/treibergs/.RData]
######################### BUILD A MATRIX WITH COUNTS OF HANDS #######################
x <- matrix(1:20,ncol=2)
xrn <- c("Number","Straight Flush","Four of a Kind","Full House","Flush","Straight",
"Three of a Kind","Two Pairs","One Pair","No Pair, less than the above")
rownames(x) <- xrn
colnames(x) <- c("Possible Poker Hands","Probability")
# The binomial coefficient is a built in function choose(). There is also factorial()
n <- choose (52,5);n
[1] 2598960
x[1,1] <- n
# Straight Flush: Same suit and in sequence, starting down from {A,K,Q,J,10,9,8,7,6,5}
# Number = Number of suits * number of starting kinds
x[2,1] <- 4 * 10
# Four of a kind
# Number = No. kinds for the four of a kind * No. remaining cards
x[3,1] <- 13 * (52-4)
>
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# Full house: Three of one kind and two of another
# Number = No. choices 1st kind * No. choices 2nd kind
                                    * No. suits for 3's * No.suits of 2's
x[4,1] <- 13*12*choose(4,3)*choose(4,2)
# Flush : All same suit but not in sequence
# Number = No. suits * combos of five in that suit - straight flushes
x[5,1] <- 4*choose(13,5) - x[2,1]
# Straight: in sequence but not flush
# Number = No. starting kinds * five choices of suits - No. straight flushes
x[6,1] <- 10*4^5 - x[2,1]
# Three of a kind
# Number = Choices of kind for three * Choice of suits of three
                                    * No. fourth card different kind * No. fifth card different than kinds
                    / No. Orders of last two cards
x[7,1] <- 13* choose(4,3) * (52-4) * (52-8) / 2
# Two pairs
# Number = No. kinds of first pair * No. kinds of second pair
# * No. suits of first pair * No. suits of second pair
# * No. remaining card of different kind / No. ordering of kinds
x[8,1] <- 13 * 12 * choose(4,2)^2 * (52-8) / 2
# One pair
# Number = No. kinds of pair * No. suits of pair * Choices of third card
                    * Choices of fourth card * Choices of fifth card
# / No. orderings of last three cards
x[9,1] <- 13 * choose(4,2) * (52-4) * (52-8) * (52-12) / factorial(3)
# No pair: none of the above
# Number = Number of hands - No. of all other types of hands = No. Everything else
x[10,1] <- x[1,1] - sum(x[2:9,1])
# The probability is the number divided by the total no. hands. We divide 1st column by n
# and store in the second column.
x[,2] <- x[,1]/n
x
    Possible Poker Hands Probability
Number 2598960 1.000000e+00
Straight Flush 40 1.539077e-05
Four of a Kind 624 2.400960e-04
Full House 3744 1.440576e-03
Flush
    5108 1.965402e-03
Straight 10200 3.924647e-03
Three of a Kind 54912 2.112845e-02
Two Pairs 123552 4.753902e-02
One Pair 1098240 4.225690e-01
No Pair, less than the above 1302540 5.011774e-01
```

```
##################### FORMATTING OUTPUT ##################################################
# The scientific notation is a little hard to see.
# To modify the printout, I'll use format() on the coloumns to right justify the first and
# not use scientific on the second. Then column-bind them together and print without quotes.
xn <- cbind(format(x[,1],justify="right"),format(x[,2],scientific=F,trim=F))
xrn <- c("Number","Straight Flush","Four of a Kind","Full House","Flush","Straight",
+ "Three of a Kind","Two Pairs","One Pair","No Pair, less than the above ")
rownames(xn) <- xrn
colnames(xn)<-c(" Hands "," Probability")
print(xn,quote=F)
\begin{tabular}{lrc} 
& \multicolumn{1}{c}{ Hands } & Probability \\
Number & 2598960 & 1.00000000000 \\
Straight Flush & 40 & 0.00001539077 \\
Four of a Kind & 624 & 0.00024009604 \\
Full House & 3744 & 0.00144057623 \\
Flush & 5108 & 0.00196540155 \\
Straight & 10200 & 0.00392464678 \\
Three of a Kind & 54912 & 0.02112845138 \\
Two Pairs & 123552 & 0.04753901561 \\
One Pair & 1098240 & 0.42256902761 \\
No Pair, less than the above & 1302540 & 0.50117739403
\end{tabular}
```

```
> ##################### RANDOMLY SELECTING POKER HANDS ######################################
```

> \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\# RANDOMLY SELECTING POKER HANDS \#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

# By the way, if you want to simulate card play, we store the card names and select

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# five randomly without replacement

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cards <- c("C-2","C-3","C-4","C-5","C-6","C-7","C-8","C-9","C10","C-J","C-Q","C-K",
cards <- c("C-2","C-3","C-4","C-5","C-6","C-7","C-8","C-9","C10","C-J","C-Q","C-K",
"C-A", "D-2", "D-3", "D-4", "D-5", "D-6", "D-7" , "D-8", "D-9", "D10" , "D-J" , "D-Q" ,"D-K",
"C-A", "D-2", "D-3", "D-4", "D-5", "D-6", "D-7" , "D-8", "D-9", "D10" , "D-J" , "D-Q" ,"D-K",
"D-A", "H-2", "H-3", "H-4", "H-5", "H-6", "H-7", "H-8" , "H-9", "H10" , "H-J" , "H-Q" , "H-K",
"D-A", "H-2", "H-3", "H-4", "H-5", "H-6", "H-7", "H-8" , "H-9", "H10" , "H-J" , "H-Q" , "H-K",
"H-A","S-2","S-3","S-4","S-5","S-6","S-7","S-8","S-9","S10","S-J","S-Q","S-K","S-A")
"H-A","S-2","S-3","S-4","S-5","S-6","S-7","S-8","S-9","S10","S-J","S-Q","S-K","S-A")
sample(cards,5,replace=F)
sample(cards,5,replace=F)
[1] "S-8" "C-7" "C-K" "S-K" "D-K"
[1] "S-8" "C-7" "C-K" "S-K" "D-K"

# Suppose we wish to deal out random hands to four players, and do this three times

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for(j in 1:3){
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+ deal <- sample(cards,20,replace=F)
+ deal <- sample(cards,20,replace=F)
+ cat(deal[1:5],"\n",deal[6:10],"\n",deal[11:15],"\n",deal[16:20],"\n\n")}
+ cat(deal[1:5],"\n",deal[6:10],"\n",deal[11:15],"\n",deal[16:20],"\n\n")}
H10 D-4 S-J H-3 D-A
H10 D-4 S-J H-3 D-A
C-Q D-Q C-6 S-K S10
C-Q D-Q C-6 S-K S10
S-4 S-7 S-6 H-8 D-K
S-4 S-7 S-6 H-8 D-K
D-5 H-J C-J H-6 H-9
D-5 H-J C-J H-6 H-9
S-5 D-6 H-8 S-6 H-K
S-5 D-6 H-8 S-6 H-K
D-K D-3 H-6 H-A S-2
D-K D-3 H-6 H-A S-2
C-A D-7 C-9 C-K S-J
C-A D-7 C-9 C-K S-J
S-A D-4 D-2 D-8 H-5
S-A D-4 D-2 D-8 H-5
H-7 S-2 H-J D-7 C-Q
H-7 S-2 H-J D-7 C-Q
H-3 D-9 C-J D-5 H-K
H-3 D-9 C-J D-5 H-K
D-K C-6 D10 C-8 D-2
D-K C-6 D10 C-8 D-2
H-4 S-3 S-K D-3 S-7

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    H-4 S-3 S-K D-3 S-7
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