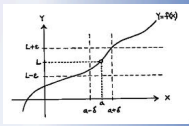
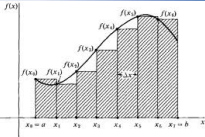


10 Rules Derivatives



$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\frac{d}{dx} \int_a^x f(t) dt = f(x)$$



$$\lim_{\max \Delta x_i \rightarrow 0} \sum_{i=1}^n f(x_i) \Delta x_i = \int_a^b f(x) dx$$

$$\int_a^b f(x) dx = F(b) - F(a)$$

Rules For Finding Derivatives

$$\frac{g(x) f'(x) - f(x) g'(x)}{(g(x))^2} = \frac{lo \cdot d hi - hi \cdot d lo}{lo \cdot lo}$$

Constant Function Rule

Identity Function Rule

Constant Multiple Rule

Sum & Difference Rule

10 Rules Derivatives

POWER RULE

n	$f(x)=x^n$	$f'(x)$	

EX 1 Find $f'(x)$ if $f(x) = 3x^7 - 4x^6 + x^5 + 2x^3 - x^2 + 4$

10 Rules Derivatives

Product Rule

If f and g are differentiable, then

$$D_x(f(x)g(x)) = f(x)D_x[g(x)] + D_x[f(x)]g(x) \quad .$$

EX 2 Find $f'(x)$ if $f(x) = (2x^3 - 4x + 1)(3x + 5)$.

a) Use the product rule:

b) Multiply out and use the power rule to check:

Quotient Rule

Let f and g be differentiable functions, $g(x) \neq 0$,

$$\text{then } D_x \frac{f(x)}{g(x)} = \frac{g(x)D_x[f(x)] - f(x)D_x[g(x)]}{g^2(x)} \quad .$$

EX 3 Find $f'(x)$ if $f(x) = \frac{2x^2 + 4x - 1}{3x - 2}$.

10 Rules Derivatives

EX 4 $y = \frac{-3}{x} + \frac{2}{x^4 - 7x}$ Find $y'(x)$

Note:

$$D_x(x^{-n}) = -nx^{-n-1} \quad \text{for } n, \text{ a positive integer}$$

EX 5 Find $f'(x)$ if $f(x) = \frac{5x-4}{x^2+1}$

EX 6 Find $D_x(y)$ if $y = 3x(x^3 - 2x + 1)$

EX 7 Find $\frac{dy}{dx}$ if $y = \frac{-3}{x^5} + \frac{2}{x}$

10 Rules Derivatives

$$\frac{g(x)f'(x) - f(x)g'(x)}{(g(x))^2}$$
$$= \frac{lo \cdot d hi - hi \cdot d lo}{lo \cdot lo}$$