

MATH 1220-6
Fall 2003
Midterm exam III

Student Name: _____

Student ID Number: _____

Course Abbreviation and Number:	<i>Math 1220</i>
Course Title:	<i>Calculus II</i>
Instructor:	<i>Vladimir Vinogradov</i>

Date of Exam:	<i>November 20, 2003</i>
Time Period:	<i>Start time: 7:00 pm End Time: 8:00 pm</i>
Duration of Exam:	<i>1 hours</i>
Number of Exam Pages:	<i>10</i>
<i>(including this cover sheet)</i>	
Exam Type:	<i>Closed Book</i>
Additional Materials Allowed:	<i>Calculator</i>

QUESTION	VALUE	SCORE
1	20	
2	20	
3	20	
4	20	
5	20	
TOTAL	100	

1. (20 points) Does the series converge or diverge? Give reasons.

a) $\sum_{n=1}^{\infty} \frac{n!}{e^n}$

ANSWER: _____

$$\text{b) } \sum_{m=1}^{\infty} (-1)^m \frac{e^{\sin(m\pi)}}{m^2}$$

ANSWER: _____

2. (20 points) Use the Integral Test to decide the convergence or divergence of the following series:

$$\sum_{n=1}^{\infty} k e^{-\frac{k^2}{2}}.$$

ANSWER: _____

3. (20 points) Find the sum of

$$\sum_{n=0}^{\infty} (n+1) \frac{2^n}{3^n}.$$

ANSWER: _____

4. (20 points) What is the interval of convergence of the power series? Show your work.

a) $\sum_{k=1}^{\infty} \frac{(3x+1)^k}{k 2^k}$

ANSWER: _____

$$\text{b) } \sum_{k=1}^{\infty} \frac{(-1)^k (x-2)^k}{k^2}$$

ANSWER: _____

5. (20 points) Find the Maclaurin series for the function.

a) $f(x) = e^{2x} - 1 - 2x$

ANSWER: _____

b) $g(x) = \frac{1}{2 + 3x}$

ANSWER: _____

Useful formulae

$$\begin{aligned}\log_a x &= \frac{\ln x}{\ln a}, & a^x &= e^{x \ln a}, \\ \log_a x^n &= n \log_a x, & a^b a^c &= a^{b+c}, \\ (x^\alpha)' &= \alpha x^{\alpha-1}, & (a^x)' &= a^x \ln a, \\ (\ln x)' &= \frac{1}{x}, & \int \ln x dx &= x \ln x - x + C\end{aligned}$$

$$e^x = \sum_{k=0}^{\infty} \frac{x^k}{k!} = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!}$$

$$(1+x)^p = 1 + \sum_{k=1}^{\infty} \binom{p}{k} x^k \quad |x| < 1,$$

where $\binom{p}{k} = \frac{p(p-1)(p-2)(p-3)\dots(p-k+1)}{k!}$

$$\frac{1}{1-x} = \sum_{k=0}^{\infty} x^k = 1 + x + x^2 + x^3 \dots \quad |x| < 1$$

$$\frac{x}{1-x} = \sum_{k=1}^{\infty} x^k = x + x^2 + x^3 + x^4 \dots \quad |x| < 1$$

$$\ln(1+x) = \sum_{k=1}^{\infty} (-1)^{k+1} \frac{x^k}{k} = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} \dots \quad |x| < 1$$