

A)

$$2^{-1} = \frac{1}{2}$$

$$5^{-1} = \frac{1}{5}$$

$$10^{-1} = \frac{1}{10}$$

$$\pi^{-1} = \frac{1}{\pi}$$

$$\sqrt{2}^{-1} = \frac{1}{\sqrt{2}}$$

$$6^{-1} = \frac{1}{6}$$

D)

$$4^{\frac{1}{2}} = 2$$

$$9^{\frac{1}{2}} = 3$$

$$16^{\frac{1}{2}} = 4$$

$$25^{\frac{1}{2}} = 5$$

$$8^{\frac{1}{3}} = 2$$

$$27^{\frac{1}{3}} = 3$$

$$64^{\frac{1}{3}} = 4$$

$$125^{\frac{1}{3}} = 5$$

B)

$$\left(\frac{1}{3}\right)^{-1} = 3$$

$$\left(\frac{1}{5}\right)^{-1} = 5$$

$$\left(\frac{1}{8}\right)^{-1} = 8$$

$$\left(\frac{1}{9}\right)^{-1} = 9$$

E)

$$8^{\frac{2}{3}} = 4$$

$$16^{\frac{3}{2}} = 64$$

$$16^{\frac{3}{4}} = 8$$

$$125^{\frac{2}{3}} = 25$$

F)

$$\left(\frac{4}{9}\right)^{-\frac{3}{2}} = \frac{27}{8}$$

$$8^{-\frac{2}{3}} = \frac{1}{4}$$

$$\left(\frac{1}{16}\right)^{-\frac{3}{2}} = 64$$

$$\left(\frac{125}{27}\right)^{-\frac{2}{3}} = \frac{9}{25}$$

$$\left(\frac{16}{25}\right)^{-\frac{3}{2}} = \frac{125}{64}$$

C)

$$\left(\frac{2}{5}\right)^{-1} = \frac{5}{2}$$

$$\left(\frac{3}{2}\right)^{-1} = \frac{2}{3}$$

$$\left(\frac{2}{17}\right)^{-1} = \frac{17}{2}$$

$$\left(\frac{5}{8}\right)^{-1} = \frac{8}{5}$$

$\log_2(1) = 0$   
 $\log_2(2) = 1$   
 $\log_2(4) = 2$   
 $\log_2(8) = 3$   
 $\log_2(16) = 4$   
 $\log_2(32) = 5$

$\log_2\left(\frac{1}{2}\right) = -1$   
 $\log_2\left(\frac{1}{4}\right) = -2$   
 $\log_2\left(\frac{1}{8}\right) = -3$   
 $\log_2\left(\frac{1}{16}\right) = -4$

$\log_2(\sqrt[2]{2}) = \frac{1}{2}$   
 $\log_2(\sqrt[3]{2}) = \frac{1}{3}$   
 $\log_2(\sqrt[4]{2}) = \frac{1}{4}$

$\log_2(\sqrt[3]{4}) = \frac{2}{3}$   
 $\log_2(\sqrt[4]{8}) = \frac{3}{4}$   
 $\log_2(\sqrt[5]{16}) = \frac{4}{5}$

$\log_2\left(\frac{1}{\sqrt[4]{32}}\right) = -\frac{5}{4}$   
 $\log_2\left(\sqrt[3]{\frac{1}{16}}\right) = -\frac{4}{3}$   
 $\log_2\left(\sqrt{\frac{1}{8}}\right) = -\frac{3}{2}$   
 $\log_3\left(\frac{1}{\sqrt[4]{81}}\right) = -\frac{4}{7}$   
 $\log_5(\sqrt[3]{125}) = \frac{3}{2}$

$\log_{10}\left(\frac{1}{1000}\right), \log_{10}\left(\frac{1}{100}\right), \log_{10}\left(\frac{1}{10}\right), \log_{10}(1), \log_{10}(10), \log_{10}(100), \log_{10}(1,000)$   
 $-3 \quad -2 \quad -1 \quad 0 \quad 1 \quad 2 \quad 3$

$\log_{10}(10^n) = n$

Erase the "last" algebra on the left side of the equation by applying its inverse to the right side.

$$x-2 = e^{16}$$
$$x = e^{16} + 2$$

$$x+3 = \log_3(14)$$
$$x = \log_3(14) - 3$$

$$5x = e^2 - 7$$
$$x = \frac{e^2 - 7}{5}$$

$$\frac{x}{7} = \log_e(3) + 2$$
$$x = 7(\log_e(3) + 2)$$

$$e^x = e^2 - 3$$
$$x = \log_e(e^2 - 3)$$

$$\log_e(x) = 7e^2$$
$$x = e^{7e^2}$$

$$e^x - 4 = 27$$
$$e^x = 31$$

$$\log_e(x) + 2 = e^6 - 1$$
$$\log_e(x) = e^6 - 3$$

$$\frac{e^x}{6} = \log_e(3) - 5$$
$$e^x = 6(\log_e(3) - 5)$$

$$7\log_e(x) = 14$$
$$\log_e(x) = 2$$

$$e^{x+2} = 17$$
$$x+2 = \log_e(17)$$
$$\log_e(4x) = e^2 + 3$$
$$4x = e^{e^2 + 3}$$

$$e^{x+2} - 7 = 5$$
$$e^{x+2} = 12$$

$$2\log_e(5x) = e + 7$$
$$\log_e(5x) = \frac{e+7}{2}$$

$$e^{3x^2 - 17x + 2} - 4 = e^3$$
$$e^{3x^2 - 17x + 2} = e^3 + 4$$

$$2\log_e(5x-7) = e^2 + 1$$
$$\log_e(5x-7) = \frac{e^2 + 1}{2}$$

$$5e^{17x-4} + 2 = 8\log_3(25) - 1$$
$$5e^{17x-4} = 8\log_3(25) - 3$$

$$2\log_e(5-4x) + 17 = 3 - e^{16}$$
$$2\log_e(5-4x) = -14 - e^{16}$$

$$8e^{x+2} = 6$$
$$e^{x+2} = \frac{3}{4}$$

Complete the following rules for log/exp ( $a > 0, a \neq 1$ )

$$a^x a^y = a^{x+y}$$

$$\frac{a^x}{a^y} = a^{x-y}$$

$$(a^x)^y = a^{xy}$$

$$a^0 = 1$$

$$\log_a(z) + \log_a(w) = \log_a(zw)$$

$$\log_a(z) - \log_a(w) = \log_a\left(\frac{z}{w}\right)$$

$$z \log_a(w) = \log_a(w^z)$$

$$\log_a(1) = 0$$

$$\log_a(a^x) = x$$

$$a^{\log_a(x)} = x$$

$$a^{-x} = \frac{1}{a^x}$$

$$\text{If } n, m \in \mathbb{N}, \quad a^{\frac{n}{m}} = \sqrt[m]{a^n} = \left(\sqrt[m]{a}\right)^n$$