- 1. Consider the vectors $\vec{u} = \mathbf{i} 2\mathbf{j} + \mathbf{k}$ and $\vec{v} = 3\mathbf{i} 4\mathbf{j} + \mathbf{k}$.
 - (a) Find the length of \vec{u} .
 - (b) Find $\vec{N} = \vec{u} \times \vec{v}$.
 - (c) Find the cartesian equation of the plane with normal \vec{N} through the point $P_0 = (1, 0, -1)$.
 - (d) Find the vector projection of \vec{v} onto \vec{u} .
- 2. Determine the area of the triangle with vertices P = (0, 0), Q = (3, 2), R = (1, 4).
- 3. Rewrite the vector $\vec{v} = 4\mathbf{i} + 5\mathbf{j}$, in the orthonormal basis $\vec{e_1} = (\sqrt{3}/2, 1/2), \vec{e_2} = (-1/2, \sqrt{3}/2)$. In other words, expand or write \vec{v} as $\vec{v} = a\vec{e_1} + b\vec{e_2}$ where a and b are scalar values.
- 4. Find the work done by the force $\vec{F} = 6\mathbf{i} + 8\mathbf{j}$ pounds in moving an object from (1,0) to (6,8) where distance is in feet.
- 5. Given three points: A = (0, 5, 3), B = (2, 7, 0), C = (-5, -3, 7)
 - (a) Which point is closest to the xz-plane? Explain your reasoning.
 - (b) Which point lies on the xy-plane? Explain your reasoning.
- 6. Determine the equation of the plane spanned by the vectors:

$$\vec{u} = 1\mathbf{i} + 3\mathbf{j} - 2\mathbf{k}$$
$$\vec{v} = 2\mathbf{i} + 6\mathbf{j} + 4\mathbf{k}$$

and which contains the origin.

- 7. Find the curvature of the line parameterized by $\vec{r}(t) = (1, 1, 1) + (2, 3, 4)t$.
- 8. Find the arc length of the helix

$$\vec{r}(t) = a\sin(t)\mathbf{i} + a\cos(t)\mathbf{j} + ct\mathbf{k}$$

for $0 \le t \le 2\pi$.

9. Find the equation of the plane orthogonal to the curve

$$\vec{r}(t) = (8t^2 - 4t + 3)\mathbf{i} + (\sin(t) - 4t)\mathbf{j} - \cos(t)\mathbf{k}$$

at the point $t = \pi/3$.

10. Determine the curvature κ of the helical curve parametrized by:

$$\vec{r}(t) = 7\sin(3t)\mathbf{i} + 7\cos(3t)\mathbf{j} + 14t\mathbf{k}$$

at $t = \pi/9$.

11. Given that the acceleration of a particle's motion is

$$\vec{a}(t) = -9\cos(3t)\mathbf{i} + -9\sin(3t)\mathbf{j} + 2t\mathbf{k}.$$

And the particle has initial velocity $\vec{v}_0 = \mathbf{i} + \mathbf{k}$ and initial position $\vec{x}_0 = \mathbf{i} + \mathbf{j} + \mathbf{k}$.

- (a) Determine the velocity function $\vec{v}(t)$.
- (b) Determine the position function $\vec{x}(t)$.
- 12. Let $\vec{u} = (2, 2)$ and $\vec{v} = (3, -1)$. Find $\vec{u} + \vec{v}$ and illustrate this vector addition with a diagram in the plane, showing \vec{u} , \vec{v} and the resultant vector.