

## Calculus: The Slope of a Line



There is only one line between any 2 points.

The slope of a line is:
The steepness of the line.
The vertical change over the horizontal change, denoted by $m$.
Given two points, $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right)$ in the Cartesian Plane,
$m=$

## Examples of slope:






EX 1
a) Find the slope of the line containing these points: $(-3,2)$ and $(2,5)$
b) Find the slope of the line containing these points: $(5,-6)$ and $(-2,-6)$

## 1 Slope of a Line

## Point-Slope Form of a Line

Given that $m=$ the slope of a line and it goes through the point $\left(x_{1}, y_{1}\right)$, then we know:

## Slope-Intercept Form of a Line

Given that the slope of a line is $m$ and the $y$-intercept is the point $(0, b)$, then the equation of the line is:

EX 2
a) Find the equation of the line going through $(-4,1)$ and $(5,2)$.
b) Find the equation of the line with slope, $m=3$ and $y$-intercept $(0,5)$.

## General Equation of a Line

Every line can be written in the form $A x+B y+C=0$, where $A, B$, and $C$ are integers.

## EX 3

Write the equations from Exercise 2 in general form.

## 1 Slope of a Line

## Parallel and Perpendicular Lines

Parallel lines have the same slope.

Perpendicular lines have negative reciprocal slopes.


EX4
a) Find the equation of the line parallel to $3 x-4 y=8$ which passes through the point $(1,3)$.
b) Find the equation of the line perpendicular to $y=-3 x+5$ which passes through the origin.

## 1 Slope of a Line

Determine the slope of each line segment in this function.


