

1. Let  $X_1$  and  $X_2$  be two independent random variables.  $X_1$  is normal  $N(1, 1)$  and  $X_2$  is normal  $N(0, 2)$ . Find  $c$  such that

$$P\{X_1 - 2X_2 \leq c\} = .1$$

using one of the tables in your book.

$$X_1 - 2X_2 \sim N(1, 1 + 4(2)) \sim N(1, 3^2)$$

$$.1 = P(X_1 - 2X_2 \leq c) = P\left(\frac{X_1 - 2X_2 - 1}{3} \leq \frac{c - 1}{3}\right)$$

$$\Rightarrow \frac{c - 1}{3} = z_{.10} \in (-1.29, -1.28)$$

$$\Rightarrow c \in (1 - 3(1.29), 1 - 3(1.28))$$