

MATLAB Project 1, Math 2280, Due Sept 28

1. These exercises will get you started on using MATLAB to answer some questions regarding basic mathematical operations.

(a) Use the function `plot` to plot the function $y = e^{-x/2} \sin(\pi x)$, $-1 \leq x \leq 5$, using a resolution that the curve looks sufficiently smooth to your eyes. Look up the help menu to learn about the calls to `axis`, `xlabel`, `ylabel`, and `title` to annotate the graph.

(b) Enter the symbolic environment by specifying needed variables, for example

```
>> syms x y
```

will define two symbolic variables x and y . Use the function `solve` to find the roots of $2x^2 - x - 1 = 0$, and `int` to find $\int \frac{1}{1+x^2} dx$.

(c) Familiarize yourself with the concept of loop by writing a short program to obtain the sum

$$\sum_{n=1}^N \frac{(-1)^{n+1}}{n} \sin(nx)$$

at $x = \pi/4$ and $7\pi/8$, with $N = 10$ and 100 .

(d) Read the manual entries for `input` and `fprintf` to understand the syntax, print the results in part (c) in a table with sufficient explanations.

2. Write a MATLAB function that implements the Runge-Kutta method to solve an initial value problem for $y' = f(x, y)$, with the function $f(x, y)$ and the initial conditions to be supplied in separate functions (similar to `frhs.m`). Use your own implementation to solve the following initial value problems

(a)

$$y' = \cos x + \sin(2y); \quad y(0) = 0, \quad 0 < x \leq 2$$

(b)

$$\frac{dv}{dt} = -(0.04)v - 9.8, \quad v(0) = 49, \quad 0 < t \leq 5$$

with step sizes $h = 0.5, 0.2$ and 0.1 .