

Solutions

Assignment 10

Math 1030

Due Monday, November 26th

1. Perimeters and Area

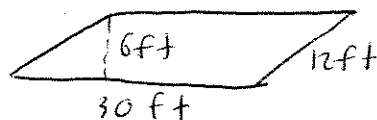
Find the perimeter and area of each of the following shapes.

- (a) A rectangular postage stamp with a length of 2.2 centimeters and a width of 2.0 centimeters.

$$\text{Perimeter} = 2 \times 2.2 \text{ cm} + 2 \times 2.0 \text{ cm} = \boxed{8.4 \text{ cm}}$$

$$\text{Area} = 2.2 \text{ cm} \times 2.0 \text{ cm} = \boxed{4.4 \text{ cm}^2}$$

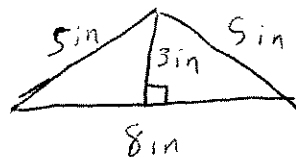
- (b) A parallelogram with sides of length 12 feet and 30 feet, and a distance between ~~the~~ 30-foot sides of 6 feet.



$$\begin{aligned} \text{Perimeter} &= 2 \times 30 \text{ ft} + 2 \times 12 \text{ ft} \\ &= \boxed{84 \text{ ft}} \end{aligned}$$

$$\text{Area} = 30 \text{ ft} \times 6 \text{ ft} = \boxed{180 \text{ ft}^2}$$

- (c) The triangle:



$$\text{Perimeter} = 5 \text{ in} + 5 \text{ in} + 8 \text{ in} = \boxed{18 \text{ in}}$$

$$\text{Area} = \frac{1}{2} (8 \text{ in}) (3 \text{ in}) = \boxed{12 \text{ in}^2}$$

2. Three Dimensional Objects

- (a) An arena has a ~~floor~~^{floor} that measures 30 meters by 40 meters, with a ceiling 8 meters high. How much air does it hold, in cubic meters? In liters?

$$\text{Volume} = 30\text{m} \times 40\text{m} \times 8\text{m} = \boxed{9,600\text{ m}^3}$$

$$\text{In liters} = (9,600\text{ m}^3) \left(\frac{1,000\text{ L}}{1\text{ m}^3} \right) = \boxed{9,600,000\text{ L}}$$

- (b) A soccer ball has a circumference of 69 centimeters. What are its volume and surface area?

$$r = \frac{C}{2\pi} = \frac{69\text{ cm}}{2\pi}$$

$$\text{Surface Area} = 4\pi r^2 = 4\pi \left(\frac{69\text{ cm}}{2\pi} \right)^2 \approx \boxed{6,062\text{ cm}^2}$$

$$\text{Volume} = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi \left(\frac{69\text{ cm}}{2\pi} \right)^3 = \boxed{5,547\text{ cm}^3}$$

- (c) Which holds more: an oil drum with a radius of 2 feet that is 3 feet high or an oil drum with a radius of 1.5 feet that is 4 feet high?

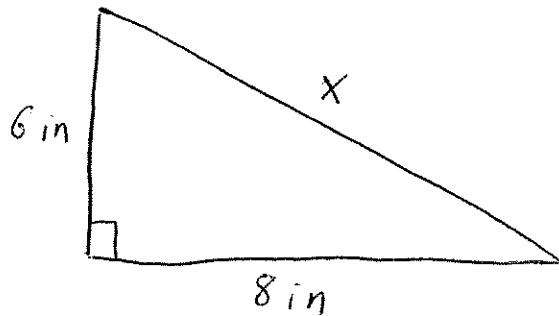
$$\text{Volume Oil drum \#1} = 3\text{ft} \times \pi (2\text{ft})^2 = 12\pi\text{ ft}^3$$

$$\text{Volume Oil drum \#2} = 4\text{ft} \times \pi (1.5\text{ft})^2 = 9\pi\text{ ft}^3$$

$$\text{So, } \boxed{\text{Oil drum \#1}}$$

3. Geometric Problem Solving

(a) What is the distance x in the right triangle below:



$$x = \sqrt{(6\text{ in})^2 + (8\text{ in})^2} = \sqrt{100\text{ in}^2} = \boxed{10\text{ in}}$$

(b) What is the angular size of a quarter viewed from a distance of 5 yards? Use 2.5 cm as the diameter of the quarter.

$$\begin{aligned} \text{Angular size} &= \frac{2.5\text{ cm}}{2\pi(5\text{ yards})} = \frac{2.5\text{ cm}}{2\pi(5\text{ yd})(91.44\text{ cm/yd})} \\ &= \boxed{8.703 \times 10^{-4}\text{ rad}} \end{aligned}$$

$$1\text{ yard} = 91.44\text{ cm}$$

Or

$$8.703 \times 10^{-4}\text{ rad} \left(\frac{360^\circ}{2\pi\text{ rad}} \right)$$

3

$$= \boxed{.05^\circ}$$