

$$5x - 2y \leq 75$$



$$\begin{bmatrix} a & b \\ c & d \end{bmatrix}$$



$$S = Pe^{rt}$$



$$APY = \left(1 + \frac{r}{n}\right)^n - 1$$

## Math 1090 ~ Business Algebra

### Section 2.2 Matrix Multiplication

Objectives:

- Determine whether two matrices can be multiplied together.
- Multiply two matrices.
- Write an Identity matrix of the proper size.

#### Definitions

##### Matrix Multiplication AB

Given A (size  $m \times n$ ) and B (size  $n \times p$ ) AB is an  $m \times p$  matrix with  $ij$  entry given by  $a_{i1}b_{1j} + a_{i2}b_{2j} + \dots + a_{in}b_{nj}$ . i.e. the product/sum of the  $i^{\text{th}}$  row of A with the  $j^{\text{th}}$  column of B.

##### Identity Matrix I

I is always a square matrix which has 1 in each diagonal entry and zeros everywhere else.

#### Properties of Matrix Multiplication

1.  $(AB)C = A(BC)$
2.  $A(B + C) = AB + AC$
3.  $(B + C)A = BA + CA$
4.  $(AB)^T = B^T A^T$

$$AB \neq BA$$

Ex 1: Given  $A = \begin{bmatrix} 1 & 0 & 4 \\ 5 & 1 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & 2 \\ 3 & -2 \\ -1 & 0 \end{bmatrix}$

Find  $AB$  and  $BA$ , if possible.

Ex 2: Is  $(AA^T)^T = A^T A$ ?

Ex 3: Given  $A = \begin{bmatrix} 0 & 1 & 3 \\ 2 & 0 & 1 \\ 0 & 0 & -4 \end{bmatrix}$ , find  $A^2$ .

Ex 4: Solve for  $x$ .

$$\begin{bmatrix} -5 \\ 10 \\ -19 \end{bmatrix} + \begin{bmatrix} -2x \\ 13 \\ -8 \end{bmatrix} + \begin{bmatrix} -8 \\ -4 \\ -7 \end{bmatrix} = \begin{bmatrix} 5 \\ 19 \\ -34 \end{bmatrix}$$

Ex 5: Solve for  $x$  and  $y$ .

$$\begin{bmatrix} 1 & 3 \\ -1 & 5 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 11 \\ 5 \end{bmatrix}$$