

Name _____ Date _____

Instructions: Please show all of your work as partial credit will be given where appropriate, **and** there may be no credit given for problems where there is no work shown. All answers should be completely simplified, unless otherwise stated.

1. (8 points) Find the directional derivative of $f(x, y) = 3x^2 - 2xy + 5y^2$ at $\mathbf{p} = (3, 1)$ in the direction of $\mathbf{a} = 2\mathbf{i} - \mathbf{j}$.

2. (8 points) In what direction \mathbf{u} does $f(x, y) = 4 - x^2y^2 + e^{2x} - 3y$ increase most rapidly at $\mathbf{p} = (0, 3)$?
 Answer: _____

3. (8 points) Find $\frac{\partial z}{\partial x}$ given $F(x, y, z) = 2x^2z - y^4 - xyz^2 = 0$.
 Answer: _____

Answer: _____

4. (8 points) Find $\frac{\partial w}{\partial t}$ for $w=e^{xy+z}$ given $x=s+t$, $y=s-t$ and $z=t^2$.

Answer: _____

5. (8 points) Find the equation of the tangent plane to $3x^2+y^2+3z^2=9$ at $(1, 0, \sqrt{2})$.

Answer : _____