

Math 1090 ~ Business Algebra

Section 3.7 Combinations of functions

Objectives:

- Form compositions of two functions.
- Determine the domain of the composite function.
 Perform arithmetic of functions.

Two functions can be combined to for a new function in these ways.

• addition
$$(f+g)(x) = f(x) + g(x)$$

• subtraction
$$(f-g)(x) = f(x) - g(x)$$

• multiplication
$$(f \cdot g)(x) = f(x) \cdot g(x)$$

• division
$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}$$

• composition
$$(f \circ g)(x) = f(g(x))$$

Ex 1 Given
$$f(x) = 2x + 5$$
 $g(x) = \frac{1}{x^3}$

a)
$$(f \circ g)(x)$$
 b) $(f+g)(1)$

c)
$$(g \circ f)(1)$$
 d) $\left(\frac{f}{g}\right)(x)$

Ex 2: Given
$$f(x) = x^2 - 1$$
 $g(x) = \frac{x}{2}$ $h(x) = \sqrt{x - 1}$ find

a)
$$(h \circ f)(x)$$
 d) $g(h(x))$

b)
$$(g-h)(1)$$
 e) $h(f(g(x)))$

c)
$$(hf)(3)$$

Ex 3: For these functions, find g(h(x)) and its domain.

Ex 4: The daily cost of producing x units in a manufacturing process is C(x) = IIx + 350. The number of units produced in t hours during a day is given by x(t) = I0t for $0 \le t \le 8$. Find, simplify and interpret C(x(t)).