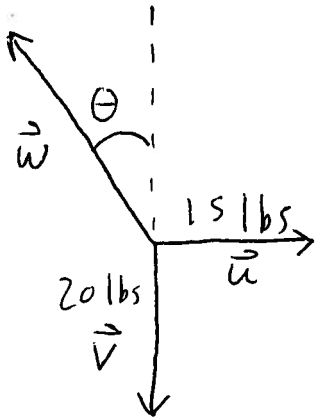


Name Key Date 7-11-2012

Instructions: Please show all of your work as partial credit will be given where appropriate, **and** there may be no credit given for problems where there is no work shown.

1. Force \mathbf{u} has a magnitude of 15 pounds in the East direction. Force \mathbf{v} has a magnitude of 20 pounds in the South direction. Find the magnitude and direction (geometrically) of the force \mathbf{w} needed to counterbalance \mathbf{u} and \mathbf{v} . (Just write answers in as simplified a form as you can without a calculator.)



$$\|\vec{w}\| = \sqrt{(15 \text{ lbs})^2 + (20 \text{ lbs})^2} \\ = 25 \text{ lbs}$$

$$\theta = \tan^{-1}\left(\frac{15}{20}\right) = \tan^{-1}\left(\frac{3}{4}\right)$$

West of North

magnitude of \mathbf{w} : 25 lbs

direction of \mathbf{w} : $N \tan^{-1}\left(\frac{3}{4}\right) W$

2. For $\mathbf{u} = \langle 0, 4, 2 \rangle$ and $\mathbf{v} = 4\mathbf{i} + 3\mathbf{j} - 2\mathbf{k}$,

(a) find $2\mathbf{u} - 3\mathbf{v}$.

$$2\langle 0, 4, 2 \rangle - 3\langle 4, 3, -2 \rangle \\ = \langle 0, 8, 4 \rangle - \langle 12, 9, -6 \rangle = \langle -12, -1, 10 \rangle$$

(b) find $\hat{\mathbf{u}}$.

$$\frac{2\mathbf{u} - 3\mathbf{v}}{\|2\mathbf{u} - 3\mathbf{v}\|} = \frac{\langle -12, -1, 10 \rangle}{\| \langle -12, -1, 10 \rangle \|}$$

$$\|\vec{u}\| = \sqrt{0^2 + 4^2 + 2^2} = \sqrt{20} = 2\sqrt{5}$$

$$\hat{\mathbf{u}} = \frac{1}{2\sqrt{5}} \langle 0, 4, 2 \rangle = \left\langle 0, \frac{2}{\sqrt{5}}, \frac{1}{\sqrt{5}} \right\rangle$$

$$\hat{\mathbf{u}} = \underline{\left\langle 0, \frac{2}{\sqrt{5}}, \frac{1}{\sqrt{5}} \right\rangle}$$

3. Find the projection of $\langle 2, 3, -3 \rangle$ onto the vector $\langle 1, 1, -2 \rangle$

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$$\vec{u} = \langle 2, 3, -3 \rangle \quad \vec{v} = \langle 1, 1, -2 \rangle$$

$$\text{proj}_{\vec{v}}(\vec{u}) = \frac{\vec{u} \cdot \vec{v}}{\vec{v} \cdot \vec{v}} \vec{v}$$

$$\vec{u} \cdot \vec{v} = 2(1) + 3(1) + (-3)(-2) = 11$$

$$\vec{v} \cdot \vec{v} = 1(1) + 1(1) + (-2)(-2) = 6$$

$$\text{proj}_{\vec{v}}(\vec{u}) = \frac{11}{6} \langle 1, 1, -2 \rangle = \left\langle \frac{11}{6}, \frac{11}{6}, -\frac{11}{3} \right\rangle$$

projection: $\left\langle \frac{11}{6}, \frac{11}{6}, -\frac{11}{3} \right\rangle$

8 4. Circle all of the following statements that make sense.

(a) $\vec{u} \cdot (\vec{v} - \vec{w})$

(b) $|\vec{u}|(\vec{v} \times \vec{w})$

(c) $(\vec{u} \times \vec{v}) \times \vec{w}$

(d) $(\vec{u} \cdot \vec{v}) \cdot \vec{w}$