

ASSIGNMENT 9

DYLAN ZWICK'S MATH

Section 6.2

In Exercises 1, 2, fill in the missing factor.

$$\mathbf{6.2.1:} \quad \frac{7x^2}{3y(x^2)} = \frac{7}{3y}, x \neq 0$$

$$\mathbf{6.2.2:} \quad \frac{14x(x-3)^2}{(x-3)(7(x-3)^2)} = \frac{7}{3y}$$

In Exercises 9-36, multiply and simplify. See Examples 1-5.

$$\mathbf{6.2.9:} \quad 4x \cdot \frac{7}{12x} = \frac{7}{3}, x \neq 0$$

$$\mathbf{6.2.11:} \quad \frac{8s^3}{9s} \cdot \frac{6s^2}{32s} = \frac{s^3}{6}, s \neq 0$$

$$\mathbf{6.2.15:} \quad \frac{8}{3+4x} \cdot (9+12x) = 24, x \neq -\frac{3}{4}$$

$$\mathbf{6.2.17:} \quad \frac{8u^2v}{3u+v} \cdot \frac{u+v}{12u} = \frac{2uv(u+v)}{3(3u+v)}, u \neq 0$$

$$\mathbf{6.2.23:} \quad \frac{4r-12}{r-2} \cdot \frac{r^2-4}{r-3} = 4(r+2), r \neq 2, 3$$

$$\mathbf{6.2.25:} \quad \frac{2t^2-t-15}{t+2} \cdot \frac{t^2-t-6}{t^2-6t+9} = 2t+5, t \neq -2, 3$$

$$\mathbf{6.2.27:} \quad (4y^2 - x^2) \cdot \frac{xy}{(x-2y)^2} = -\frac{xy(x+2y)}{x-2y}$$

$$\mathbf{6.2.29:} \quad \frac{x^2+2xy-3y^2}{(x+y)^2} \cdot \frac{x^2-y^2}{x+3y} = \frac{(x-y)^2}{x+y}, x \neq -3y$$

$$\mathbf{6.2.31:} \quad \frac{x+5}{x-5} \cdot \frac{2x^2-9x-5}{3x^2+x-2} \cdot \frac{x^2-1}{x^2+7x+10} = \frac{(x-1)(2x+1)}{(3x-2)(x+2)}, x \neq 5, -5, -1$$

In Exercises 37-52, divide and simplify. See Examples 6-8.

$$\mathbf{6.2.37:} \quad \frac{x}{x+2} \div \frac{3}{x+1} = \frac{x(x+1)}{3(x+2)}, x \neq -1$$

$$\mathbf{6.2.41:} \quad \frac{2x}{5} \div \frac{x^2}{15} = \frac{6}{x}$$

$$\mathbf{6.2.47:} \quad \frac{4x}{3x-3} \div \frac{x^2+2x}{x+x-2} = \frac{4}{3}x \neq -2, 1, 0$$

$$\mathbf{6.2.51:} \quad \frac{x^2+2x-15}{x^2+11x+30} \div \frac{x^2-8x+15}{x^2+2x-24} = \frac{x-4}{x-5}, x \neq 6, -5, 3$$

6.2.69: The number of jobs J (in millions) in Florida, and the population P (in millions) of Florida, for the years 2001 through 2006 can be modeled by $J = \frac{-0.696t+8.94}{-0.092t+1}$, $1 \leq t \leq 6$ and $P = 0.352t + 15.97$, $1 \leq t \leq 6$ where t represents the year, with $t = 1$ corresponding to 2001. Find a model Y for the number of jobs per person during these years. $Y = \frac{0.696t+8.94}{(-0.092t+1)(0.352t+15.97)}, 1 \leq t \leq 6$

Section 6.3

In Exercises 1-22, combine and simplify. See Examples 1-3.

$$\mathbf{6.3.1:} \quad \frac{5x}{6} + \frac{4x}{6} = \frac{3x}{2}$$

$$\mathbf{6.3.2:} \quad \frac{7y}{12} + \frac{9y}{12} = \frac{4y}{3}$$

$$\mathbf{6.3.7:} \quad \frac{z^2}{3} + \frac{z^2-2}{3} = \frac{2z^2-2}{3}$$

$$\mathbf{6.3.15:} \quad \frac{w}{w^2-4} + \frac{2}{w^2-4} = \frac{1}{w-2}, w \neq -2$$

$$\mathbf{6.3.17:} \quad \frac{c}{c^2+3c-4} - \frac{1}{c^2+3c-4} = \frac{1}{c+4}, c \neq 1$$

In Exercises 23, 29, 32, find the least common multiple of the expressions. See Example 4.

$$\mathbf{6.3.23:} \quad 5x^2, 20x^3 \rightarrow 20x^3$$

$$\mathbf{6.3.29:} \quad 63z^9z + 1, 14(z + 1)^2$$

$$\mathbf{6.3.32:} \quad 6(x^2 - 4), 2x(x + 2)$$

In Exercises 41, 47, find the least common denominator of the two fractions and rewrite each fraction using the least common denominator.

$$\mathbf{6.3.41:} \quad \frac{n+8}{3n-12}, \frac{10}{6n^2}$$

$$\mathbf{6.3.47:} \quad \frac{x-8}{x^2-25}, \frac{9x}{x^2-10x+25}$$

In Exercises 49-82, combine and simplify. See Examples 5-9.

