

## ASSIGNMENT 7

DYLAN ZWICK'S MATH

### Section 5.1

In Exercises 1-20, use the rules of exponents to simplify the expression.

**5.1.1:** (a)  $-3x^3 \cdot x^5$  (b)  $(-3x)^2 \cdot x^5$

**5.1.2:** (a)  $5^2 y^4 \cdot y^2$  (b)  $(5y)^2 \cdot y^4$

**5.1.5:** (a)  $(u^3 v)(2v^2)$  (b)  $(-4u^4)(u^5 v)$

**5.1.8:** (a)  $(3y)^3(2y^2)$  (b)  $3y^3 \cdot 2y^2$

**5.1.11:** (a)  $\frac{27m^5 n^6}{9mn^3}$  (b)  $\frac{-18m^3 n^6}{-6mn^3}$

**5.1.13:** (a)  $(\frac{3x}{4y})^2$  (b)  $(\frac{5u}{3v})^3$

**5.1.15:** (a)  $-\frac{(-2x^2 y)^3}{9x^2 y^2}$  (b)  $-\frac{(-2xy^3)^2}{6y^2}$

**5.1.17:** (a)  $[\frac{(-5u^3 v)^2}{10u^2 v}]^2$  (b)  $[\frac{-5(u^3 v)^2}{10u^2 v}]^2$

**5.1.19:** (a)  $\frac{x^{2n+4} y^{4n}}{x^5 y^{2n+1}}$  (b)  $\frac{x^{6n} y^{n-7}}{x^{4n+2} y^5}$

In Exercises 21-50, evaluate the expression.

**5.1.21:**  $5^{-2}$

**5.1.27:**  $\frac{1}{4^{-3}}$

**5.1.30:**  $-\frac{1}{6^{-2}}$

**5.1.38:**  $\frac{5^{-1}}{5^2}$

**5.1.39:**  $\frac{10^3}{10^{-2}}$

**5.1.44:**  $\frac{10^{-5}}{10^{-6}}$

**5.1.50:**  $(32 + 4^{-3})^0$

In Exercises 51-90, rewrite the expression using only positive exponents, and simplify.

**5.1.51:**  $y^4 \cdot y^{-2}$

**5.1.55:**  $7x^{-4}$

**5.1.63:**  $\frac{(4t)^0}{t^{-2}}$

**5.1.67:**  $(-3x^{-3}y^2)(4x^2y^{-5})$

**5.1.69:**  $(3x^2y^{-2})^{-2}$

**5.1.73:**  $\frac{6x^3y^{-3}}{12x^{-2}y}$

**5.1.75:**  $\left(\frac{3u^2v^{-1}}{3^3u^{-1}v^3}\right)^{-2}$

**5.1.78:**  $\left(\frac{a^{-3}}{b^{-3}}\right)\left(\frac{a}{b}\right)^3$

**5.1.80:**  $(ab)^{-2}(a^2b^2)^{-1}$

**5.1.87:**  $(u + v^{-2})^{-1}$

**5.1.90:**  $\frac{u^{-1}-v^{-1}}{u^{-1}+v^{-1}}$

In Exercise 91, evaluate the expression when  $x = -3$ ,  $y = -4$

**5.1.91:**  $x^2 \cdot x^{-3} \cdot x \cdot y$

In Exercises 101-114, write the number in scientific notation.

**5.1.101:** 3,600,000

**5.1.105:** 0.00031

**5.1.108:** 0.0000000000692

In Exercise 115, write the number in decimal notation.

**5.1.115:**  $7.2 \times 10^8$

In Exercise 133, evaluate the expression

**5.1.133:**  $\frac{64,000,000}{0.00004}$

**5.1.144:** A study by Australian astronomers estimated the number of stars within range of modern telescopes to be 70,000,000,000,000,000,000. Write this number in scientific notation.

**5.1.145:** A cube of copper with an edge of 1 centimeter has approximately  $8.483 \times 10^{22}$  free electrons. Write this real number in decimal notation.

**5.1.151:** In 2005, the resident population of the United States was about 296 million people, and it would have cost each resident about \$26,600 to pay off the federal debt. Use these two numbers to approximate the federal debt in 2005.

## Section 5.2

In Exercises 1-12, write the polynomial in standard form, and find its degree and leading coefficient.

