Different Interpretations of Trigonometric Functions, Fall 2014

|  | Setting/Picture | $\cos (\theta)$ | $\sin (\theta)$ | Other trig functions | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A. | Unit Circle, ( $a, b$ ) is the point where the angle intersects the unit circle | input: angle in standard position output: a (the x-coordinate) | input: angle in standard position output: $b$ (the y-coordinate) | Obtained from sine and cosine: $\begin{aligned} & \tan \theta=\frac{\sin \theta}{\cos \theta} \\ & \cot \theta=\frac{\cos \theta}{\sin \theta} \\ & \sec \theta=\frac{1}{\cos \theta} \\ & \csc \theta=\frac{1}{\sin \theta} \end{aligned}$ | A. is like B. with $\mathrm{r}=1$ |
| B. | Circle with center $(0,0)$, radius $r$. $(a, b)$ is the point where the angle intersects the circle | input: angle in standard position output: the ratio $\frac{a}{r}=\frac{\mathrm{x}-\text { coord. of point }}{\text { radius of circle }}$ | input: angle in standard position output: the ratio $\frac{b}{r}=\frac{\mathrm{y}-\text { coord. of point }}{\text { radius of circle }}$ | Ratios of $\mathrm{x}-, \mathrm{y}$ coordinates and/or the radius of the circle: $\begin{aligned} \tan \theta & =\frac{b}{a} \\ \cot \theta & =\frac{a}{b} \\ \sec \theta & =\frac{r}{a} \\ \csc \theta & =\frac{r}{b} \end{aligned}$ | B. is like C, but you need to add the sign based on which quadrant the terminal side of the angle is in. |
| C. | Right Triangle | input: an angle between 0 and $90^{\circ}$ <br> output: ratio of sides of a right triangle, $\frac{\text { adj }}{\text { hyp }}$ | input: an angle between 0 and $90^{\circ}$ output: ratio of sides of a right triangle $\frac{\text { opp }}{\text { hyp }}$ | Ratios of sides of the triangle: $\begin{aligned} & \tan \theta=\frac{\text { opp }}{\text { adj }} \\ & \cot \theta=\frac{\text { adj }}{\text { opp }} \\ & \sec \theta=\frac{\text { hyp }}{\text { adj }} \\ & \csc \theta=\frac{\text { hyp }}{\text { opp }} \end{aligned}$ | C. is like B. with all triangles in Quadrant 1 |
| D. | Graph on coordinate | input: any real number <br> output: the real number obtained by computing cosine (use method A.) of $\theta$ radians | Similar to cosine | Similar to cosine |  |

