

Final Exam Review

Math 1100-005

Topics to Study

Limits & Continuity

- take limits, algebraically and graphically, including one-sided limits
- take limits as $x \rightarrow \infty$ and $x \rightarrow -\infty$ (ie. horizontal asymptotes)

Derivatives

- find the equation for the slope of a tangent line
- state and use the definition of a derivative
- find derivatives of algebraic, exponential & log functions both explicitly & implicitly
- find average, instantaneous and marginal rates of change

First Derivative Test & Extrema

- find critical points, inc/dec intervals, relative AND absolute extrema

Second Derivative Test

- find inflection points & concavity
- use the 2nd derivative test to find relative extrema

Optimization

- maximize/minimize functions & solve optimization problems
- find elasticity AND regions that are elastic/inelastic

Asymptotes & Sketching

- find both vertical and horizontal asymptotes
- sketch a graph if given or by finding
 - intercepts, inc/dec intervals, extrema, concavity, & asymptotes

Integrals

- compute definite & indefinite integrals
- find business functions if given their marginals (ie. cost, revenue, profit, price)
- find average value, annuities, present value, etc. using integrals
- find the area under curve or between 2 curves (including the applications)

How to Study

- REDO all previous reviews
- REDO all previous exams
- REDO all worksheets
- DO the following review

Equations TO KNOW!

$$f'(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x} \quad (\text{Definition of Derivative})$$

$$\frac{\Delta y}{\Delta x} = \frac{f(b) - f(a)}{b - a} \quad (\text{Average Rate of Change})$$

$$\text{Profit} = \text{Total Revenue} - \text{Total Cost}$$

$$\text{Revenue} = \text{price} * \text{quantity}$$

$$\text{Total Cost} = \text{Fixed Costs} + \text{Variable Costs}$$

$$\text{Average Cost} = \frac{\text{Cost}}{\text{quantity}}$$

$$\eta = \frac{\text{change in demand}}{\text{change in price}} = \frac{p/x}{dp/dx} \quad (\text{Price Elasticity of Demand})$$

$$\text{Average Value of } f \text{ on } [a, b] = \frac{1}{b - a} \int_a^b f(x) dx$$

$$\text{Consumer Surplus} = \int_0^{x_o} [\text{demand} - p_o] dx$$

$$\text{Producer Surplus} = \int_0^{x_o} [p_o - \text{supply}] dx$$

$$\text{Profit over } T \text{ years} = \int_0^T [R(t) - C(t)] dt$$

Equations GIVEN

$$\text{Perimeter} = \text{add up lengths of all sides}$$

$$\text{Area} = \text{length} \cdot \text{width}$$

$$\text{Volume} = \text{length} \cdot \text{width} \cdot \text{height}$$

$$\text{Surface Area of Rectangle} = \text{add up areas of all sides}$$

$$\text{Distance between } (x_1, y_1) \text{ and } (x_2, y_2) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\text{Area of Circle} = \pi r^2$$

$$\text{Circumference of Circle} = 2\pi r$$

$$\text{Volume of Sphere} = \frac{4}{3}\pi r^3$$

$$\text{Surface Area of Sphere} = 4\pi r^2$$

$$\text{Volume of Cylinder} = \pi r^2 h$$

$$\text{Surface Area of Cylinder} = 2\pi r h + 2\pi r^2$$

$$\text{Amount of Annuity} = e^{rT} \int_0^T c(t) e^{-rt} dt$$

$$\text{Actual Income over T years} = \int_0^T c(t) dt$$

$$\text{Present Value} = \int_0^T c(t) e^{-rt} dt$$

Review Problems for material not covered on previous exams - DON'T ONLY study these!!

1. Evaluate the following integrals:

(a) $\int_0^2 x^2 \sqrt{x^3 + 1} dx$

(b) $\int_{-2}^2 x^2 - 3x - 1 dx$

(c) $\int_1^5 x(x + 3)^2 dx$

(d) $\int \ln(x - 2) dx$

(e) $\int x^2 \ln(x) dx$

(f) $\int_0^2 (x - 1)e^{-x} dx$

2. Find the area of the regions bounded by the curves

(a) $y = x^2 + 3$, $y = x$, $x = -1$, and $x = 1$

(b) $y = 2 - x$, $y = \sqrt{x}$, $x = 0$

3. Find the average value of $f(x) = \frac{x}{2x^2-1}$ on the interval $[1, 3]$.

4. Find the amount of an annuity if the income is given by $c(t) = 3000$ with interest rate 5% for 10 years.

5. Find the producer and consumer surplus if the demand is given by $p_1(x) = 100 - 0.4x^2$ and the supply is given by $p_2(x) = 42x$.

6. Find the present value over 5 years of an income given by $c(t) = 500 + t$ with an annual inflation rate of 3%.