

Exam Review (Exam is Friday, in class. Closed book & note. No graphing calculators allowed. I'll provide you with the book's integral tables - you should know basic integrals & method of substitution.)

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Double & Triple integrals

- Riemann sums \rightarrow integrals are limits of these, so understanding of what integrals mean (area, volume, mass, moments, etc.) is based on finite Riemann sums.
- Computing iterated integrals (by partial integration) (relatively "easy")
- Converting a description of a region into an "iteration", so that you can write down iterated integrals for functions defined on that region (and vice-verse!) (harder!)
- change of variables to polar, cylindrical, or spherical coords
- applications
 - mass (2-d, 3-d regions); includes area & volume
 - center of mass (for 2-d, 3-d regions) (centroid)
 - moments of inertia (3-d regions)
 - Surface area (for surfaces in space)

Know

$$dA = r dr d\theta$$

$$dV = r dr d\theta dz$$

$$dV = \rho^2 \sin\phi d\rho d\phi d\theta$$

Sample test Not inclusive!

- Compute $\iint_R f dA$ if $f(x,y) = xy$ and R is the rectangle $1 \leq x \leq 2$ $0 \leq y \leq 2$
 - Change limits (by first sketching region), and then evaluate $\int_0^4 \int_{\sqrt{y}}^2 \frac{ye^{x^2}}{x^3} dx dy$
- Consider the pyramid in the first octant bounded by the three coord planes and the skew plane $x+2y+3z=6$
 - Find its volume with a triple integral
 - Find the x-coord of its centroid (assume density = 1).
- Let D be the disk of radius 2 centered at the origin. Find $\iint_D \frac{1}{1+x^2+y^2} dA$

Know all formulas

$$A = \iint_R 1 dA, \quad V = \iiint_R 1 dV$$

$$m = \iint_R \delta dA \quad \text{or} \quad \iiint_R \delta dV$$

$$\bar{x} = \frac{1}{m} \iint_R x \delta A \quad (\text{or } \frac{1}{m} \iiint_R x \delta dV)$$

$$\bar{y} =$$

$$\bar{z} =$$

$$I_z = \iiint_R (x^2 + y^2) dV$$

$$A = \iint_{u-v \text{ region}} |\vec{x}_u \times \vec{x}_v| du dv$$

for $\vec{x}\left(\begin{matrix} u \\ v \end{matrix}\right) = \begin{bmatrix} x \\ y \\ f(x,y) \end{bmatrix}$

becomes

$$A = \iint_{x-y \text{ region}} \sqrt{1 + f_x^2 + f_y^2} dx dy$$