

Math 4200-001
Week 10 concepts and homework
3.2-3.3
Due Wednesday November 6 at start of class.

3.3 1ab, 4, 6, 8, 13, 15, 17, 18, 19, 20

w10.1 Let f be an entire function. Suppose $f\left(\frac{1}{n}\right) = \frac{1}{n^2}$ for all positive integers n . Is it possible for $f(-1)$ to equal -1 ? Explain.

w10.2) Use power series or L'Hopital's rule to find

$$\lim_{z \rightarrow 0} \frac{\cos(z) - 1}{z \sin(z)}$$

w10.3) Continuing the text problem 3.3.4, find the Laurent series for

$$\frac{1}{z(z-1)(z-2)}$$

valid for $|z| > 2$.

w10.4) Which of these functions has a removable singularity at $z = 0$?

a) $\frac{\cos(z) - 1}{z \sin(z)}$ (see w10.2)

b) $\frac{\cos(z) - 1}{z^3}$.