2018-2019 Undergraduate Problem Solving Contest

Problem Number 1

Due October 29, 2018

Find all the \mathbb{R} solutions to the following system of equations.

$$x^4 + y^4 = 1$$

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Provide the numerical solution or solutions, and prove that your \mathbb{R} solution(s) are the only ones that can exist.

New and old problems are posted online at http://www.math.utah.edu/undergrad/involvement.php

In the spirit of UPSC, you should not use the internet or look up the solution in a book. Please include your name, student ID number, and email address on your solution. Submit answers at the front desk of the T. Benny Rushing Mathematics Center.