

1. Let  $X_1, X_2, X_3$  be independent identically distributed normal  $N(0, 6)$  random variables.  
Find  $c$  such that

$$P\{X_1^2 + X_2^2 + X_3^2 \leq c\} = .95$$

using one of the enclosed tables.

$$.95 = P\left(\left(\frac{X_1}{\sqrt{6}}\right)^2 + \left(\frac{X_2}{\sqrt{6}}\right)^2 + \left(\frac{X_3}{\sqrt{6}}\right)^2 \leq \frac{c}{6}\right)$$

$$\Rightarrow \frac{c}{6} = \chi_{.95}^2(3) = 7.8$$

$$\Rightarrow c = 7.8(6) = 46.8$$