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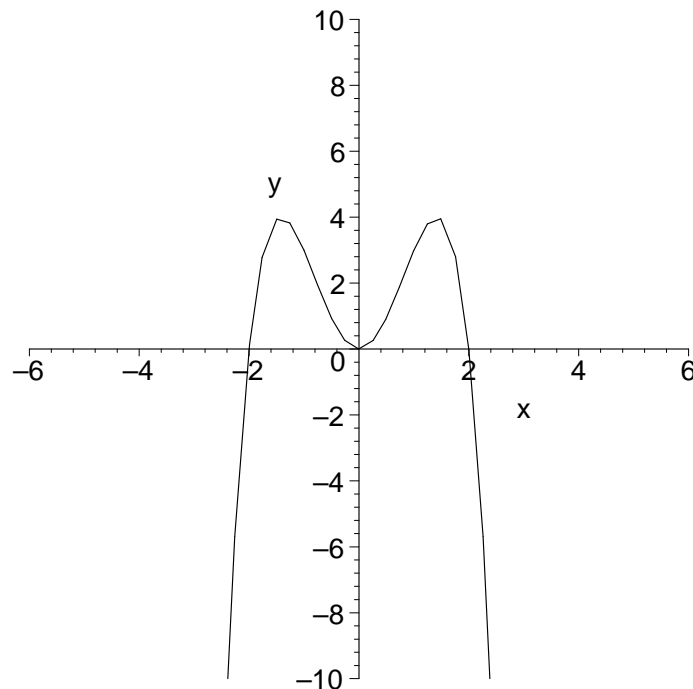
**Math 1210-3**

**Quiz 3**

January 25, 2008

Show all work for complete credit! There are two sides to this quiz!

Here is a computer sketch of the graph  $y = f(x)$ , for the polynomial function  $f(x) = -x^4 + 4x^2$ . All the problems on the quiz are related to this particular function and its graph.



1a) How is the graph of  $y = -2x^4 + 8x^2$  related to the graph of  $y = f(x)$  shown above? Answer this question in words, and then carefully sketch the graph of  $y = -2x^4 + 8x^2$  into the picture above. (2 points)

1b) How is the graph of  $y = -(x+3)^4 + 4(x+3)^2 - 1$  related to the graph of  $y = -x^4 + 4x^2$ ? Answer this question in words, and then carefully sketch the new graph into the picture above. (2 points)

1c) Is the function  $f(x) = -x^4 + 4x^2$  even, odd, or neither? Explain your answer, using the definition of what even or odd means. How is this even or odd property reflected in a symmetry property of the graph  $y = -x^4 + 4x^2$ ?

(2 points)

1d) Let  $g(x) = \sqrt{x}$ , and  $f(x) = -x^4 + 4x^2$  as always. What is the formula for  $g \circ f$ ? What is the natural domain of this new function?

(2 points)

1e) Using the same functions as in part (1d), What is the formula for the function  $g \circ f$ ? What is the natural domain for this new function? (Hint: Let the graph on page one help you.)

(2 points)