

## EXTRA CREDIT #2 – MATH 311W

SEPTEMBER 28TH, 2012

Suppose  $a, b \in \mathbb{Z}$  and  $n \in \mathbb{Z}_{>0}$ . We know we can write

$$ra + sb = \gcd(a, b).$$

What can you say about  $r, s$ . In particular, find all the  $r$  and  $s$  that work.

A complete answer is not necessary to receive partial credit. You can explore some special cases. For example, you could explore  $a = 7, b = 10$ . Alternately, you could explore  $a = 3$  while  $b$  is anything. Or you could explore  $a = n$  and  $b = n + 1$  (or whatever strikes your fancy).

You can get some credit just for identifying patterns, or you can more credit for proving that the patterns you identify are correct.

This is worth 6 points to your homework score, of those 4 of those are for the mathematics, 2 are for the write-up. Please consider typing up your work on this.