

Math 2210-1
Wed Nov. 3

HW for 11/10

14.3 7, 10, 14, 20, 27, 30, 37, 41
14.4 4, 5, 13, 14, 23, 24, 29, 41
14.5 11, 13, 41, 42, 45, 46, 51

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Redo your exams!

- neatly, on separate sheets, attach to original exam.
- hand back in on Monday (11/8), at start of class
- use book, notes, etc., but work on your own. (Discuss concepts or related problems with friends if you wish.)
- you can earn back up to $\frac{1}{2}$ of the points you lost.

§ 14.3 Area and volume by double integration

Explain: (using Riemann sum def of integral)

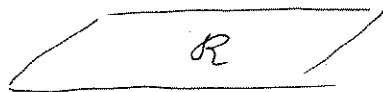
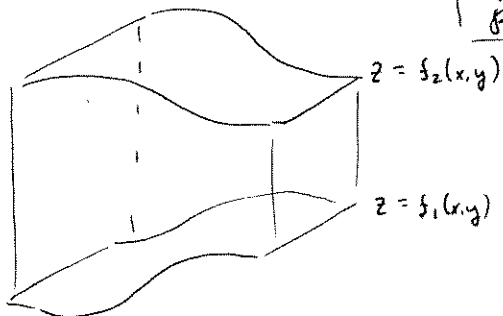
- If R is a region in the plane, then its area is $\boxed{\iint_R 1 \, dA}$

- If R is a region in the plane
and $z = f_1(x, y)$
 $z = f_2(x, y)$ $f_1 \leq f_2$

are two graphs over R

then the volume between the two graphs

is $\boxed{\iint_R [f_2(x, y) - f_1(x, y)] \, dA}$



example (#2, p 1011).

Find the area of the region in the x - y plane
 bounded between $y = x^2 - 2x$ (ans = $9/2$)
 and $y = x$.

example (#4, p 1012)

Let R be the region between
 $y = x^2$
 $y = 2 - x^2$

Let $f_1(x, y) = 2y$
 $f_2(x, y) = 6$

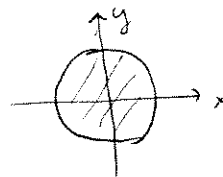
Sketch region (volume)
 between graphs of f_1 & f_2

Find volume.

(Ans = $\frac{32}{3}$)

Conceptual questions (p. 1012)

Deduce - without actual explicit computation - the following double integral values. Explain.



The region R is the unit disk $x^2 + y^2 \leq 1$ in each case.

$$1. \iint_R \sqrt{1-x^2-y^2} \, dA$$

$$2. \iint_R (10 - x + y) \, dA$$

$$3. \iint_R (1 - \sqrt{x^2+y^2}) \, dA$$

$$4. \iint_R \sqrt{x^2+y^2} \, dA \quad (\text{use 3!})$$

$$5. \iint_R 5 - x^2 \sin x + y^3 \cos y \, dA.$$