

Math 2250–1

Week 12 concepts and homework, due November 18.

Recall that problems which are underlined are good for seeing if you can work with the underlying concepts; that the underlined problems are to be handed in; and that the Friday quiz will be drawn from all of these concepts and from these or related problems.

10.4: using convolution integrals to find inverse Laplace of $F(s)G(s)$; using the differentiation theorem to find the Laplace transform of $t \cdot f(t)$; using these (and other) techniques to solve linear differential equations.

10.4: 2, 3, 9, 10, 15, 16, 29, 30, 37, 38

10.5: using the unit step function to turn forcing on and off; Laplace transform of non-sinusoidal periodic functions

10.5: 3, 7, 11, 13, 25, 31, 26, 34

w12.1) Solve this initial value problem and then sketch the solution. Explain what happens. The forcing term is a sum of instantaneous unit impulses, as discussed in EP7.6 and Monday's class notes.

$$\begin{aligned}x''(t) + 4x(t) &= \delta(t - \pi) - \delta(t - 3\pi). \\x(0) &= 0 \\x'(0) &= 0\end{aligned}$$

6.1: finding eigenvalues and eigenvectors (or a basis for the eigenspace if the eigenspace is more than one-dimensional).

6.1: 7, 8, 17, 18, 20, 24

6.2: diagonalizability: recognizing matrices for which there is an eigenbasis, and those for which there is not one. Writing the eigenbasis equation as $AP = PD$ where P is the matrix of eigenvector columns, and D is the diagonal matrix of eigenvalues.

6.2: 4, 10, 28 In 4, 10, 28, make sure to verify that $AP = PD$ in the cases that A is diagonalizable.

w12.2)

a) Using your work in 6.1.20, verify that $AP = PD$ for the matrix A in that problem.

b) Explain what happens if you re-order the eigenvector columns of P , and why.