Math 3070 § 1.	Probabilistic Computations	Name: Example
Treibergs	Five Card Stud Poker Hands	May 24, 2011

 $\mathbf{R}$  ( $\mathbf{C}$ ) can do probabilistic computations, using its built in combinations function. We build a table that has the counts of various poker hands and their probabilities. We add labels and adjust the format to make a nicer presentation.

## **R** Session:

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R version 2.11.1 (2010-05-31)
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R is free software and comes with ABSOLUTELY NO WARRANTY.
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R is a collaborative project with many contributors.
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'help.start()' for an HTML browser interface to help.
Type 'q()' to quit R.
[R.app GUI 1.34 (5589) i386-apple-darwin9.8.0]
[Workspace restored from /home/1004/ma/treibergs/.RData]
> x <- matrix(1:20,ncol=2)</pre>
> xrn <- c("Number","Straight Flush","Four of a Kind","Full House","Flush","Straight",
+ "Three of a Kind", "Two Pairs", "One Pair", "No Pair, less than the above")
> rownames(x) <- xrn</pre>
> colnames(x) <- c("Possible Poker Hands","Probability")</pre>
>
> # The binomial coefficient is a built in function choose(). There is also factorial()
> n <- choose(52,5);n</pre>
[1] 2598960
> x[1,1] <- n
> # Straight Flush: Same suit and in sequence, starting down from {A,K,Q,J,10,9,8,7,6,5}
> #
       Number = Number of suits * number of starting kinds
> x[2,1] <- 4 * 10
>
> # Four of a kind
> #
       Number = No. kinds for the four of a kind * No. remaining cards
> x[3,1] <- 13 * (52-4)
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> # Full house: Three of one kind and two of another
       Number = No. choices 1st kind * No. choices 2nd kind
> #
> #
                  * No. suits for 3's * No.suits of 2's
> x[4,1] <- 13*12*choose(4,3)*choose(4,2)</pre>
>
> # Flush : All same suit but not in sequence
       Number = No. suits * combos of five in that suit - straight flushes
> #
> x[5,1] <- 4*choose(13,5) - x[2,1]
> # Straight: in sequence but not flush
> #
        Number = No. starting kinds * five choices of suits - No. straight flushes
> x[6,1] <- 10*4<sup>5</sup> - x[2,1]
>
> # Three of a kind
> #
       Number = Choices of kind for three * Choice of suits of three
> #
                 * No. fourth card different kind * No. fifth card different than kinds
> #
                 / No. Orders of last two cards
> x[7,1] <- 13 * choose(4,3) * (52-4) * (52-8) / 2
>
> # Two pairs
        Number = No. kinds of first pair * No. kinds of second pair
> #
> #
                 * No. suits of first pair * No. suits of second pair
> #
                 * No. remaining card of different kind / No. ordering of kinds
> x[8,1] <- 13 * 12 * choose(4,2)<sup>2</sup> * (52-8) / 2
>
> # One pair
> #
       Number = No. kinds of pair * No. suits of pair * Choices of third card
> #
                 * Choices of fourth card * Choices of fifth card
> #
                  / No. orderings of last three cards
> x[9,1] <- 13 * choose(4,2) * (52-4) * (52-8) * (52-12) / factorial(3)
>
> # No pair: none of the above
        Number = Number of hands - No. of all other types of hands = No. Everything else
> #
> x[10,1] <- x[1,1] - sum(x[2:9,1])
> # The probability is the number divided by the total no. hands. We divide 1st column by n
> # and store in the second column.
>
> x[,2] <- x[,1]/n
> x
                             Possible Poker Hands Probability
                                          2598960 1.000000e+00
Number
Straight Flush
                                               40 1.539077e-05
Four of a Kind
                                              624 2.400960e-04
Full House
                                             3744 1.440576e-03
Flush
                                             5108 1.965402e-03
                                            10200 3.924647e-03
Straight
Three of a Kind
                                            54912 2.112845e-02
Two Pairs
                                           123552 4.753902e-02
One Pair
                                         1098240 4.225690e-01
No Pair, less than the above
                                         1302540 5.011774e-01
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2
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> # The scientific notation is a little hard to see.
> # To modify the printout, I'll use format() on the coloumns to right justify the first and
> # not use scientific on the second. Then column-bind them together and print without quotes.
>
> xn <- cbind(format(x[,1],justify="right"),format(x[,2],scientific=F,trim=F))</pre>
> xrn <- c("Number","Straight Flush","Four of a Kind","Full House","Flush","Straight",</pre>
+ "Three of a Kind", "Two Pairs", "One Pair", "No Pair, less than the above
                                                                         ")
> rownames(xn) <- xrn</pre>
                            "," Probability")
> colnames(xn)<-c(" Hands</pre>
> print(xn,quote=F)
                                 Hands
                                           Probability
                                2598960
                                           1.0000000000
Number
Straight Flush
                                    40
                                           0.00001539077
Four of a Kind
                                    624
                                           0.00024009604
Full House
                                   3744
                                           0.00144057623
Flush
                                   5108
                                           0.00196540155
Straight
                                  10200
                                           0.00392464678
Three of a Kind
                                  54912
                                           0.02112845138
Two Pairs
                                 123552
                                           0.04753901561
One Pair
                                1098240
                                           0.42256902761
No Pair, less than the above
                                1302540
                                           0.50117739403
> # By the way, if you want to simulate card play, we store the card names and select
> # five randomly without replacement
>
> cards <- c("C-2","C-3","C-4","C-5","C-6","C-7","C-8","C-9","C10","C-J","C-Q","C-K",
+ "C-A", "D-2", "D-3", "D-4", "D-5", "D-6", "D-7", "D-8", "D-9", "D10", "D-J", "D-Q", "D-K",
+ "D-A", "H-2", "H-3", "H-4", "H-5", "H-6", "H-7", "H-8", "H-9", "H10", "H-J", "H-Q", "H-K",
+ "H-A", "S-2", "S-3", "S-4", "S-5", "S-6", "S-7", "S-8", "S-9", "S10", "S-J", "S-Q", "S-K", "S-A")
> sample(cards,5,replace=F)
[1] "S-8" "C-7" "C-K" "S-K" "D-K"
> # Suppose we wish to deal out random hands to four players, and do this three times
> for(j in 1:3){
+
               deal <- sample(cards,20,replace=F)</pre>
               cat(deal[1:5],"\n",deal[6:10],"\n",deal[11:15],"\n",deal[16:20],"\n\n")}
+
H10 D-4 S-J H-3 D-A
C-Q D-Q C-6 S-K S10
S-4 S-7 S-6 H-8 D-K
D-5 H-J C-J H-6 H-9
S-5 D-6 H-8 S-6 H-K
D-K D-3 H-6 H-A S-2
C-A D-7 C-9 C-K S-J
S-A D-4 D-2 D-8 H-5
H-7 S-2 H-J D-7 C-Q
H-3 D-9 C-J D-5 H-K
D-K C-6 D10 C-8 D-2
H-4 S-3 S-K D-3 S-7
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