**5.2.1:**  $4y + 16$

**5.2.3:**  $2x + x^2 - 6$

**5.2.7:**  $4 - 14t^4 + t^5 - 20t$

**5.2.11:**  $v_0t - 16t^2$  ( $v_0$  is constant.)

In Exercises 13-18, determine whether the polynomial is a monomial, a binomial, or a trinomial.

**5.2.13:**  $12 - 5y^2$

**5.2.15:**  $x^3 + 2x^2 - 4$

**5.2.16:**  $t^3$

In Exercises 19-22, give an example of a polynomial in  $x$  that satisfies the conditions.

**5.2.19:** A monomial of degree 2

**5.2.22:** A monomial of degree 0

In Exercises 23-26, state why the expression is not a polynomial.

**5.2.23:**  $y^{-3} - 2$

**5.2.1:**  $6 - \sqrt{n}$

In Exercises 27-42, use a horizontal format to find the sum.

**5.2.29:**  $(2x^2 - 3) + (5x^2 + 6)$

**5.2.31:**  $(5y + 6) + (4y^2 - 6y - 3)$

**5.2.34:**  $(z^3 + 6z - 2) + (3z^2 - 6z)$

**5.2.40:**  $(2 - \frac{1}{4}y^2 + y^4) + (\frac{1}{3}y^4 + 7x - \frac{1}{2}x^3)$

In Exercises 43-50, use a vertical format to find the sum.

**5.2.43:**

|                            |      |
|----------------------------|------|
| $5x^2 - 3x$                | $+4$ |
| $-3x^2$                    | $4$  |
| <hr style="width: 100%;"/> |      |

**5.2.47:**  $(5p^2 - 4p + 2) + (-3p^2 + 2p - 7)$

**5.2.53:**  $(3x^2 - 2x + 1) - (2x^2 + x - 1)$

**5.2.61:** Subtract  $3x^3 - (x^2 + 5x)$  from  $x^3 - 3x$

$$\begin{array}{r} x^2 - \phantom{0000} x + 3 \\ -( \phantom{0000} x - 2 ) \end{array}$$

**5.3.3:**  $2y(5 - y)$

**5.3.5:**  $4x(2x^2 - 3x + 5)$

**5.3.7:**  $-2m^2(7 - 4m + 2m^2)$

**5.3.10:**  $-y^4(7y^3 - 4y^2 + y - 4)$

**5.3.12:**  $-7t(2t)(6 - 3t)$

In Exercises 15-32, multiply using the FOIL Method.

**5.3.15:**  $(x + 2)(x + 4)$

**5.3.17:**  $(x - 4)(x + 4)$

**5.3.20:**  $(x - 6)(x + 6)$

**5.3.23:**  $(5x - 2)(2x - 6)$

**5.3.24:**  $(4x + 7)(3x + 7)$

**5.3.28:**  $(3z - \frac{3}{4})(4z - 8)$

**5.3.30:**  $(2x - y)(3x - 2y)$

In Exercises 33, 41, use a horizontal format to find the product.

**5.3.33:**  $(x - 1)(x^2 - 4x + 6)$

**5.3.41:**  $(5x^2 + 2)(x^2 + 4x - 1)$

In Exercises 45, 50 , use a vertical format to find the product.

**5.3.45:**

$$\begin{array}{r} 7x^2 - \phantom{00} \\ \times \phantom{00} 14x + 9 \\ \hline \end{array}$$

**5.3.50:**  $(2s^2 - 5s + 6)(3s - 4)$

In Exercises 53-82, use a special product formula to find the product.

**5.3.53:**  $(x + 2)(x - 2)$

**5.3.61:**  $(2a + 5b)(2a - 5b)$

**5.3.69:**  $(x + 5)^2$

**5.3.100:** A closed rectangular box has sides of lengths  $2n - 2$ ,  $2n + 2$ ,  $2n$  inches.

(a) Write a polynomial function  $V(n)$  that represents the volume of the box.

(b) What is the volume if the length of the shortest side is 4 inches?

(c) Write a polynomial function  $A(n)$  that represents the area of the base of the box.

(d) Write a polynomial function for the area of the base if the length and width increase by 3. Show that the area of the base is not  $A(n + 4)$ .