

- Go over the murder mystery on page 3 of Monday's notes - Hopefully you worked this out yesterday after class.
- Discuss oscillation (3) & projectiles (4) on page 2 Monday notes.

§1.2 1<sup>st</sup> order DE's you solve by antidifferentiation

$$\frac{dy}{dx} = f(x) \quad \xrightarrow{\text{sol'n}} \quad y = \int f(x) dx$$

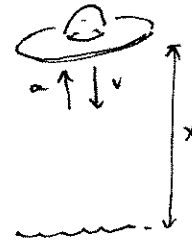
↑  
y does not  
appear on RHS

example 1 Solve the initial value problem

$$\text{IVP} \begin{cases} \frac{dy}{dx} = x - 3 \\ y(1) = 2 \end{cases}$$

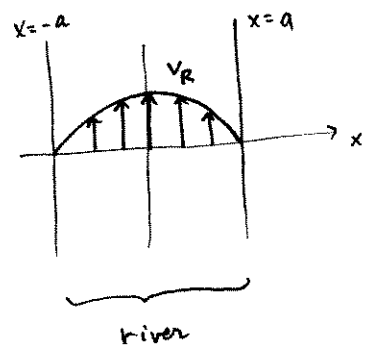
ans.  $y = \frac{x^2}{2} - 3x + \frac{9}{2}$

example 2: p. 12-13 text: lunar lander problem

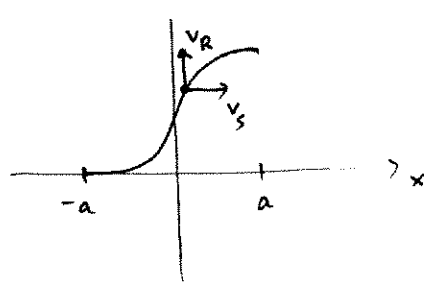


velocity to moon is  
450 m/s.  
retro-rockets provide  
deceleration of  
2.5 m/s<sup>2</sup>.  
At what height to  
fire rockets to  
get soft landing, i.e.  
 $v=0$  exactly when  
height  $x=0$ ?

example 3 (actually example 4, the swimmer's problem, page 15)



$v_R = v_0 \left(1 - \frac{x^2}{a^2}\right)$  is velocity profile of river water



swimmer swims due east with constant velocity  $v_s$ .  
she starts at  $(-a, 0)$ .

find the function  $y = f(x)$  whose graph is describing her route!!

then, if  $\phi$  river is 1 mile wide  
 if  $v_s = 3$  mi/h (this is a very good swimmer)  
 $v_0 = 9$  mi/h (pretty fast river)

where does swimmer land on opposite shore?

example 4

The velocity  $v = \frac{dx}{dt}$  of a car traveling along the x-axis is shown in the following graph. The car starts at  $x_0 = 0$ .

Sketch the graph of its location at time  $t$  (and, find a formula for  $x(t)$ !)  
How far did the car travel,  $0 \leq t \leq 3$  minutes?

