

### Basic Identities

$$\begin{aligned} \tan t &= \frac{\sin t}{\cos t} & \cot t &= \frac{\cos t}{\sin t} \\ \sec t &= \frac{1}{\cos t} & \csc t &= \frac{1}{\sin t} \\ 1 + \tan^2 t &= \sec^2 t & 1 + \cot^2 t &= \csc^2 t \end{aligned}$$

### Cofunction Identities

$$\sin\left(\frac{\pi}{2} - t\right) = \cos t \quad \cos\left(\frac{\pi}{2} - t\right) = \sin t \quad \tan\left(\frac{\pi}{2} - t\right) = \cot t$$

### Odd-even Identities

$$\sin(-t) = -\sin t \quad \cos(-t) = \cos t \quad \tan(-t) = -\tan t$$

### Addition Formulas

$$\begin{aligned} \sin(s+t) &= \sin s \cos t + \cos s \sin t & \sin(s-t) &= \sin s \cos t - \cos s \sin t \\ \cos(s+t) &= \cos s \cos t - \sin s \sin t & \cos(s-t) &= \cos s \cos t + \sin s \sin t \\ \tan(s+t) &= \frac{\tan s + \tan t}{1 - \tan s \tan t} & \tan(s-t) &= \frac{\tan s - \tan t}{1 + \tan s \tan t} \end{aligned}$$

### Double Angle Formulas

$$\begin{aligned} \sin 2t &= 2 \sin t \cos t & \tan 2t &= \frac{2 \tan t}{1 - \tan^2 t} \\ \cos 2t &= \cos^2 t - \sin^2 t = 1 - 2 \sin^2 t = 2 \cos^2 t - 1 \end{aligned}$$

### Half Angle Formulas

$$\sin \frac{t}{2} = \pm \sqrt{\frac{1 - \cos t}{2}} \quad \cos \frac{t}{2} = \pm \sqrt{\frac{1 + \cos t}{2}} \quad \tan \frac{t}{2} = \frac{1 - \cos t}{\sin t}$$

### Product Formulas

$$\begin{aligned} 2 \sin s \cos t &= \sin(s+t) + \sin(s-t) & 2 \cos s \cos t &= \cos(s+t) + \cos(s-t) \\ 2 \cos s \sin t &= \sin(s+t) - \sin(s-t) & 2 \sin s \sin t &= \cos(s-t) - \cos(s+t) \end{aligned}$$

### Factoring Formulas

$$\begin{aligned} \sin s + \sin t &= 2 \cos \frac{s-t}{2} \sin \frac{s+t}{2} & \cos s + \cos t &= 2 \cos \frac{s+t}{2} \cos \frac{s-t}{2} \\ \sin s - \sin t &= 2 \cos \frac{s+t}{2} \sin \frac{s-t}{2} & \cos s - \cos t &= -2 \sin \frac{s+t}{2} \sin \frac{s-t}{2} \end{aligned}$$

### Laws of Sines and Cosines



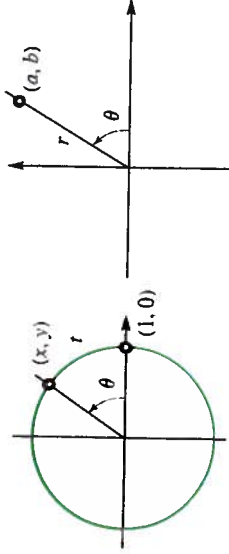
$$\frac{\sin \alpha}{a} = \frac{\sin \beta}{b} = \frac{\sin \gamma}{c}$$

$$a^2 = b^2 + c^2 - 2bc \cos \alpha$$

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here

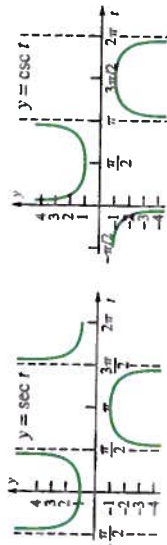
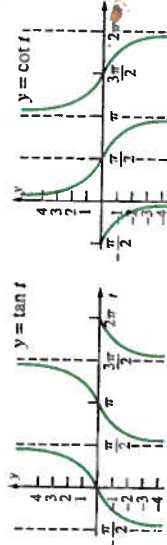
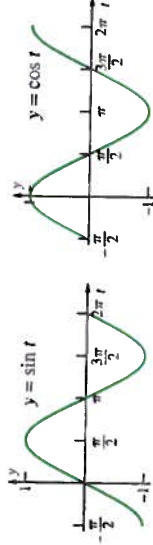
### TRIGONOMETRY



$$\sin t = \sin \theta = \frac{y}{r} = \frac{a}{r} \quad \cos t = \cos \theta = \frac{x}{r} = \frac{a}{r}$$

$$\tan t = \tan \theta = \frac{y}{x} = \frac{b}{a} \quad \cot t = \cot \theta = \frac{x}{y} = \frac{a}{b}$$

### Graphs



### Inverse Trigonometric Functions

$$\begin{aligned} y &= \sin^{-1} x \Leftrightarrow x = \sin y, -\pi/2 \leq y \leq \pi/2 \\ y &= \cos^{-1} x \Leftrightarrow x = \cos y, 0 \leq y \leq \pi \\ y &= \tan^{-1} x \Leftrightarrow x = \tan y, -\pi/2 < y < \pi/2 \\ y &= \sec^{-1} x \Leftrightarrow x = \sec y, 0 \leq y \leq \pi, y \neq \pi/2 \\ &\quad \sec^{-1} x = \cos^{-1}(1/x) \end{aligned}$$

