Name_____

Student I.D._____

Math 2250-4 Quiz 12 April 20, 2012

1) Find the general solution $[x_1(t), x_2(t)]^T$ to the homogeneous system of second order differential equations, which could result from two masses coupled together with springs:

$$x_1''(t) = -3 x_1 + x_2$$

$$x_2''(t) = 2 x_1 - 2 x_2.$$

(8 points)

2) Use Newton's second law to derive the system of differential equations above, from the configuration below. $x_1(t), x_2(t)$ are the displacements from equilibrium of two masses. The mass values and spring constants are as shown.

(2 points)

$$m_1 = 2$$

$$k_1 = 4 \quad N/m$$

$$m_2 = 1$$

$$k_2 = 2 \quad N/m$$

$$m_2 = 1$$

$$k_3 \quad \int x_2(t)$$