

Name _____ Date _____

Instructions: Please show all of your work as partial credit will be given where appropriate, **and** there may be no credit given for problems where there is no work shown. All answers should be completely simplified, unless otherwise stated.

1. (15 points) Take the region $R = \{(x, y) : 0 \leq x \leq 4, 0 \leq y \leq 8\}$, the function $f(x, y) = x^2 + 2xy - y + x^3$, and the partition P of R into eight equal squares by the lines $x = 2$, $y = 2$, $y = 4$, and $y = 6$.

Approximate $\iint_R f(x, y) dA$ by calculating the corresponding Riemann sum $\sum_{k=1}^8 f(\bar{x}_k, \bar{y}_k) \Delta A_k$, assuming that (\bar{x}_k, \bar{y}_k) are the centers of the eight squares.

Answer: _____

2. Evaluate the following integrals.

(a) $\int_0^3 \int_1^3 (x^2 + x + y + 1) dx dy$. (10 points)

Answer : _____

(b) $\int_{-1}^1 \int_{-x}^{2-x^2} (x + y) dy dx$. (15 points)

Answer: _____