

Name Dylan Zwick (Solutions) Date 6/03/09

Instructions: Please show all of your work as partial credit will be given where appropriate, **and** there may be no credit given for problems where there is no work shown. All answers should be completely simplified, unless otherwise stated.

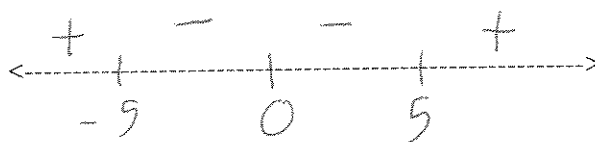
1. (8 points) For $f(x) = \frac{2(x-5)^2}{x}$

(with derivatives given by $f'(x) = \frac{2x^2 - 50}{x^2}$, $f''(x) = \frac{100}{x^3}$)

(a) Find the x-value of the vertical asymptote. (1 point)

V.A.: $x = 0$

(b) Fill in the sign line for $f'(x)$. (2 points)

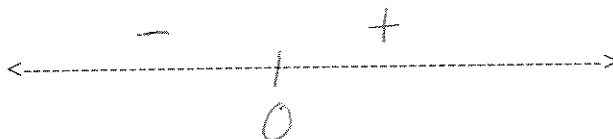


(c) Find all local min and max points, if there are any. (2 points)

Max points: $(-5, -40)$

Min points: $(5, 0)$

(d) Fill in the sign line for $f''(x)$. (2 points)



(e) Find all inflection points, if there are any. (1 point)

Inflection points: None

Note: $x = 0$ is not an inflection point, as $f(0)$ is not defined

2. (4 points) For $f(x) = 2x^2 - 5x + 1$ on $[0, 3]$, decide whether or not the Mean Value Theorem (for derivatives) applies. If it does, find all acceptable values of c . If not, then state the reason.

$f(x)$ is continuous on $[0, 3]$

$f'(x) = 4x - 5$ is well defined on $(0, 3)$.

So, the MVT applies.

$$\frac{f(3) - f(0)}{3 - 0} = \frac{4 - 1}{3} = 1, \quad f'(x) = 1 \Rightarrow 4x - 5 = 1 \\ \Rightarrow x = \frac{6}{4} = \frac{3}{2}$$

MVT applies: True or False (circle one)

If true, then $c = \underline{\frac{3}{2}}$

If false, then why? NA

3. (3 points) Evaluate.

$$\int (3x^4 - \sin x + \sqrt[5]{x^3}) dx$$

$$\int (3x^4 - \sin x + \sqrt[5]{x^3}) dx$$

$$= \int (3x^4 - \sin x + x^{3/5}) dx$$

$$= \frac{3}{5} x^5 + \cos x + \frac{x^{8/5}}{\frac{8}{5}} + C$$

$$= \frac{3}{5} x^5 + \cos x + \frac{5}{8} x^{8/5} + C$$

Answer 3: $\boxed{\frac{3}{5} x^5 + \cos x + \frac{5}{8} x^{8/5}}$