

University of Utah  
Math 1090, Fall 2009  
Name:

Key

Quiz # 2

Time: 10 minutes

Show all work. Check your answers.

Solve the following system of equations:

$$\begin{cases} \textcircled{1} & x + 2y + z = 2 \\ \textcircled{2} & 2x - 2y + z = 5 \\ \textcircled{3} & 3x - 4y - 2z = 1 \end{cases}$$

We proceed by Left-to-Right Elimination:

Step 1: Replace line  $\textcircled{2}$  by  $\textcircled{2} - 2 \times \textcircled{1}$ :  $-6y - z = 1$

Replace line  $\textcircled{3}$  by  $\textcircled{3} - 3 \times \textcircled{1}$ :  $-10y - 5z = -5$   
(or better:  $2y + z = 1$ )

The system becomes

$$\begin{cases} \textcircled{1} & x + 2y + z = 2 \\ \textcircled{2} & -6y - z = 1 \\ \textcircled{3} & 2y + z = 1 \end{cases}$$

Step 2: Replace line  $\textcircled{3}$  by  $\textcircled{3} + \frac{1}{3} \times \textcircled{2}$ :  $\frac{2}{3}z = \frac{4}{3} \rightarrow \boxed{z = 2}$

then backsubstitute  $-6y - z = 1 \rightarrow \boxed{y = -\frac{1}{2}}$

$$x + 2y + z = 2 \rightarrow \boxed{x = 1}$$

Then check these values by plugging them into the original 3 equations

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