Name	
Student I.D.	

Math 1210-3 Final Exam April 29, 2003

Please show all work for full credit. When in doubt as to whether your reasoning is clear, add an explanation. This exam is closed book and closed note, but you may use a scientific calculator. You may not use a calculator which does graphing or symbolic differentiation, however. I have provided you with some integral tables, geometry identities, when all moment formulas. There are 200 points possible, as indicated below and in the exam. You have two hours to complete this exam, so apportion your time accordingly. Good Luck!!

Score	
	POSSIBLE
1	15
2	25
3	30
4	25
5	15
6	30
7	45
8	15
TOTAL	200

1) Compute the following limits 1a)

$$\lim_{x \to 5} \frac{x^2 - 4x - 5}{x^2 - 6x + 5}$$

(5 points)

1b)

$$\lim_{t \to I^+} \frac{t+3}{t-t^2}$$

(5 points)

1c)

$$\lim_{x \to (-\infty)} \frac{3 x^3 - x^2}{5 x^2 + 2 x + x^3}$$

2) Compute the following derivatives

$$D_x \left(12 \, x^3 - 5 \, x^5 + \frac{61}{x^2} \right)$$

(5 points)

$$D_t \left(\frac{t^2}{3 t + 7} \right)$$

(5 points)

$$\left[\frac{d}{dx}\right] \left[\sin(3x+1)\right]^4$$

(5 points)

2d) Suppose f(1)=5, g(1)=-2, f(1)=3, g'(1)=2. Compute the derivative of the function $(f(x)+2g(x))^3$, at x=1.

(10 points)

3) Compute the following integrals

3a)

$$\int 12 u^2 + 3 \cos(u) + \frac{21}{u^3} du$$

(10 points)

3b)

$$\int_{0}^{\frac{1\pi}{4}} \cos(2x) \left[\sin(2x)\right]^{2} dx$$

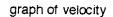
(10 points)

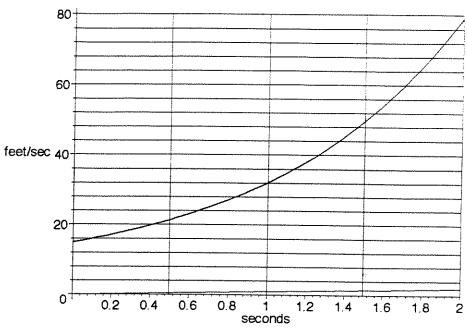
3c)

$$\int_{0}^{2} x \left(x^2 + 1\right)^3 dx$$

(10 points)

4) Here is the graph of the velocity function, for an object moving along a straight line:





Use the velocity graph above to answer the following questions. Make sure to use correct units, and to explain your reasoning:

4a) Estimate the object velocity at time t = 1 second.

(5 points)

4b) Estimate the acceleration of the object at t=1.

4c) About how far does the object travel between t=0 and t=2? Obtain an estimate that within 8 feet or better. Explain.	is accurate to
within 8 feet of better. Explain.	(10 points)
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4d) Estimate the average velocity of the object over the time interval [0,2].	
the time time time time time time time tim	(5 points)

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5) A drinking trough for cattle has a cross section in the form of an isoceles triangle (with the base at the top, of length 4 feet). The triangle's height is 2 feet and the trough is 20 feet long. If water is filling the trough at the rate of 3 cubic feet per minute, then how fast is the water depth increasing, when the depth is one and a half feet?

6)	Consider	the	fun	ction
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$$f(x) = -x^3 + 12x$$

6a) On what intervals is f increasing and decreasing?

(5 points)

6b) On what intervals is f concave up and concave down?

(5 points)

6c) Identify where all local extrema of f occur, find their values, and identify whether they are local maxima or local minima.

(5 points)

(d) Find the x intercepts for the graph of f.

6e) Create an accurate graph for y=f(x), using all of your results from 6a-6d.

(10 points)

7) Consider the region bounded between the curves $y=x^2$ and $y=4$. 7a) Sketch the region. Find the coordinates where the curves cross.	(5 points)
7b) Find the area of the region	(5 points)
7c) Find the centroid of this region.	(15 points)

7d) Use slicing or cylindrical shells to compute the volume of revolution obtained by taking this and rotating it around the line $x=3$.	region
	points)
7e) Check your answer in 7d), by using Pappus' Theorem to recompute the volume of revolution.	
(5 p	oints)

8a) Consider the line segment $y = \frac{1}{2}x$, for x in the interval [0, 2]. Rotate this line segment about the x-axis, to obtain a cone surface. Write down and evaluate the definite integral for this surface's area. (10 points)

8b) Check your answer to 8a) by using the area for cone surfaces which you can deduce from your geometry table.