MATH 1030-004, Quiz 5 Solution

1. (4 pts) Draw a set of axes in the coordinate plane, and then plot and label the following points: a = (-2, 3), b = (1, 3), c = (3, -1), d = (0, -2).



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- 2. Suppose your pet dog weighed 2 pounds at birth, and weighed 10 pounds after two years.
 - (a) **(3 pts)** Based on these two data points find a linear function that describes how weight varies with age.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{10 - 2}{2 - 0} = 4.$$

Since one of the points is (0, 2), the *y*-intercept is b = 2, so the equation becomes

$$y = 4x + 2.$$

(b) (3 pts) Use this function to find how much your dog will weigh when it's 5 years old?

$$y = 4 \cdot 5 + 2 = 22.$$

- 3. A snowplow has a maximum speed of 30 miles per hour on a dry highway. Its maximum speed decreases by 1.2 miles per hour for every inch of snow on the highway.
 - (a) (3 pts) Write a linear function to model the situation described.

Here the y-intercept is b = 30, and the rate of change (the slope) is m = -1.2. So the equation becomes

$$y = -1.2x + 30.$$

(b) (3 pts) Use this function to find how deep the snow is if the snowplow's maximum speed is 8 miles per hour.

$$8 = -1.2 \cdot x + 30$$

1.2 \cdot x = 30 - 8
$$x = \frac{22}{1.2} = 18.33.$$

4. (Extra Credit: 4 pts) Solve for x in $12^{x/4} = 1,000$. (*Hint:* $\log_{10} a^b = b \cdot \log_{10} a$.)

We just take log of both sides:

$$\log_{10} \left(12^{x/4} \right) = \log_{10} 1,000$$
$$\frac{x}{4} \cdot \log_{10} 12 = 3$$
$$x = \frac{4 \cdot 3}{\log_{10} 12} = 11.12.$$