

## MATH 5010 – Quiz 4

Name:

Date:

**2.9** A retail establishment accepts American express and VISA credit cards. A total of 24 percent of its customers carry an American Express card, 61 percent carry a VISA card, and 11 percent carry both cards.

1. A customer is selected at random. What is the probability that this customer carries a credit card that the establishment will accept?

$$.24 + .61 - .11$$

$$= \boxed{.74}$$

2. Prove that  $P(\{\}) = 0$  using only the axioms.

$$\text{Let } E_1 = S$$

$$E_i = \emptyset \text{ for } i = 2, 3, \dots$$

$$\text{Then } 1 = P(S) = P(\cup E_i) = \sum P(E_i) = P(S) + \sum_{i=2}^{\infty} P(E_i)$$

$$= 1 + \sum_{i=2}^{\infty} P(\emptyset)$$

$$\Rightarrow P(\emptyset) = 0 \text{ since } P(\emptyset) \geq 0 \text{ and } \sum P(\emptyset) = 0$$