

1. Let  $X$  be a random variable with density function

$$f(x) = \begin{cases} 2x & \text{if } x \in (0, 1) \\ 0 & \text{if } x \notin (0, 1). \end{cases}$$

Compute the moment generating function of  $X$  and the moment generating function of  $2X$ .