

1. Let  $X_1, X_2$  and  $X_3$  be three independent random variables.  $X_1$  is  $\chi^2(3)$  and  $X_2$  is  $\chi^2(2)$  and  $X_3$  is  $\chi^2(2)$ . Determine  $c$  such that

$$P\left\{ \frac{X_1}{X_2 + X_3} \leq c \right\} = .9$$

using one of the enclosed tables.

2. Let  $X_1, X_2, \dots, X_n$  be independent identically distributed random variables with density function

$$g(t, \theta) = \begin{cases} 0, & \text{if } t \notin [0, \theta] \\ \frac{2}{\theta^2}t, & \text{if } t \in [0, \theta]. \end{cases}$$

Find a moment estimator for  $\theta$ .

3. Let  $X_1, X_2, \dots, X_n$  be independent identically distributed random variables with density function

$$h(t; \theta) = \begin{cases} 0, & \text{if } t \notin [0, 1] \\ \theta t^{\theta-1}, & \text{if } t \in [0, 1]. \end{cases}$$

Find the maximum likelihood estimator for  $\theta$ .

4. Let  $X$  be a random variable with density function

$$f(t, \theta) = \frac{1}{(2\pi\theta)^{1/2}} e^{-t^2/(2\theta)}.$$

Compute the Cramer-Rao lower bound.

5. Let  $X_1, X_2, \dots, X_n$  be independent identically distributed random variables with density function

$$g(t, \theta) = \begin{cases} 0, & \text{if } -\infty < t < \theta \\ e^{-(t-\theta)}, & \text{if } \theta \leq t < \infty \end{cases}$$

Find the uniformly minimum variance estimator for  $\theta$  (justify your answer).