### 2.1 Numeration Systems

Number--an idea that represents a quantity.

## Number uses:

1. 
2. 
3. 

Natural numbers $=$

Whole numbers $=$

## Historical Numeration Systems:

## 1. Tally System

## Positive Characteristics/Benefits:

2. Egyptian System

Decimal Egyptian Number Symbol

## Positive Characteristics/Benefits:

$$
\begin{aligned}
& 1=\| \text { staff } \\
& 10=\prod \text { heel bone } \\
& 100=9 \text { coil of rope } \\
& 1000=\mathbf{z}^{\mathbf{8}} \text { lotus flower } \\
& 10,000=/ 7 \text { pointing finger } \\
& 100,000=\sim \text { tadpole } \\
& 1,000,000=\text { astonished man }
\end{aligned}
$$

Ex 1 What are the values of these numbers?
(a)

(b)


## 3. Roman Numeral System

| I | V | X | L | C | D | M |
| :--- | :---: | :--- | :--- | :--- | :--- | :--- |
| 1 | 5 | 10 | 50 | 100 | 500 | 1000 |
| Example: |  |  |  |  |  |  |
| XXXII $=32$ |  | XLVII $=48$ |  |  |  |  |

## Positive Characteristics/Benefits:

| I | 1 |
| :--- | ---: |
| II | 2 |
| III | 3 |
| IV | 4 |
| V | 5 |
| VI | 6 |
| VII | 7 |
| VIII | 8 |
| IX | 9 |
| X | 10 |
| XI | 11 |
| XII | 12 |
| XIII | 13 |
| XIV | 14 |
| XV | 15 |
| XVI | 16 |
| XVII | 17 |
| XVIII | 18 |
| XIX | 19 |
| XX | 20 |


| XXI | 21 |
| :--- | :--- |
| XXII | 22 |
| XXIII | 23 |
| XXIV | 24 |
| XXV | 25 |
| XXVI | 26 |
| XXVII | 27 |
| XXVIII | 28 |
| XXIX | 29 |
| XXX | $\mathbf{3 0}$ |
| XXXI | $\mathbf{3 1}$ |
| XXXII | $\mathbf{3 2}$ |
| XXXIII | $\mathbf{3 3}$ |
| XXXIV | $\mathbf{3 4}$ |
| XXXV | $\mathbf{3 5}$ |
| XXXVI | $\mathbf{3 6}$ |
| XXXVII | $\mathbf{3 7}$ |
| XXXVIII | $\mathbf{3 8}$ |
| XXXIX | $\mathbf{3 9}$ |
| XL | $\mathbf{4 0}$ |


| XLI | 41 |
| :--- | :--- |
| XLII | 42 |
| XLIII | 43 |
| XLIV | 44 |
| XLV | 45 |
| XLVI | 46 |
| XLVII | 47 |
| XLVIII | 48 |
| XLIX | 49 |
| L | 50 |
| LI | 51 |
| LII | 52 |
| LIII | 53 |
| LIV | 54 |
| LV | 55 |
| LVI | 56 |
| LVII | 57 |
| LVIII | 58 |
| LIX | 59 |
| LX | 60 |


| LXI | 61 | LXXXI | 81 |
| :---: | :---: | :---: | :---: |
| LXII | 62 | LXXXII | 82 |
| LXIII | 63 | LXXXIII | 83 |
| LXIV | 64 | LXXXIV | 84 |
| LXV | 65 | LXXXV | 85 |
| LXVI | 66 | LXXXVI | 86 |
| LXVII | 67 | LXXXVII | 87 |
| LXVIII | 68 | LXXXVIII | 88 |
| LXIX | 69 | LXXXIX | 89 |
| LXX | 70 | XC | 90 |
| LXXI | 71 | XCI | 91 |
| LXXII | 72 | XCII | 92 |
| LXXIII | 73 | XCIII | 93 |
| LXXIV | 74 | XCIV | 94 |
| LXXV | 75 | XCV | 95 |
| LXXVI | 76 | XCVI | 96 |
| LXXVII | 77 | XCVII | 97 |
| LXXVIII | 78 | XCVIII | 98 |
| LXXIX | 79 | XCIX | 99 |
| LXXX | 80 | C | 100 |
|  |  | D | 500 |
|  |  | M | 1000 |

## 4. Babylonian Numeration System

## Positive Characteristics/Benefits:

$V$One


Ten

5. Mayan Numeration System

## Positive Characteristics/Benefits:



## Two examples:

(a)

- $20^{2}$ place
2007
(b)


6. Hindu-Arabic Numeration System (our current system)

Positive Characteristics/Benefits:

## Other Bases

## We still have place value!!!

## Base 5:

## Ex Convert 12 to base 10.

Ex Convert $341_{5}$ to base 10.

Ex Convert 39 to base 5.

Ex Convert 401 to base 5.

Convert these numbers to base 10.
(a) $1011101_{2}$
(b) $1237_{8}$
(c) $2 E T_{12}$
(d) $654_{7}$

Convert these numbers from base 10 to the indicated base.
(a) 76 to base 2
(b) 982 to base 4
(c) 131 to base 3
(d) 519 to base 8

