

Name _____
Student I.D. _____

Math 2250-1

Quiz 4

September 14, 2012

1) Consider the following linear drag initial value problem:

$$\frac{dv}{dt} = 6 - 0.2 v .$$

$$v(0) = 0 .$$

1a) Use a phase diagram to determine the limiting velocity $\lim_{t \rightarrow \infty} v(t)$ for the solution to this IVP.

(2 points)

1b) Solve the initial value problem above. (Your solution should be consistent with the correct answer to part (a) above.)

(6 points)

1c) Use Newton's Law to convert the following information below into a differential equation initial value problem - your IVP should end up being equivalent to the IVP at the top of this page, if you keep track of your units correctly.

A small motor boat and its pilot weigh a total of 640 lbs. The motor provides a thrust force of 120 lbs. The drag from the boat depends on the velocity v of the boat, and is 4 lbs for each ft/sec of velocity v . Aside from the motor and the drag forces, there are no other forces acting on the boat, and the boat starts from rest. Hint: recall that in the English system every 32 pounds of force $= mg$ corresponds to 1 slug of mass.

(2 points)