### Hyperbolic Functions

$$\begin{aligned} \sinh x &= \frac{1}{2}(e^x - e^{-x}) & \cosh x &= \frac{1}{2}(e^x + e^{-x}) \\ \tanh x &= \frac{\sinh x}{\cosh x} & \coth x &= \frac{\cosh x}{\sinh x} \\ \operatorname{sech} x &= \frac{1}{\cosh x} & \operatorname{csch} x &= \frac{1}{\sinh x} \end{aligned}$$

### Series

$$\begin{aligned} \frac{1}{1-x} &= 1 + x + x^2 + x^3 + \dots, -1 < x < 1 \\ \ln(1+x) &= x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots, -1 < x \leq 1 \\ \tan^{-1} x &= x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \dots, -1 \leq x \leq 1 \\ e^x &= 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots \\ \sin x &= x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots \\ \cos x &= 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots \\ \sinh x &= x + \frac{x^3}{3!} + \frac{x^5}{5!} + \frac{x^7}{7!} + \dots \\ \cosh x &= 1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \frac{x^6}{6!} + \dots \\ (1+x)^p &= 1 + \binom{p}{1}x + \binom{p}{2}x^2 + \binom{p}{3}x^3 + \dots, -1 < x < 1 \\ \binom{p}{k} &= \frac{p(p-1)(p-2)\dots(p-k+1)}{k!} \end{aligned}$$

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## GEOMETRY



Right triangle

### Triangles

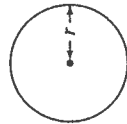
Pythagorean Theorem

$$a^2 + b^2 = c^2$$



Any triangle

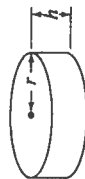
$$\begin{aligned} \text{Angles } \alpha + \beta + \gamma &= 180^\circ \\ \text{Area } A &= \frac{1}{2}bh \end{aligned}$$



### Circles

Circumference  $C = 2\pi r$

Area  $A = \pi r^2$



### Cylinders

Surface area  $S = 2\pi r^2 + 2\pi rh$

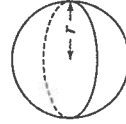
Volume  $V = \pi r^2 h$



### Cones

Surface area  $S = \pi r^2 + \pi r \sqrt{r^2 + h^2}$

Volume  $V = \frac{1}{3}\pi r^2 h$



### Spheres

Surface area  $S = 4\pi r^2$

Volume  $V = \frac{4}{3}\pi r^3$

## CONVERSIONS

- 1 inch = 2.54 centimeters
- 1 liter = 1000 cubic centimeters
- 1 kilogram  $\approx$  2.20 pounds
- $\pi$  radians = 180 degrees
- 1 kilometer  $\approx$  0.62 miles
- 1 liter  $\approx$  1.057 quarts
- 1 pound  $\approx$  453.6 grams
- 1 cubic foot  $\approx$  7.48 gallons

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## INTEGRALS

1.  $\int u \, dv = uv - \int v \, du$
2.  $\int u^n \, du = \frac{1}{n+1} u^{n+1} + C, n \neq -1$
3.  $\int \frac{1}{u} \, du = \ln|u| + C$
4.  $\int e^u \, du = e^u + C$
5.  $\int a^u \, du = \frac{a^u}{\ln a} + C$
6.  $\int \sin u \, du = -\cos u + C$
7.  $\int \cos u \, du = \sin u + C$
8.  $\int \sec^2 u \, du = \tan u + C$
9.  $\int \csc^2 u \, du = -\cot u + C$
10.  $\int \sec u \tan u \, du = \sec u + C$
11.  $\int \csc u \cot u \, du = -\csc u + C$
12.  $\int \tan u \, du = -\ln|\cos u| + C$
13.  $\int \cot u \, du = \ln|\sin u| + C$
14.  $\int \sec u \, du = \ln|\sec u + \tan u| + C$
15.  $\int \csc u \, du = \ln|\csc u - \cot u| + C$
16.  $\int \frac{1}{\sqrt{a^2 - u^2}} \, du = \sin^{-1} \frac{u}{a} + C$
17.  $\int \frac{1}{a^2 + u^2} \, du = \frac{1}{a} \tan^{-1} \frac{u}{a} + C$
18.  $\int \frac{1}{a^2 - u^2} \, du = \frac{1}{2a} \ln \left| \frac{u+a}{u-a} \right| + C$
19.  $\int \frac{1}{u\sqrt{u^2 - a^2}} \, du = \frac{1}{a} \sec^{-1} \left| \frac{u}{a} \right| + C$

Formula Card  
to accompany

# CALCULUS, 9/E

Varberg, Purcell, and Rigdon

## DERIVATIVES

- |  |  |
|--|--|
| $D_x x^n = nx^{n-1}$                       | $D_x  x  = \frac{ x }{x}$                      |
| $D_x \sin x = \cos x$                      | $D_x \cos x = -\sin x$                         |
| $D_x \tan x = \sec^2 x$                    | $D_x \cot x = -\csc^2 x$                       |
| $D_x \sec x = \sec x \tan x$               | $D_x \csc x = -\csc x \cot x$                  |
| $D_x \sinh x = \cosh x$                    | $D_x \cosh x = \sinh x$                        |
| $D_x \tanh x = \text{sech}^2 x$            | $D_x \text{sech } x = -\text{sech } x \tanh x$ |
| $D_x \ln x = \frac{1}{x}$                  | $D_x \text{csch } x = -\text{csch } x \coth x$ |
| $D_x e^x = e^x$                            | $D_x \log_a x = \frac{1}{x \ln a}$             |
| $D_x \sin^{-1} x = \frac{1}{\sqrt{1-x^2}}$ | $D_x \cos^{-1} x = \frac{-1}{\sqrt{1-x^2}}$    |
| $D_x \tan^{-1} x = \frac{1}{1+x^2}$        | $D_x \sec^{-1} x = \frac{1}{ x \sqrt{x^2-1}}$  |