$$\mathbf{6.3.51:} \quad \frac{7}{a} + \frac{14}{a^2}$$

$$\mathbf{6.3.55:} \quad \frac{20}{x-4} + \frac{20}{4-x}$$

$$\mathbf{6.3.62:} \quad \frac{3}{y-1} + \frac{5}{4y}$$

$$\mathbf{6.3.63:} \quad \frac{x}{x+3} - \frac{5}{x-2}$$

$$\mathbf{6.3.65:} \quad \frac{12}{x^2-9} + \frac{2}{x-3}$$

$$\mathbf{6.3.69:} \quad \frac{4}{x^2} - \frac{4}{x^2+1}$$

$$\mathbf{6.3.71:} \quad \frac{x}{x^2-x-30} - \frac{1}{x+5}$$

$$\mathbf{6.3.77:} \quad \frac{4}{x} - \frac{2}{x^2} + \frac{4}{x+3}$$

Section 6.4

In Exercises 1-22, simplify the complex fraction. See Examples 1-4.

$$\mathbf{6.4.1:} \quad \frac{\left(\frac{3}{16}\right)}{\left(\frac{12}{9}\right)}$$

$$\mathbf{6.4.3:} \quad \frac{\left(\frac{8x^2y}{3z^2}\right)}{\left(\frac{4xy}{9z^5}\right)}$$

$$\mathbf{6.4.5:} \quad \frac{\left(\frac{6x^3}{(5y)^2}\right)}{\left(\frac{(3x)^2}{15y^4}\right)}$$

$$\mathbf{6.4.7:} \quad \frac{\left(\frac{y}{3-y}\right)}{\left(\frac{y^2}{y-3}\right)}$$

$$\mathbf{6.4.10:} \quad \frac{\left(\frac{5x}{x+7}\right)}{\left(\frac{10}{x^2+8x+7}\right)}$$

$$\mathbf{6.4.11:} \quad \frac{\left(\frac{x^2+3x-10}{x+4}\right)}{3x+6}$$

$$\mathbf{6.4.15:} \quad \frac{\left(\frac{6x^2-17x+5}{3x^2+3x}\right)}{\left(\frac{3x-1}{3x+1}\right)}$$

$$\mathbf{6.4.20:} \quad \frac{t^3+t^2-9t-9}{t^2-5t+6} \div \frac{t^2+6t+9}{t-2}$$

In Exercises 25-44, simplify the complex fraction. See Examples 5 and 6.

$$\mathbf{6.4.25:} \quad \frac{\left(\frac{4}{x}+3\right)}{\left(\frac{4}{x}-3\right)}$$

$$\mathbf{6.4.28:} \quad \frac{\left(1-\frac{2}{x}\right)}{\left(\frac{4}{x}\right)}$$

$$\mathbf{6.4.39:} \quad \frac{\left(\frac{10}{x+1}\right)}{\left(\frac{1}{2x+2}+\frac{3}{x+1}\right)}$$

$$\mathbf{6.4.41:} \quad \frac{\left(\frac{1}{x}-\frac{1}{x+1}\right)}{\left(\frac{1}{x+1}\right)}$$

In Exercise 45, simplify the expression. See Example 7.

$$\mathbf{6.4.45:} \quad \frac{2y-y^{-1}}{10-y^{-2}}$$

6.4.55: Determine the average of two real numbers $\frac{x}{5}$ and $\frac{x}{6}$

Section 6.5

In Exercises 1-14, perform the division.

6.5.1: $(7x^3 - 2x^2) \div x$

6.5.4: $(5y^3 + 6y^2 - 3y) \div (-y)$

6.5.5: $(m^4 + 2m^2 - 7) \div m$

6.5.7: $\frac{50z^3+30z}{-5z}$

6.5.10: $\frac{6x^4+8x^3-18x^2}{3x^2}$

In Exercise 15, use the long division algorithm to perform the division. See Example 2.

6.5.15: Divide 1013 by 9.

In Exercises 19-56, perform the division. See Examples 3-6.

6.5.19: $\frac{x^2-8x+15}{x-3}$

6.5.22: $(y^2 - 6y - 16) \div (y + 2)$

6.5.25: $(21 - 4x - x^2) \div (3 - x)$

6.5.27: $\frac{5x^2+2x+3}{x+2}$

6.5.35: $\frac{x^3-2x^2+4x-8}{x-2}$

6.5.41: $\frac{x^2+16}{x+4}$

6.5.49: $(x^3 + 4x^2 + 7x + 7) \div (x^2 + 2x + 3)$

6.5.50: $(2x^3 + 2x^2 - 2x + 15) \div (2x^2 + 4x + 5)$

6.5.52: $(8x^5 + 6x^4 - x^3 + 1) \div (2x^3 - x^2 - 3)$

6.5.53: Divide $x^4 - 1$ by $x - 1$

6.5.54: Divide $x^6 - 1$ by $x - 1$

In Exercises 61-72, use synthetic division to divide. See Example 7.

6.5.61: $(x^2 + x - 6) \div (x - 2)$

6.5.62: $(x^2 + 5x - 6) \div (x + 6)$

6.5.65: $\frac{x^4 - 4x^3 + x + 10}{x - 2}$

6.5.69: $\frac{10x^4 - 50x^3 - 800}{x - 6}$

In Exercises 73, completely factor the polynomial given one of its factors. See Example 8.

6.5.73: $x^3 - x^2 - 14x + 24$