Math5700 Inequalities Homework Spring, 2017

A. Solve these inequalities.

(1)
$$|4-2x|+1 \ge 11$$

(2)
$$(y+4)^4+5<0$$

(3)
$$\frac{2x^2 + 10x - 16}{x - 4} \le 3$$

(4)
$$\log_4(w-1)^4 + 2 \le \log_4(2w-2)$$

(5)
$$\log_4(w-1)^3+2 \le \log_4(2w-2)$$

(6)
$$-2(9^{x^6-1}) \ge 36$$

(7)
$$x(2x-1)(x-3)^2 < 0$$

(8)
$$\frac{1}{x+2} \ge \frac{2}{x-2}$$

B. If you're given this inequality $\frac{13}{31} < \frac{8}{19}$ and you need to verify if it is in fact correct, how would you explain this to your students (without a calculator)? And, would it be reasonable to "cross multiply" to check the validity of the statement? Why or why not?

What if the inequality is
$$-\frac{13}{31} < -\frac{8}{19}$$
 instead?

What if the inequality is
$$\frac{13}{31} < \frac{8}{19x}$$
 instead?

C. In which setting or under what conditions do you need to consider different cases in solving an inequality?